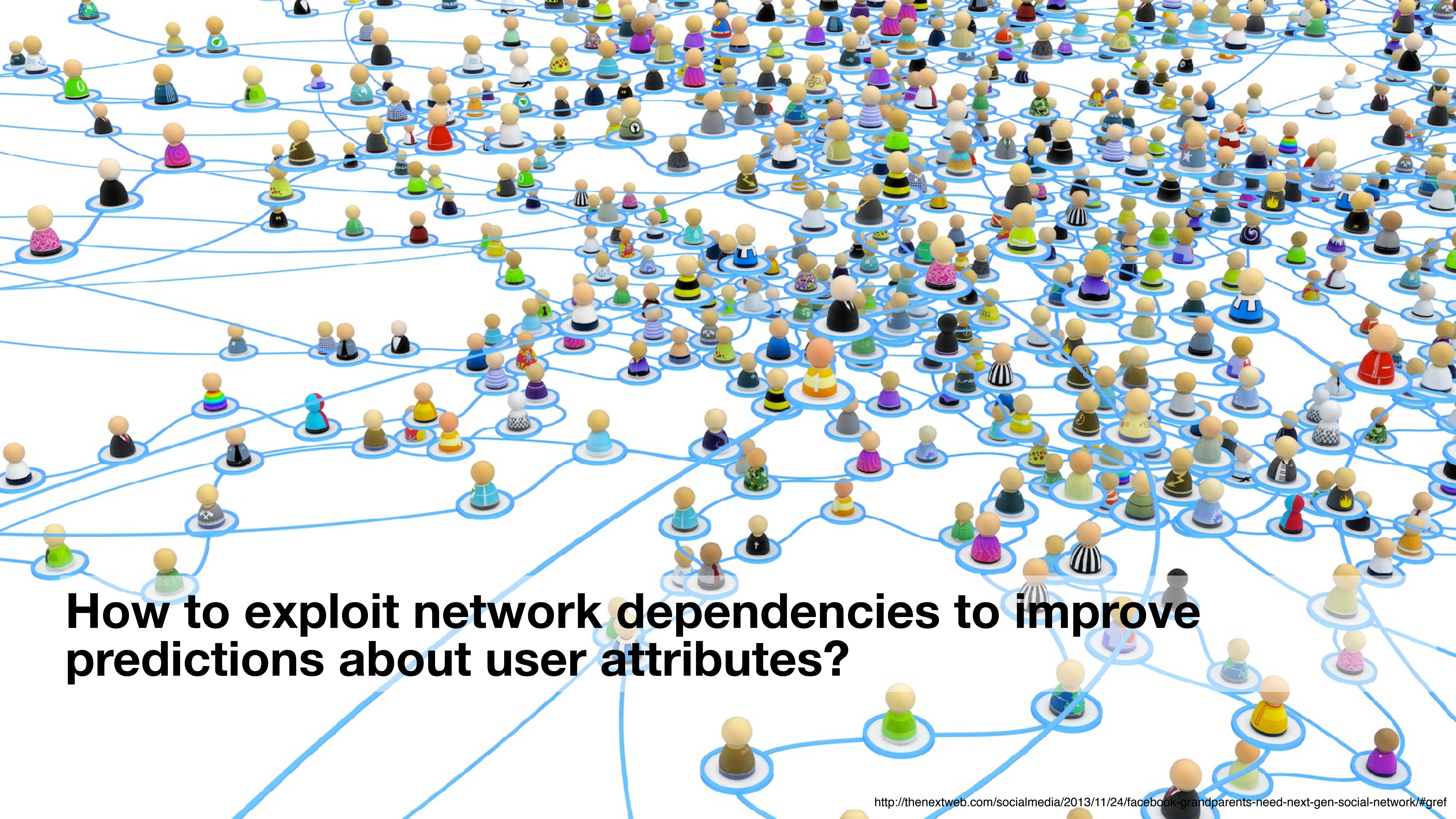




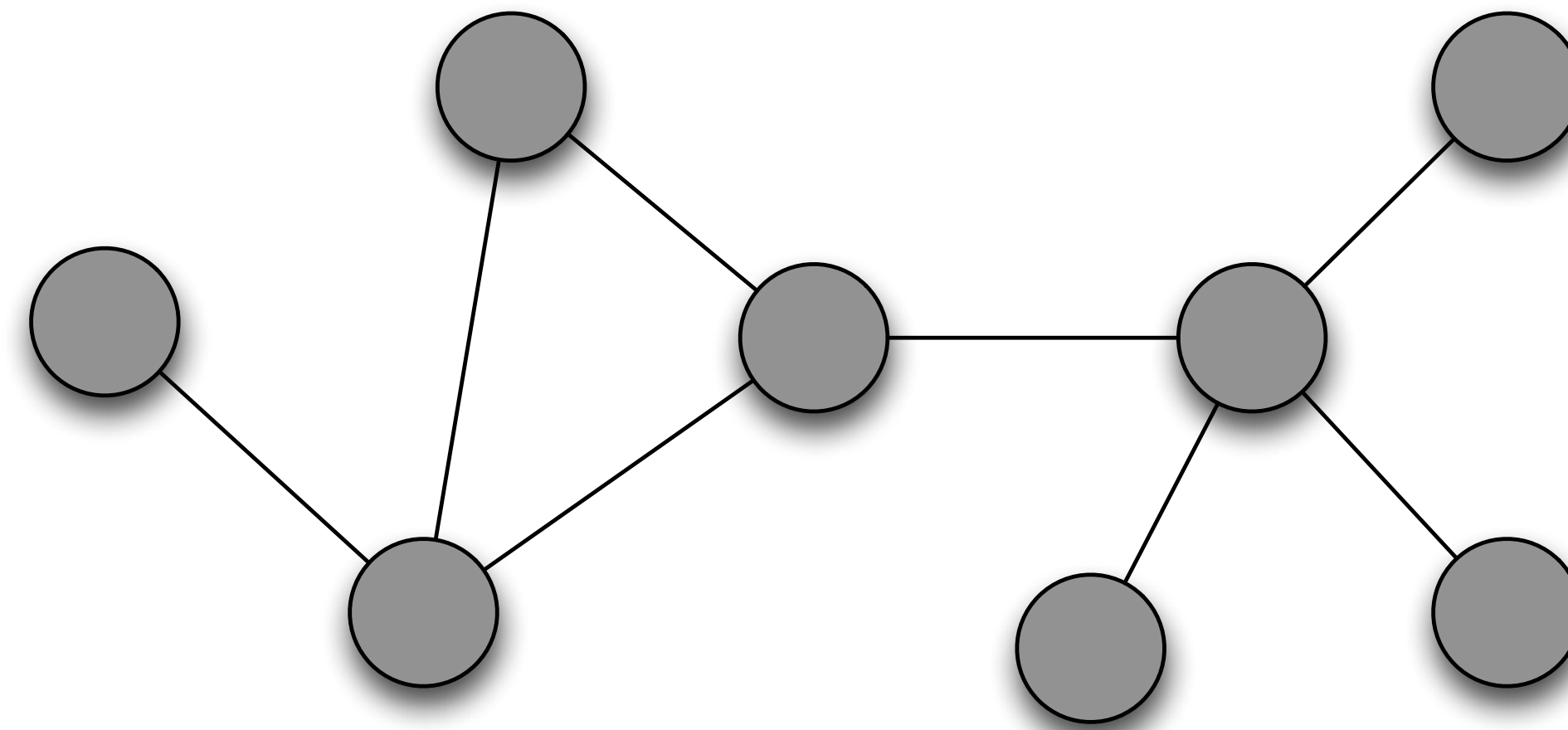
# Deep Learning for Relational Networks

Jennifer Neville  
Departments of Computer Science and Statistics  
Purdue University

*(joint work with Dan Goldwasser, Yi-Yu Lai, Changping Meng, John Moore,  
S Chandra Mouli, and Bruno Ribeiro)*



# How to exploit network dependencies to improve predictions about user attributes?

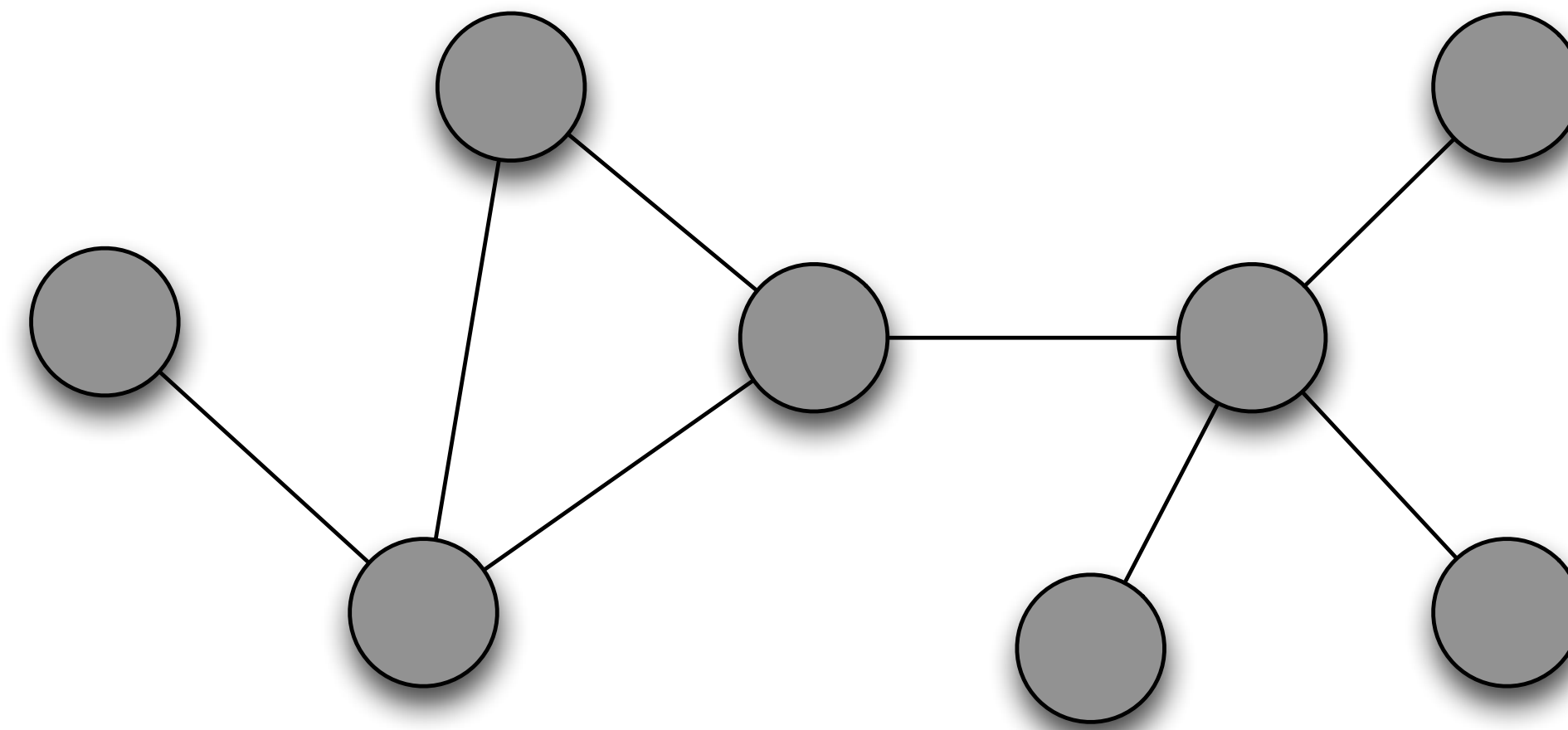


Data network

$$G = (V, E)$$

$V := users$

$E := friendships$

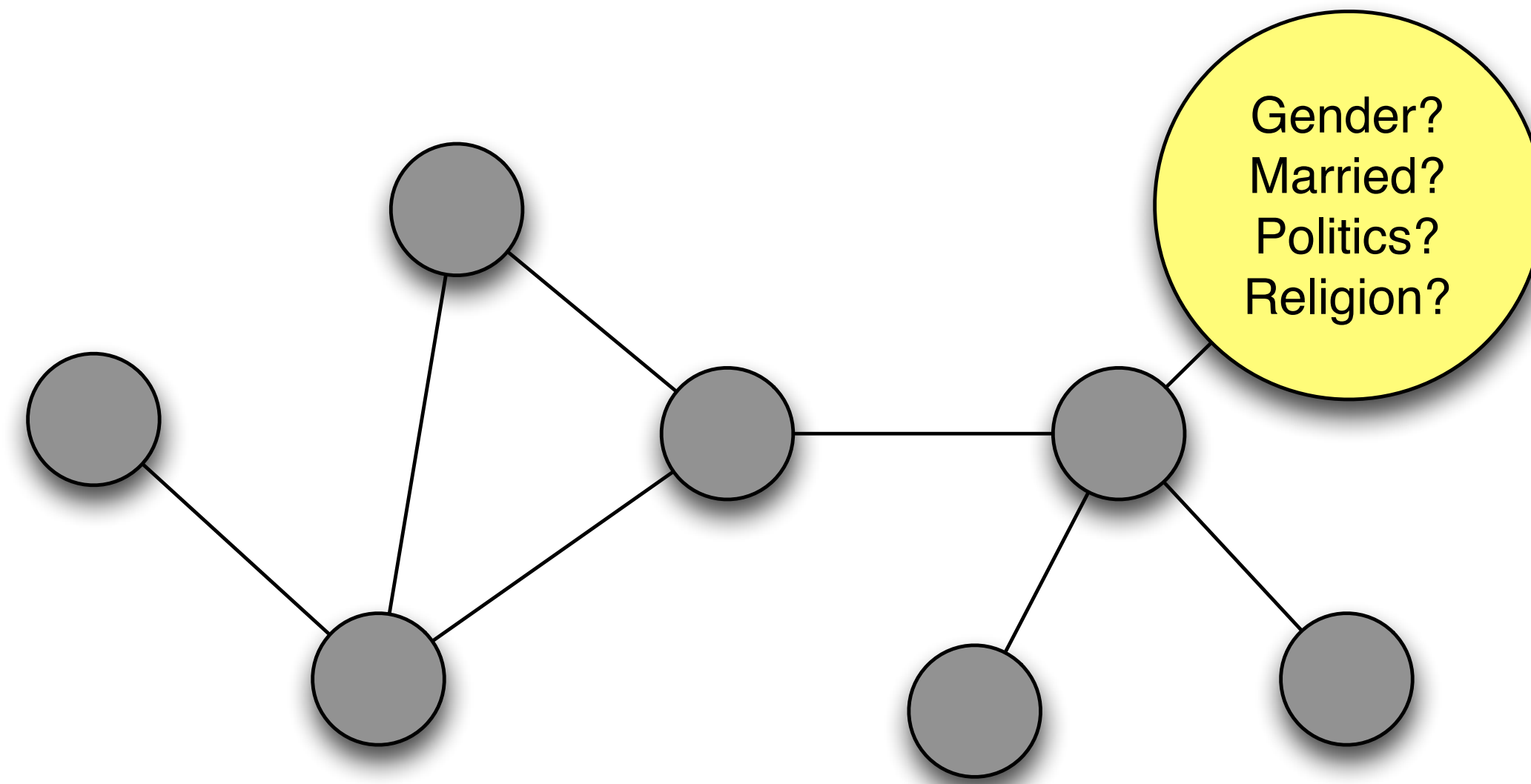


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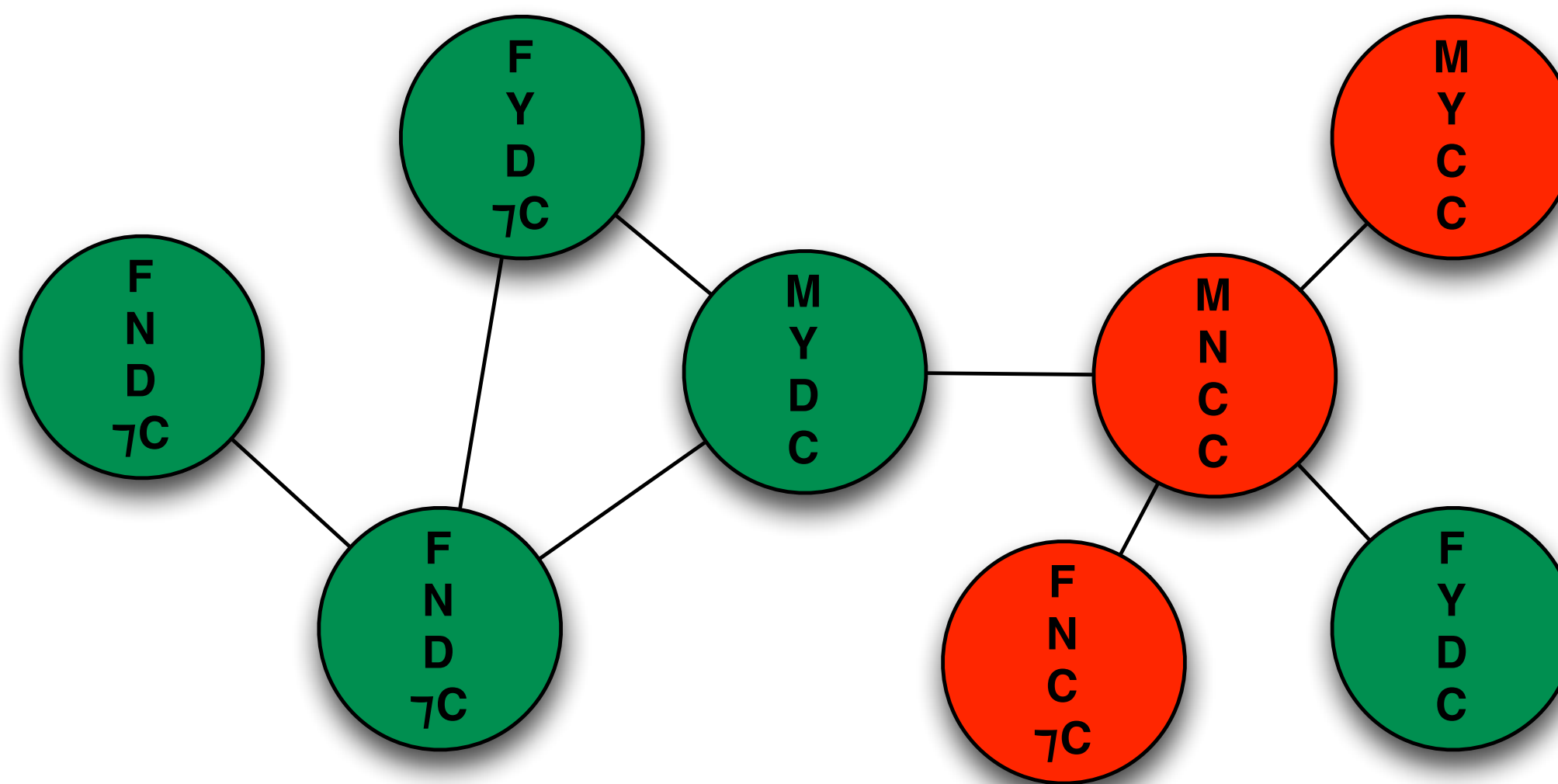


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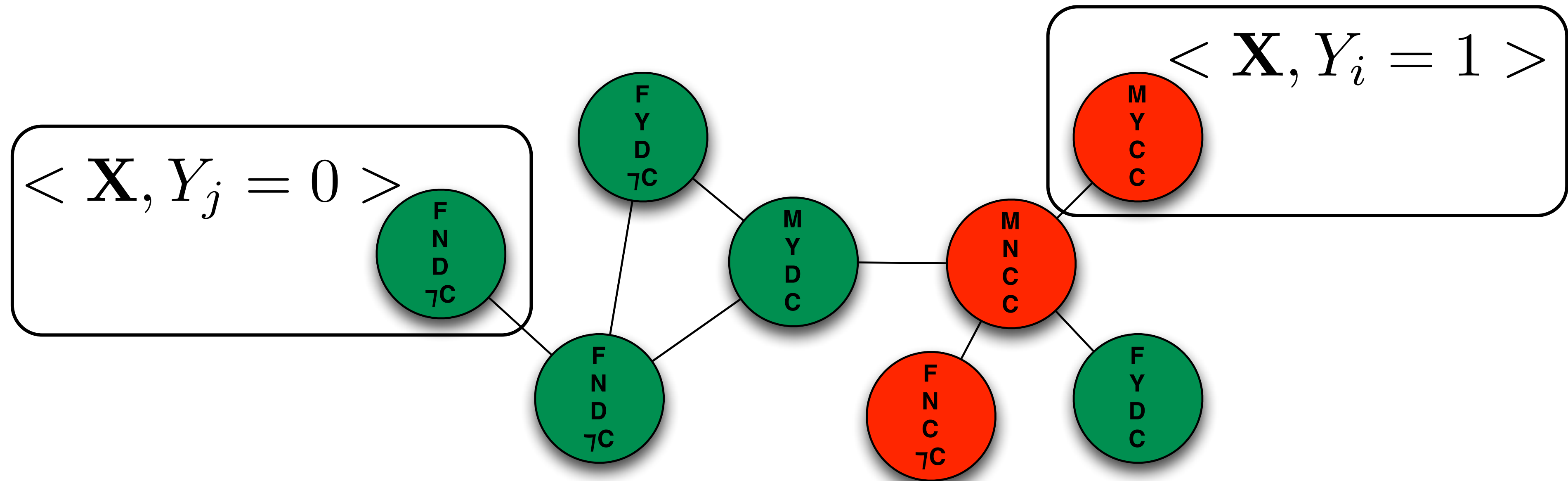


Attributed network

$$G = (V, E)$$

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$E := friendships$



$$G = (V, E)$$

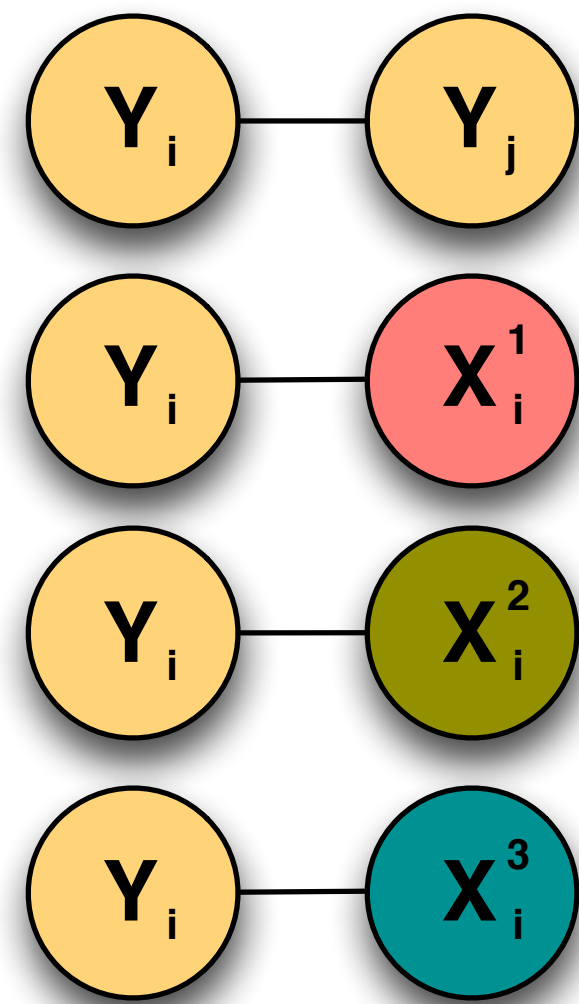
$V := users$

$E := friendships$

*For prediction:* estimate joint distribution of class labels (**Y**) over network

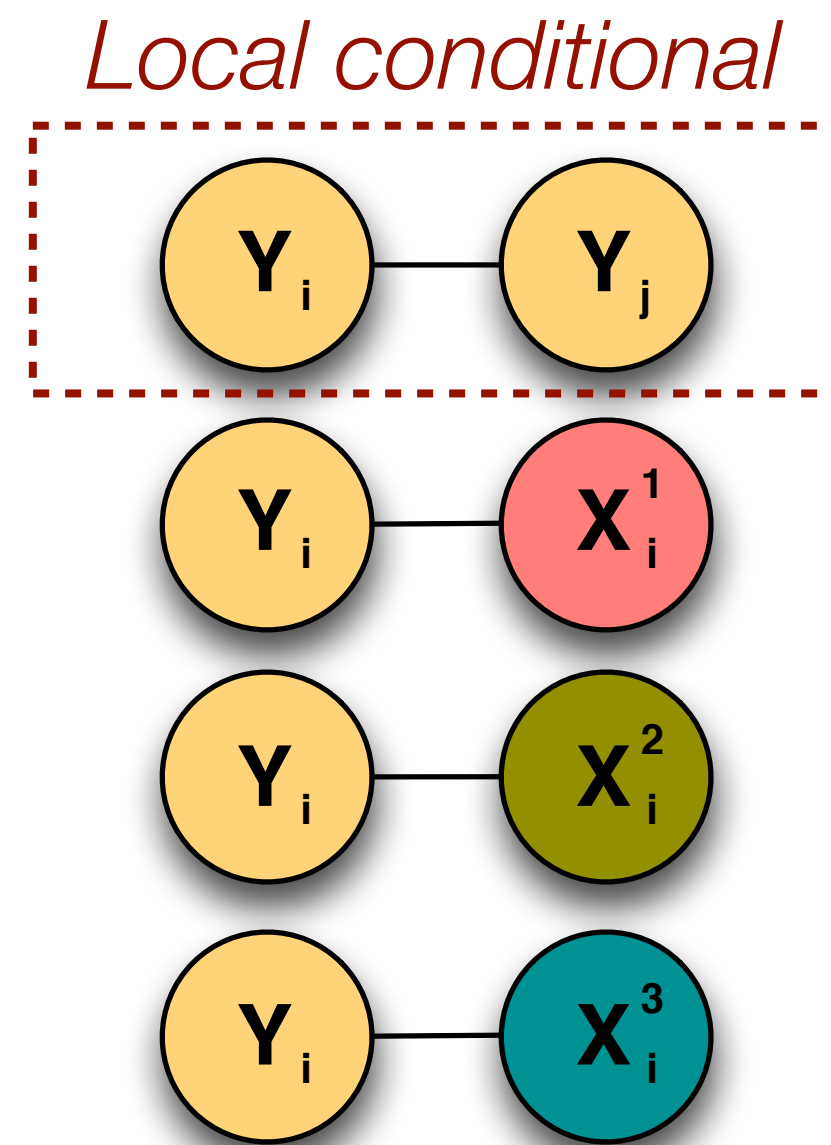


**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions



Model template

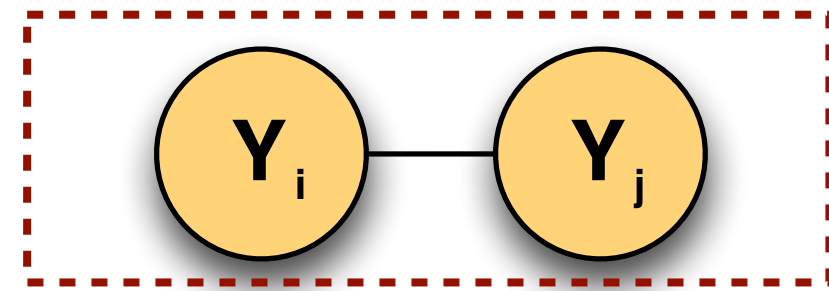
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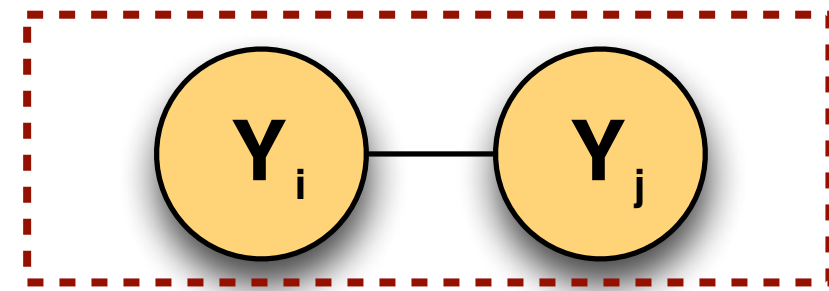
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*Local conditional*



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*Local conditional*

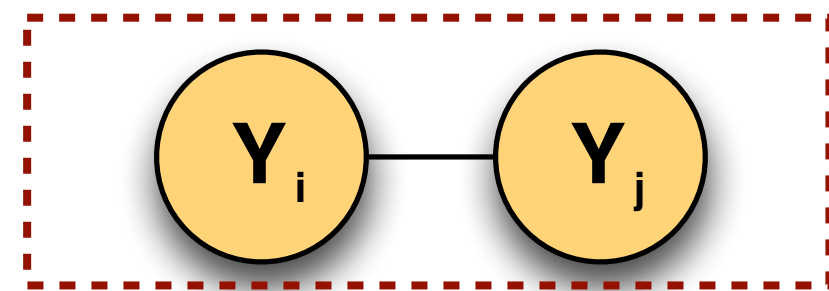


**Local component:**

any model to predict class  
label based on neighbor  
class/attribute values

**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions

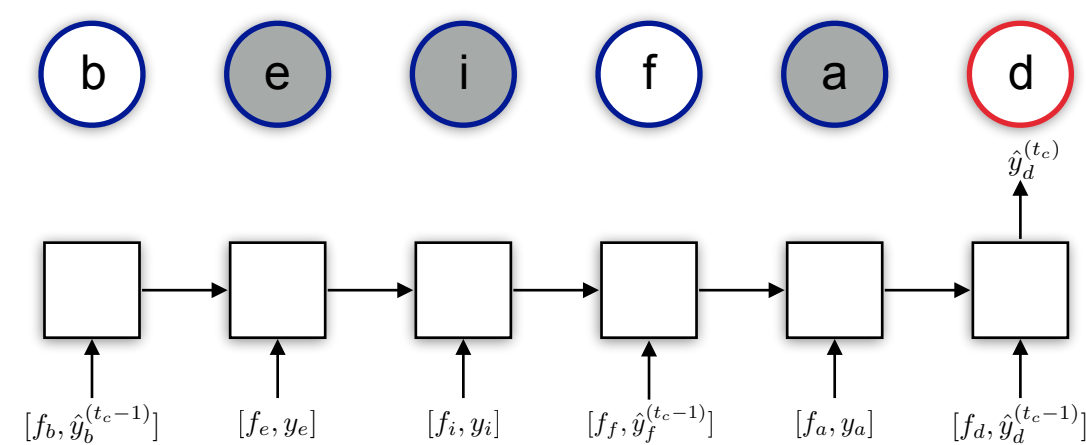
*Local conditional*



**Local component:**

any model to predict class label based on neighbor class/attribute values

**Neural network (e.g., LSTM):**



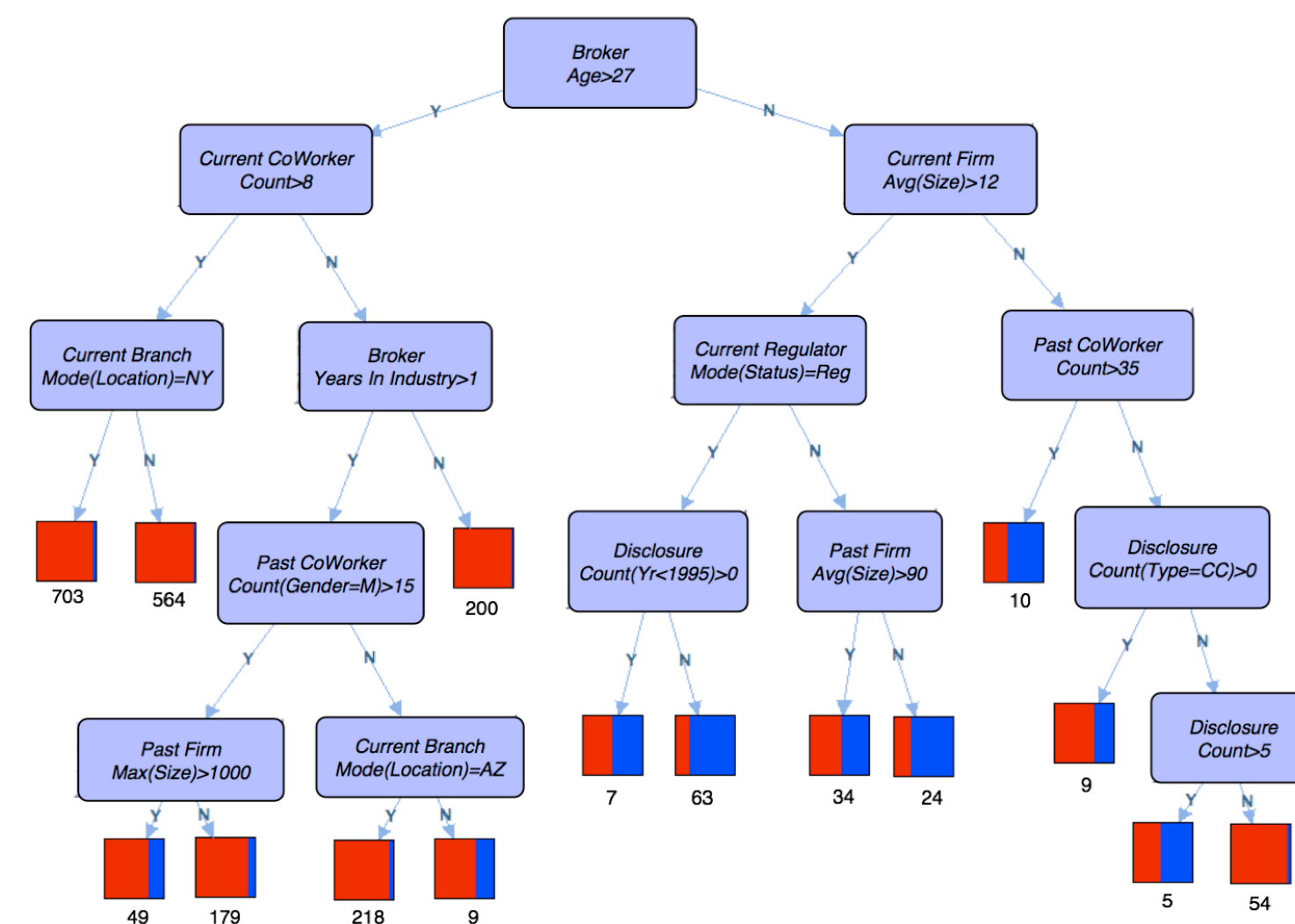
**Naive Bayes:**

$$P(Y_i | \mathcal{N}_i) \propto \prod_{v_j \in \mathcal{N}_i} P(Y_j | Y_i) P(Y_i)$$

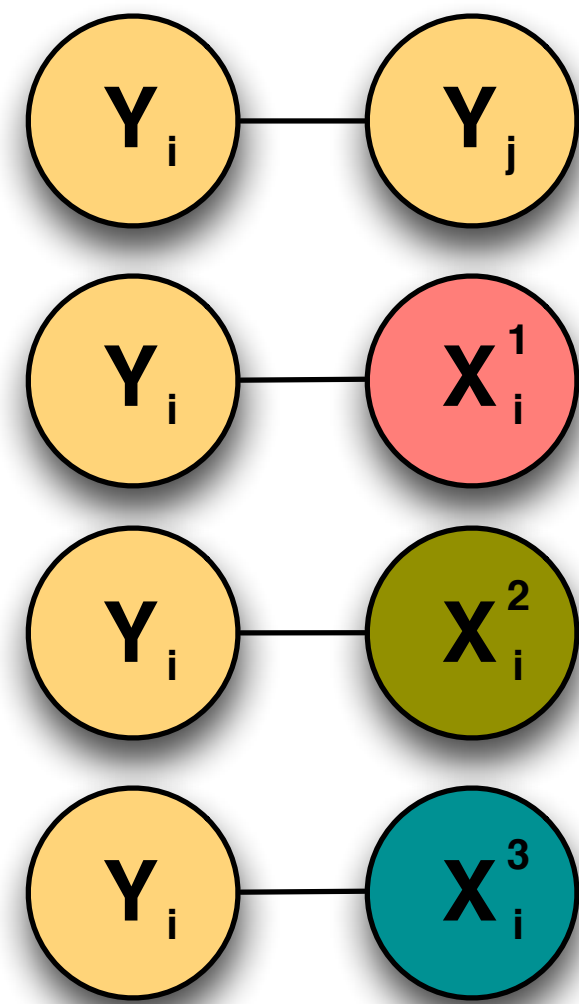
**Logistic regression:**

$$P(Y_i | \mathcal{N}_i) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 \sum_{j \in \mathcal{N}_i} Y_j + \beta_2 \sum_{j \in \mathcal{N}_i} |1 - Y_j|)}}$$

**Decision tree:**

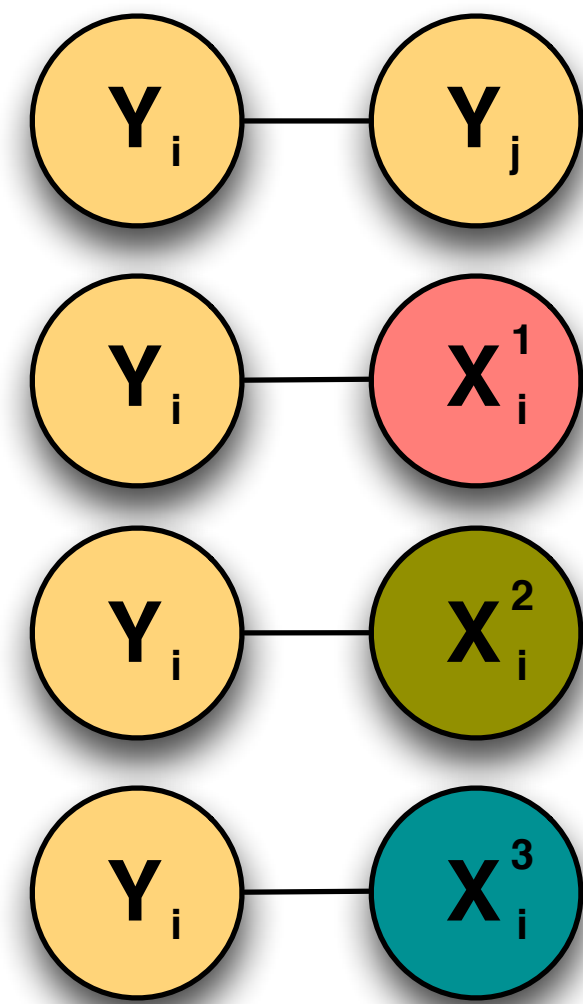


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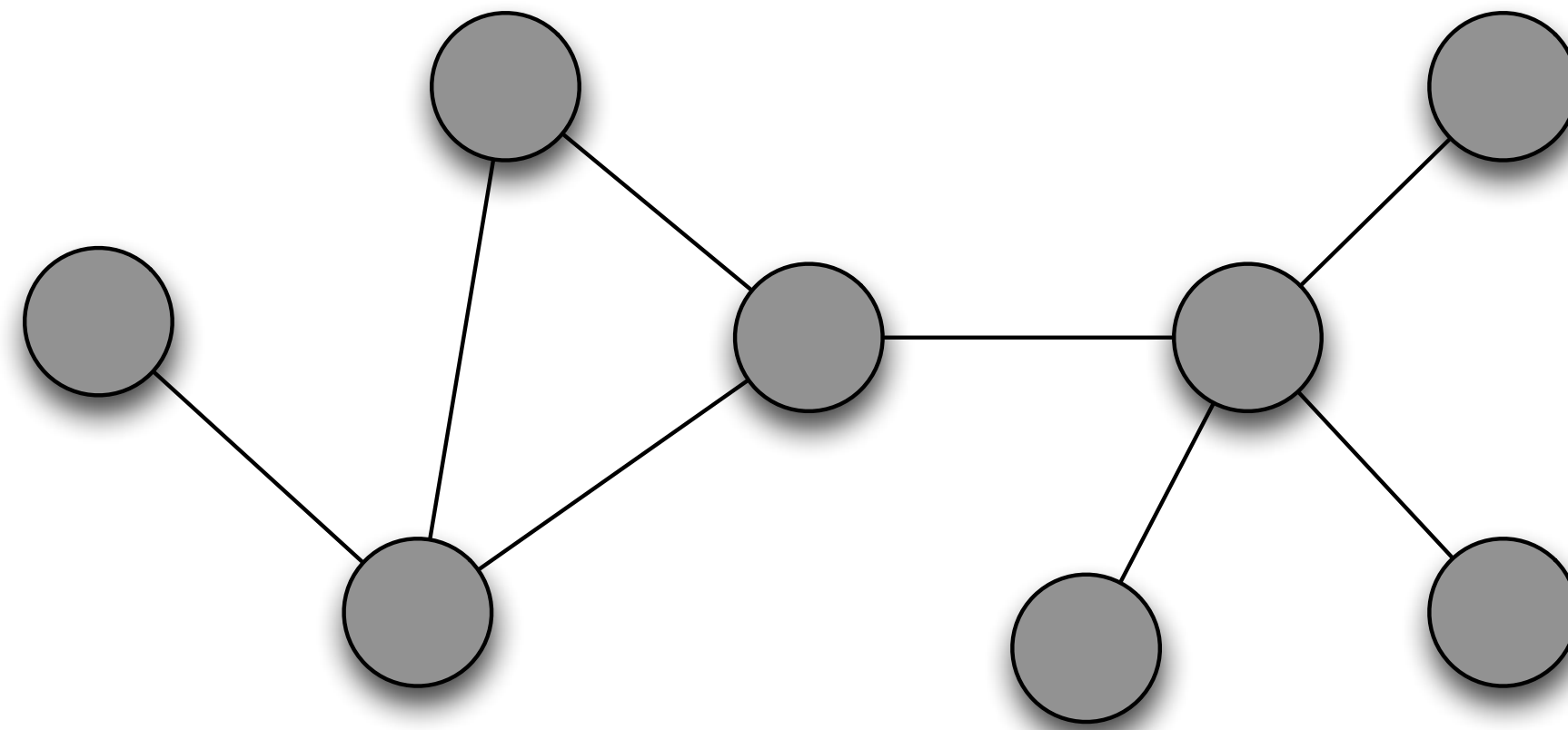
Model template

**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions



Model template

+



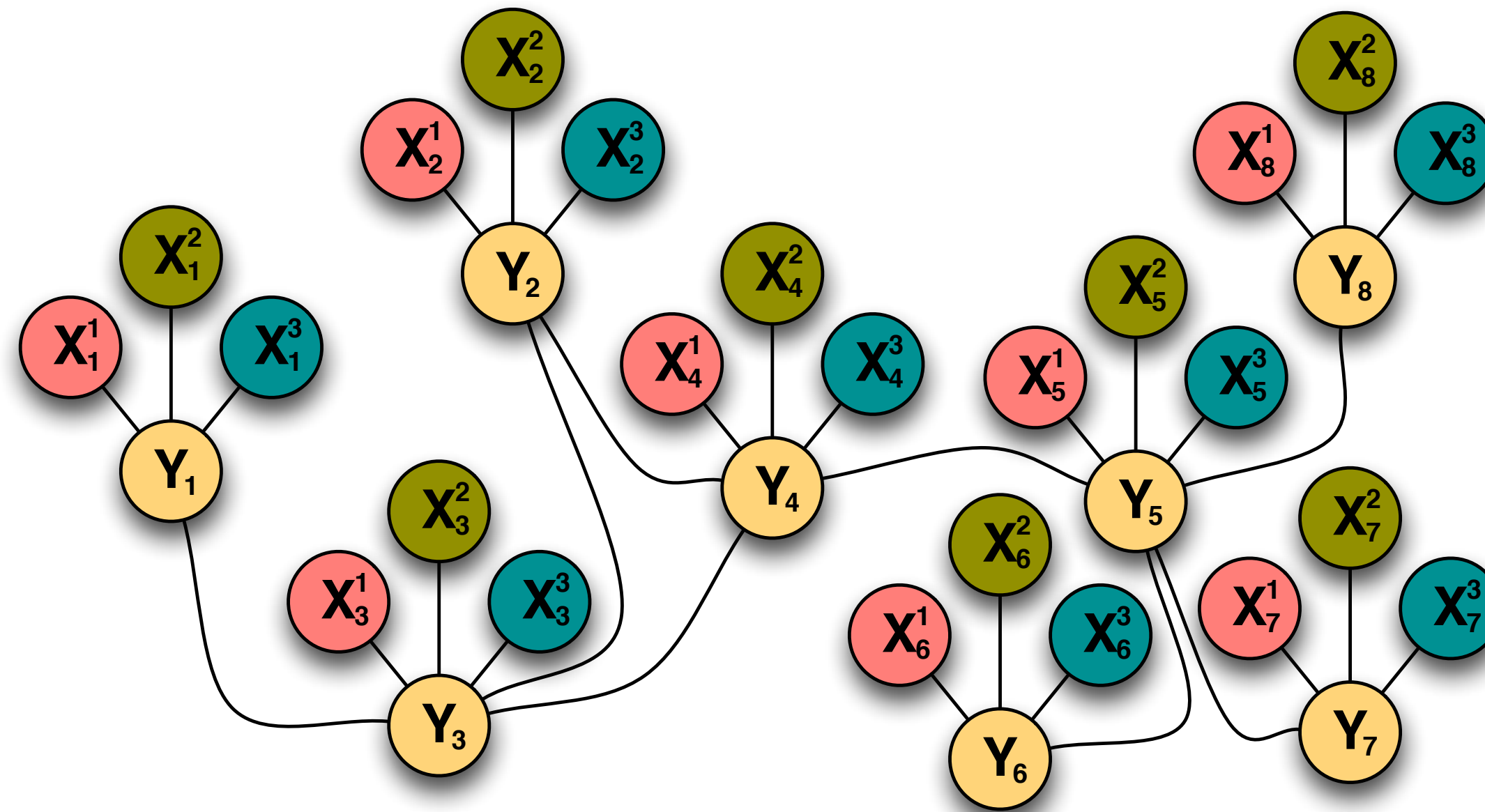
Data network

***Model is produced by “rolling out” templates over relational structure in data network***

**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions

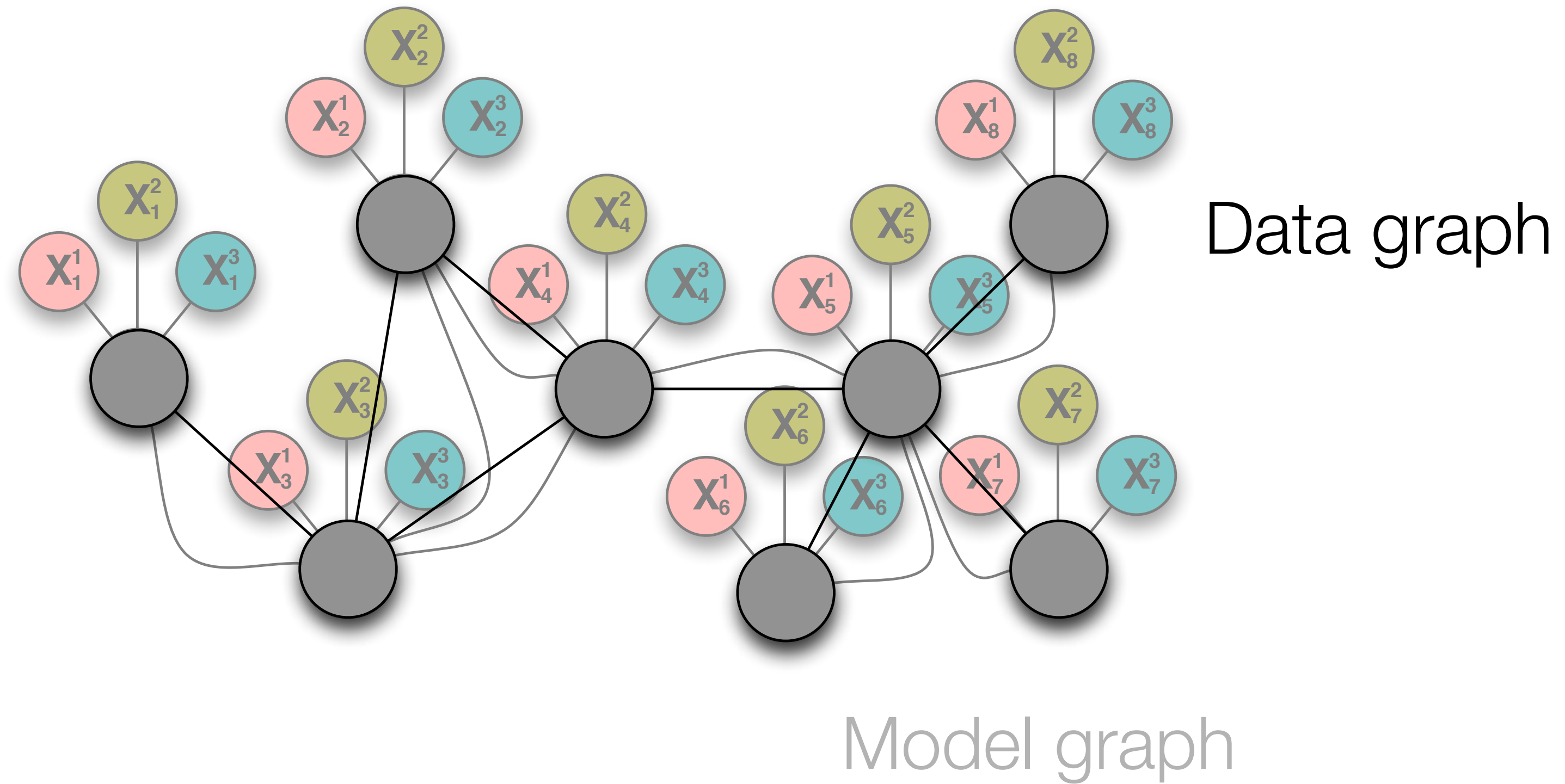


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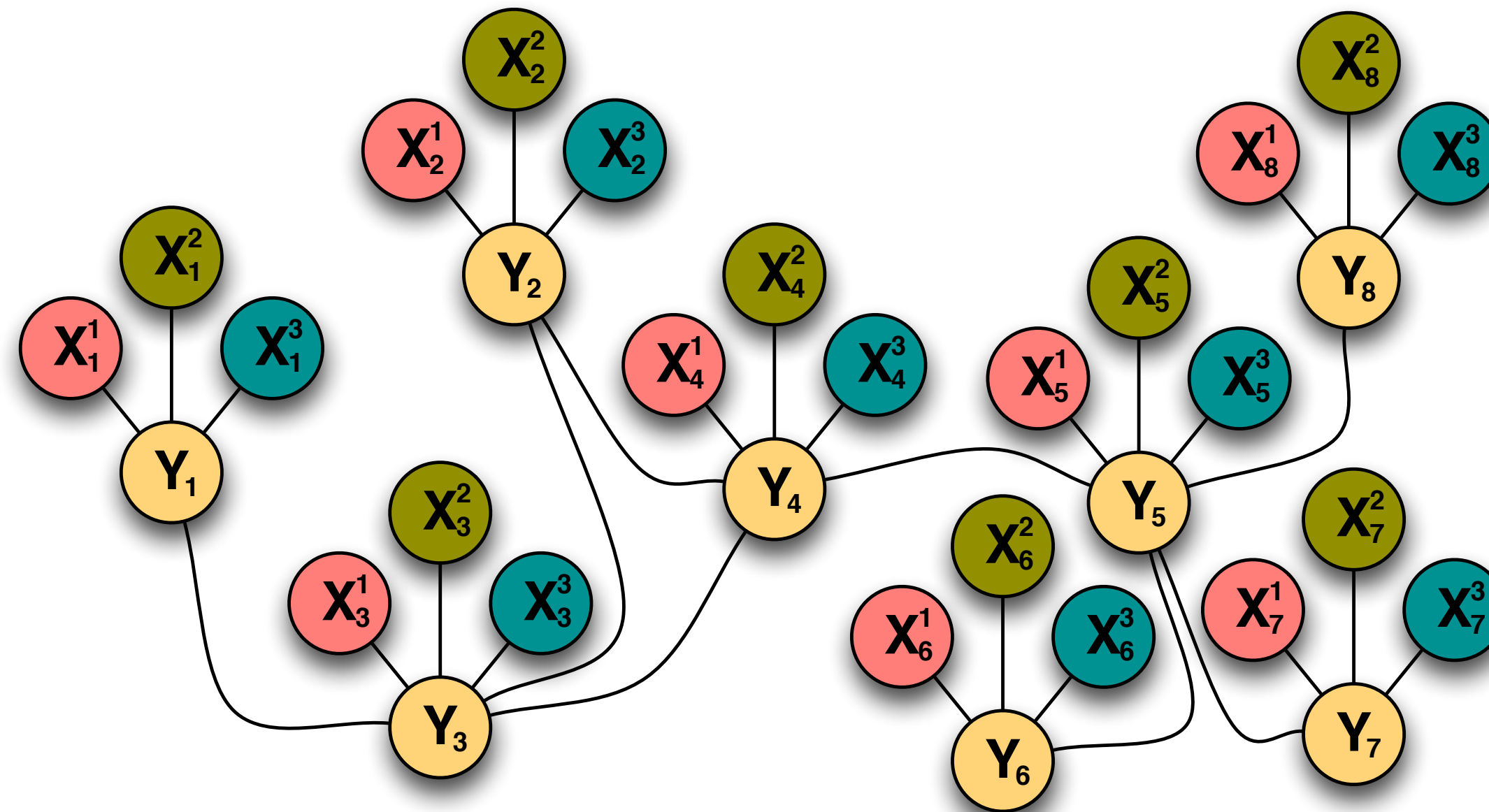


Model graph

**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions



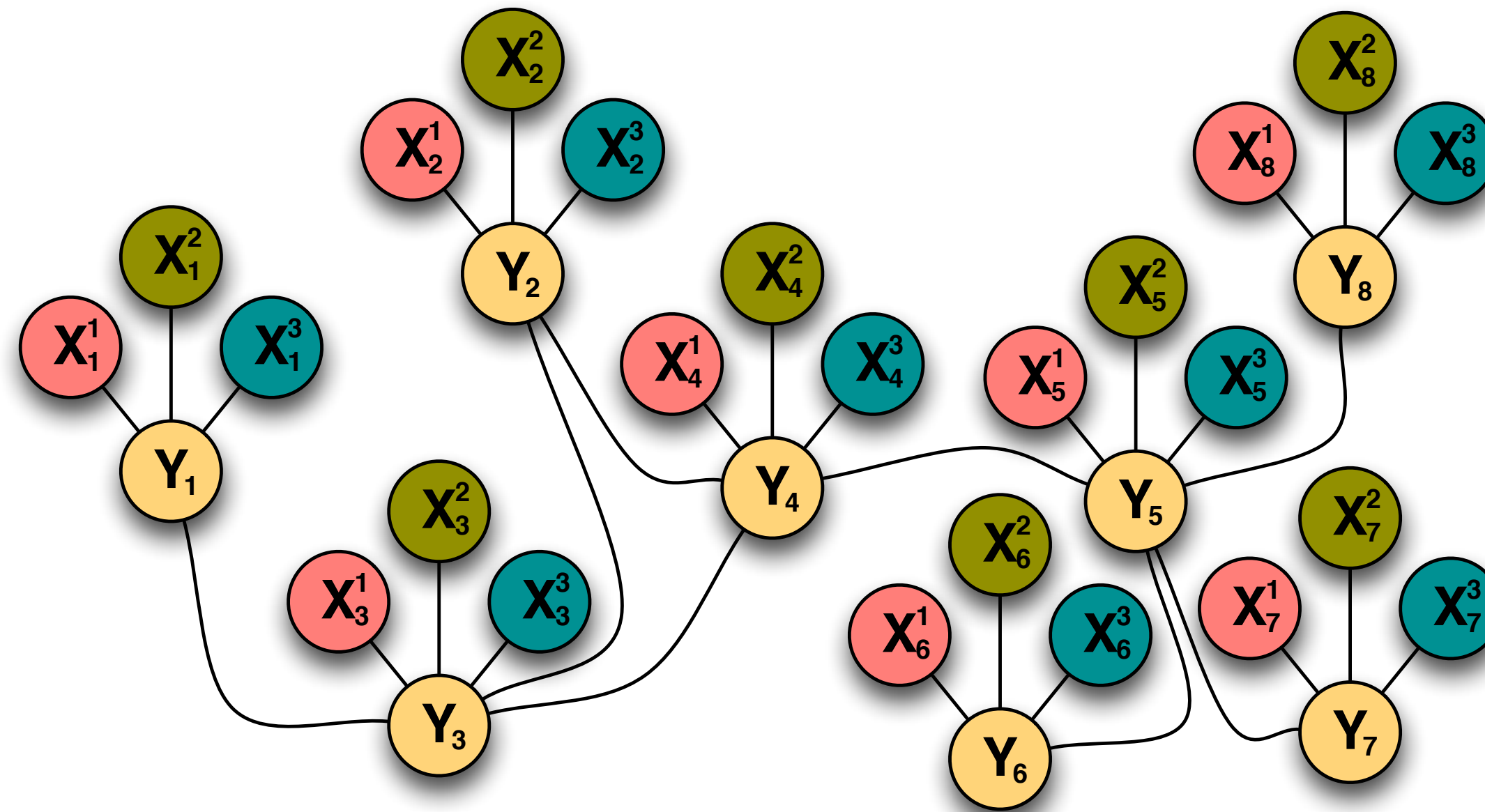
**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions



Learn joint model via optimization, tying parameters across templates

$$P(\mathbf{y}_G | \mathbf{x}_G) = \frac{1}{Z(\theta, \mathbf{x}_G)} \prod_{T \in \mathcal{T}} \prod_{C \in \mathcal{C}(T(G))} \Phi_T(\mathbf{x}_C, \mathbf{y}_C; \theta_T)$$

**Probabilistic modeling:** *Learn* set of models templates and use joint inference to combine together to make predictions



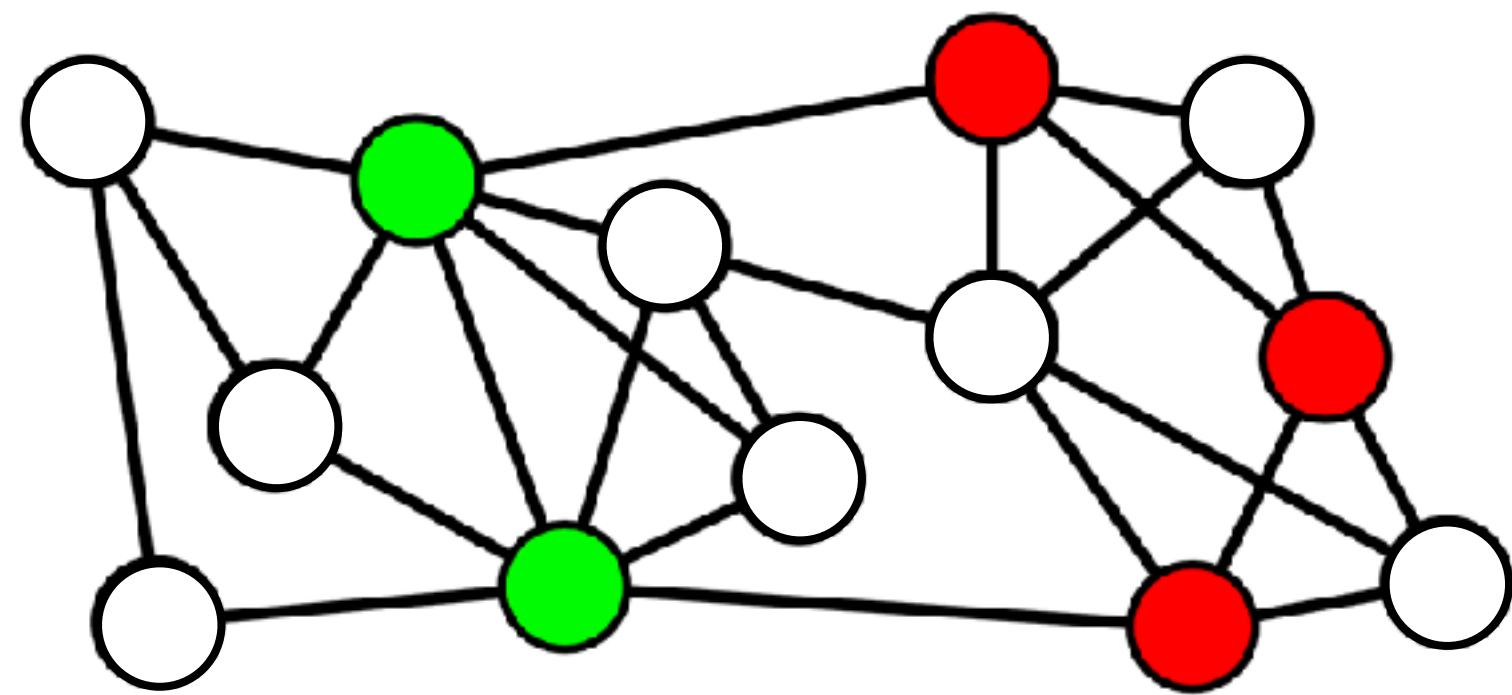
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**Note: this implicitly conditions on graph structure G**

How do we estimate over a partially labeled graph?

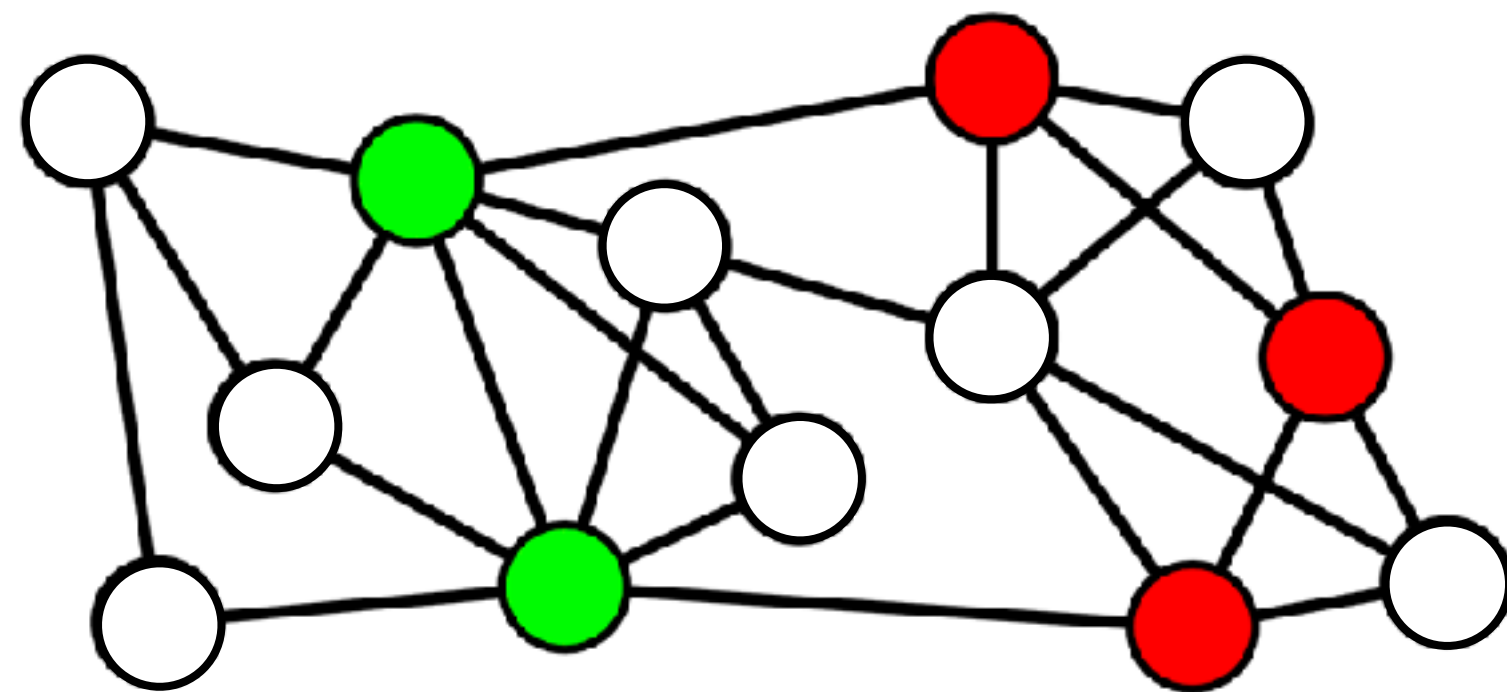
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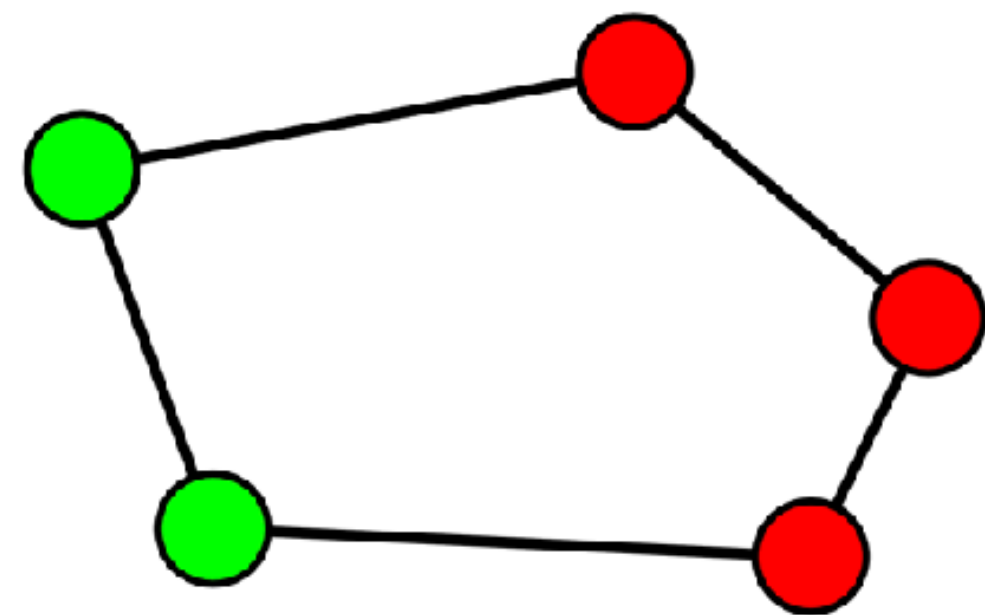
Partially labeled network ( $G$ )

# How do we estimate over a partially labeled graph?

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Partially labeled network ( $G$ )

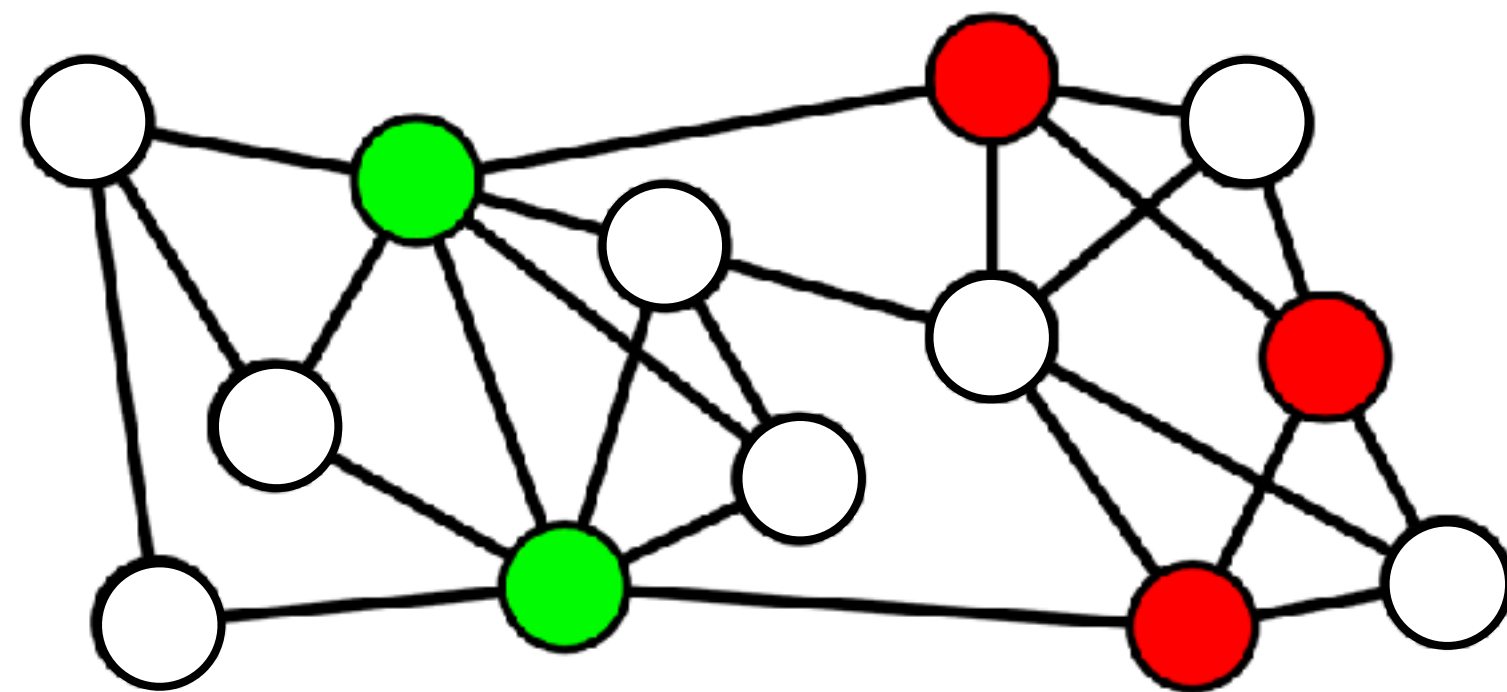


Pseudolikelihood ( $G_L$ )

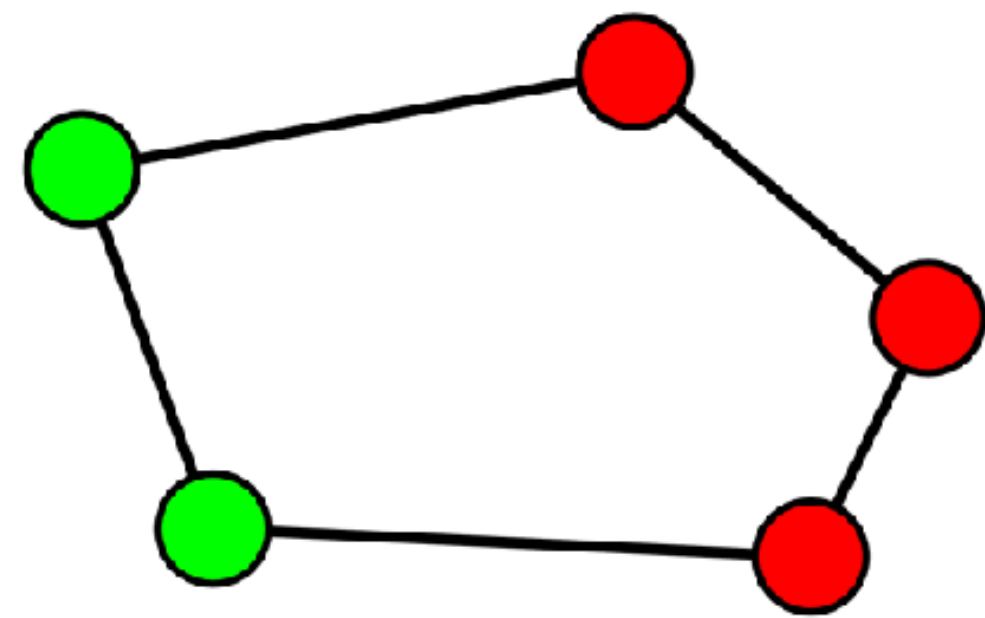
**Approach 1:**  
*ignore unlabeled network during learning*

# How do we estimate over a partially labeled graph?

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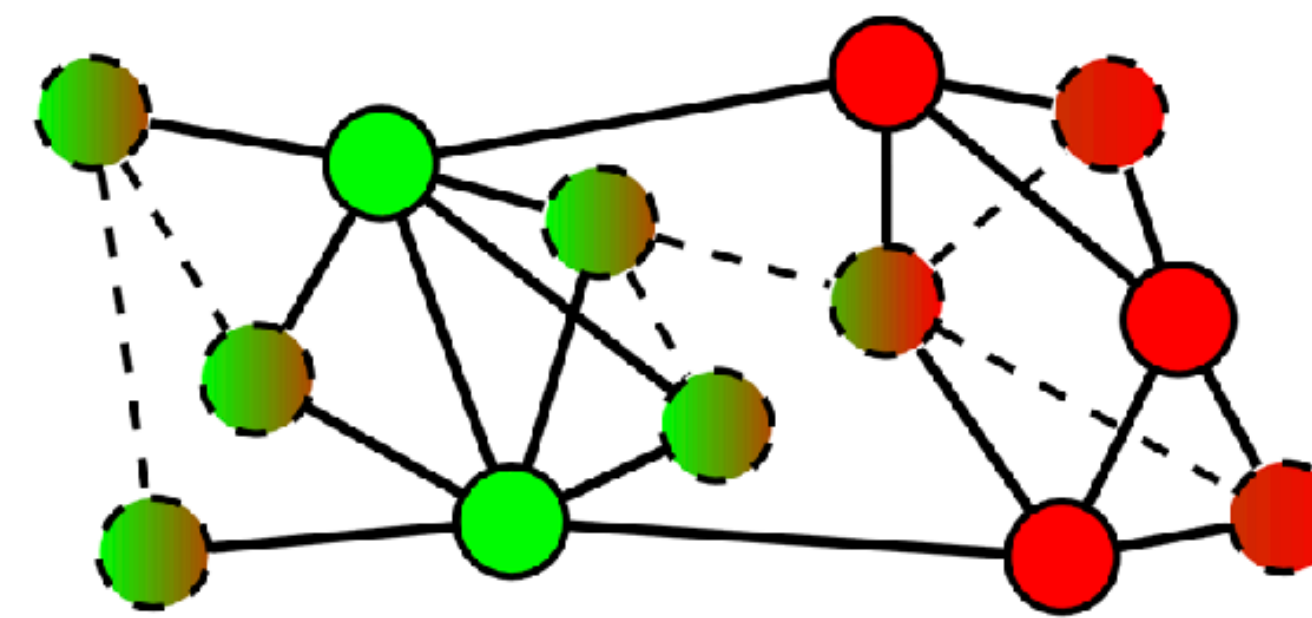


Partially labeled network ( $G$ )



Pseudolikelihood ( $G_L$ )

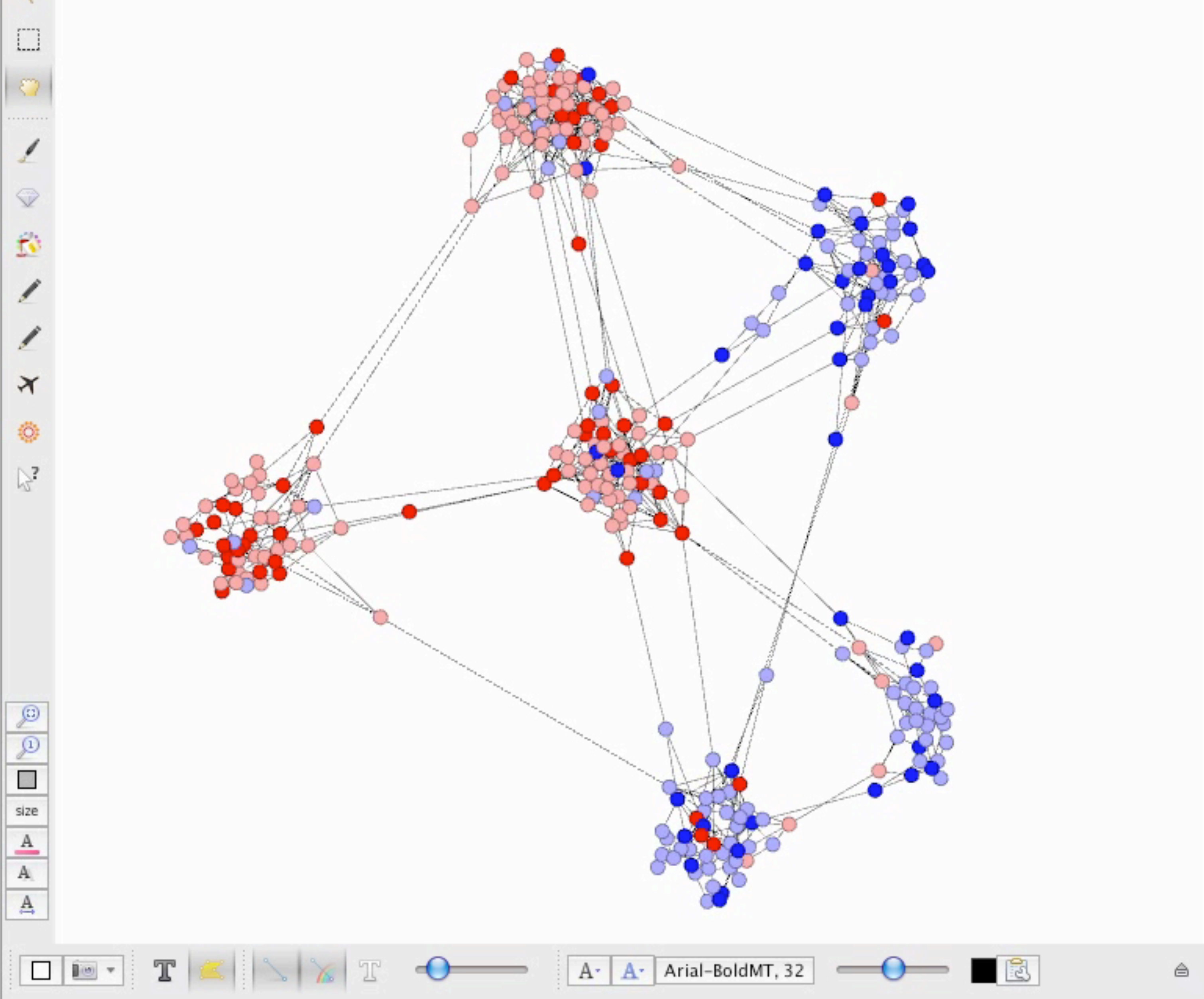
**Approach 1:**  
*ignore unlabeled network during learning*



Composite Likelihood ( $G$ )

**Approach 2:** *semi-supervised,  
use unlabeled only as features of labeled*

Make predictions using *collective inference*



*Small world graph*  
*Labeled nodes: 30%*  
*Autocorrelation: 0.5*

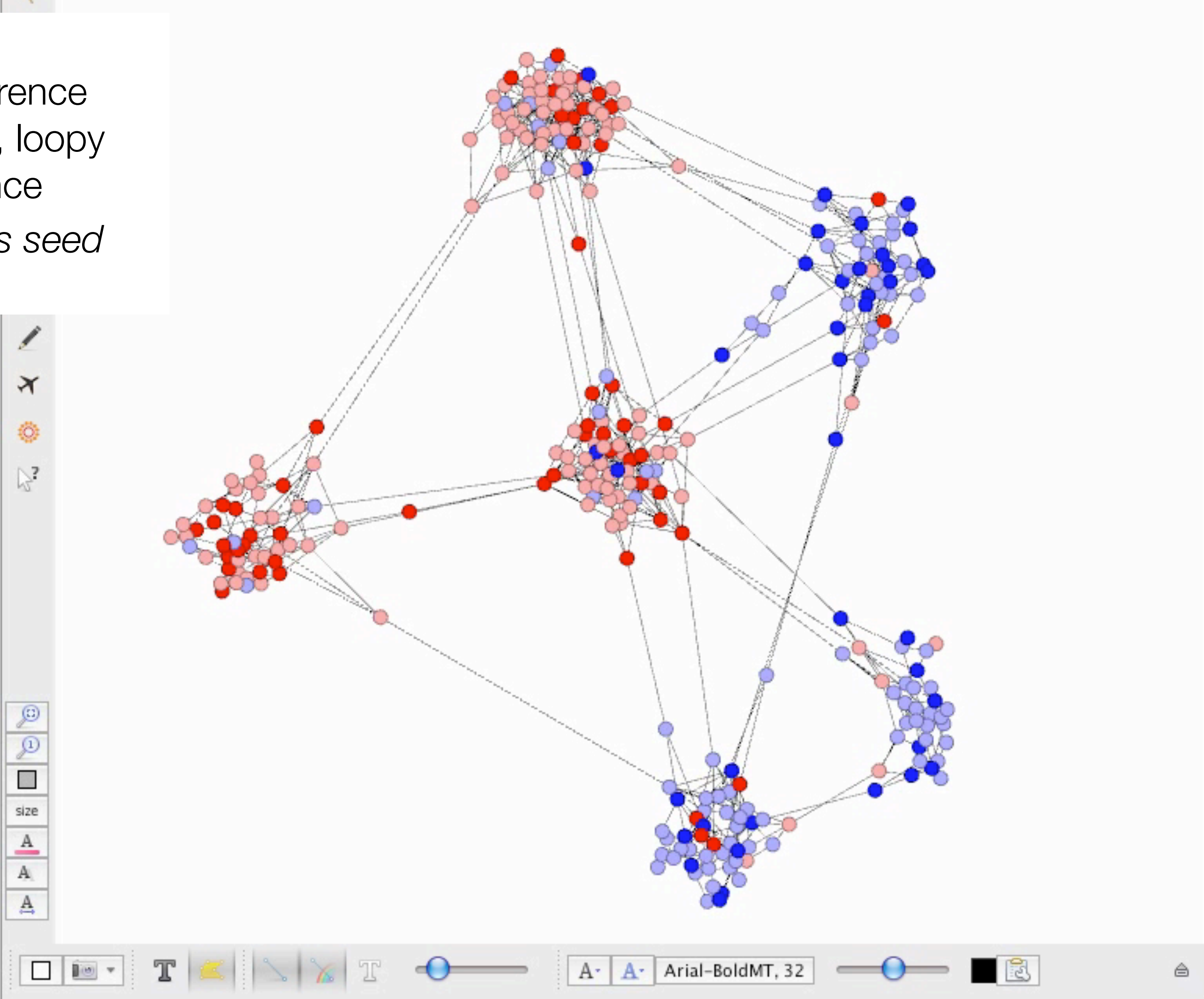


# Make predictions using *collective inference*

**Inference method:**

any approximate inference  
e.g., Gibbs sampling, loopy  
BP, variational inference

*Note: observed labels seed  
inference process*



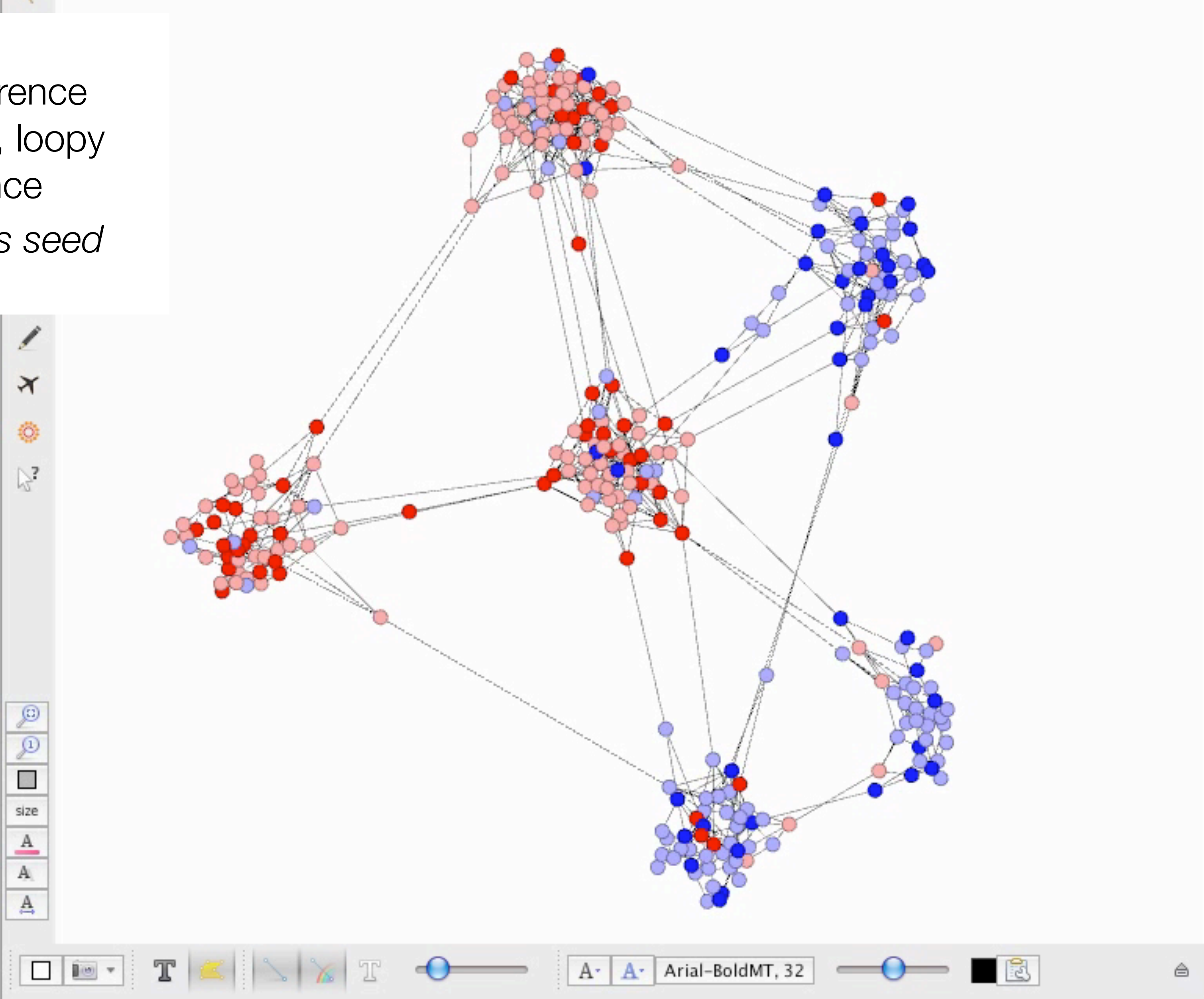
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Can neural networks improve semi-supervised collective inference?

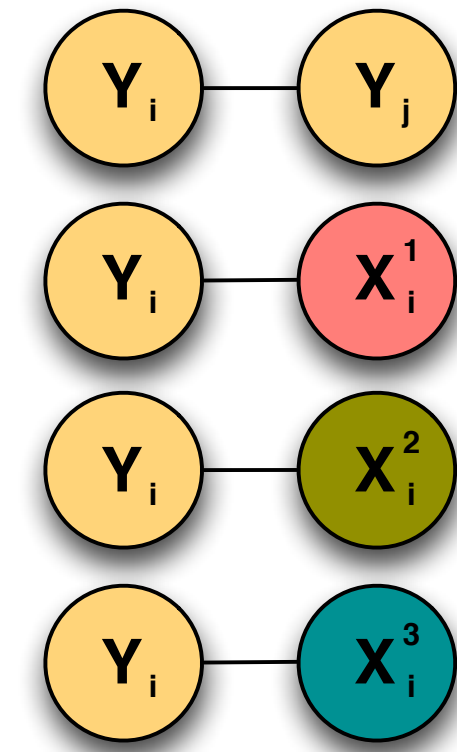
# Semi-supervised relational deep learning

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- To learn with partially labeled network, use **semi-supervised** collective classification
  - Use relational EM for estimation over full network
- Recall that joint relational model = set of local conditional models + joint inference

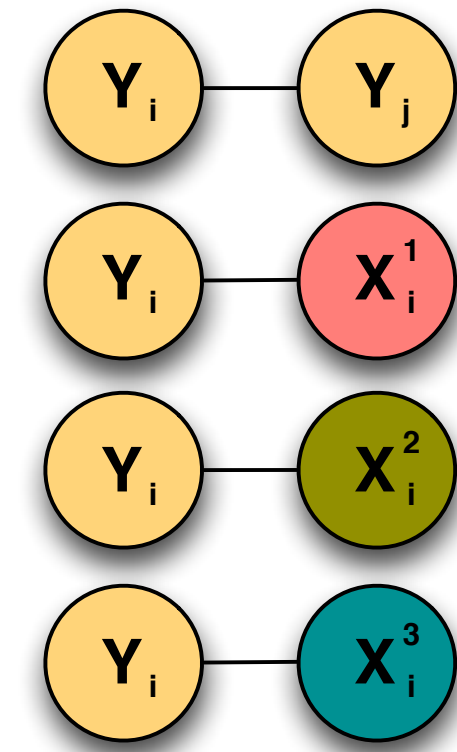


Model template

# Semi-supervised relational deep learning

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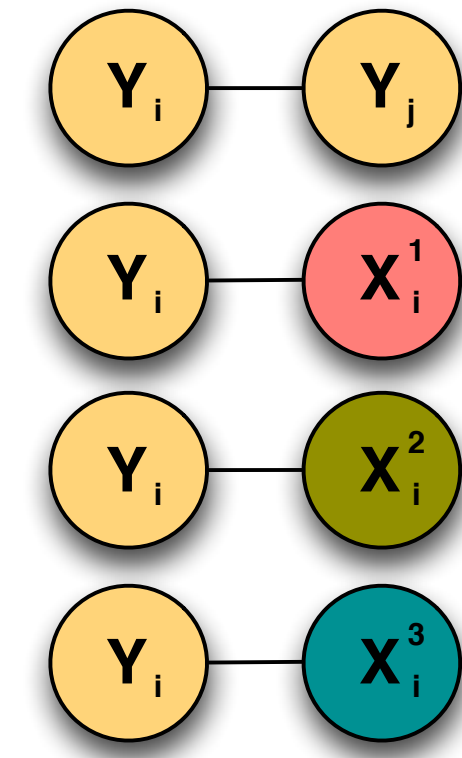
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Model template

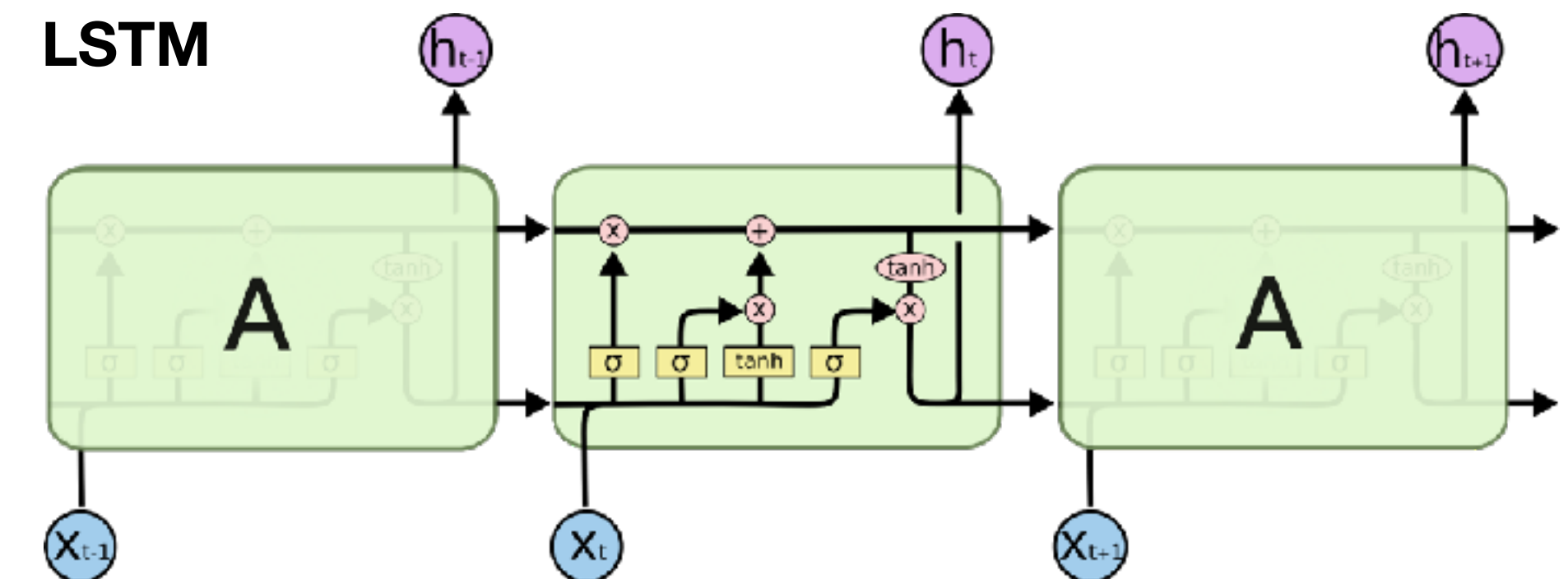
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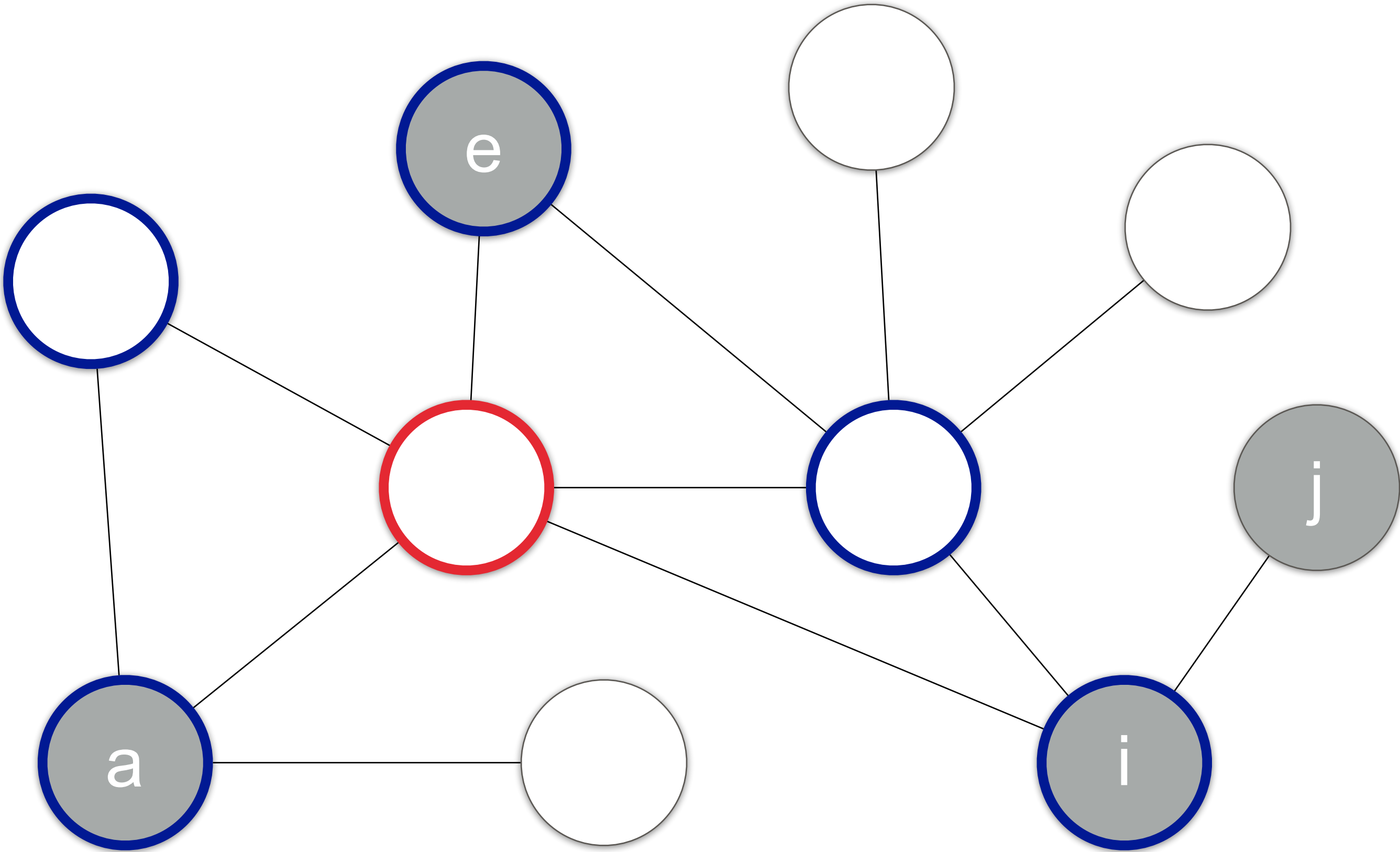
Model template

- *Can* neural networks be used to learn better local conditional?  
Need a permutation-invariant vector representation for heterogeneous graphs
  - Represent set of neighbors as a **sequence**, in *random order*
  - To deal with heterogenous inputs (i.e., varying number of neighbors), use a **recurrent** neural network (e.g., LSTM)



# Network instance in partially labeled graph

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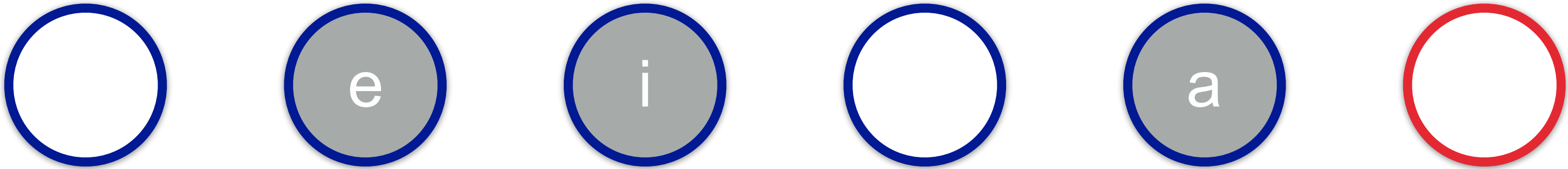
red = target node  
blue = neighbors  
grey = labeled  
white = unlabeled



# Network instance in partially labeled graph

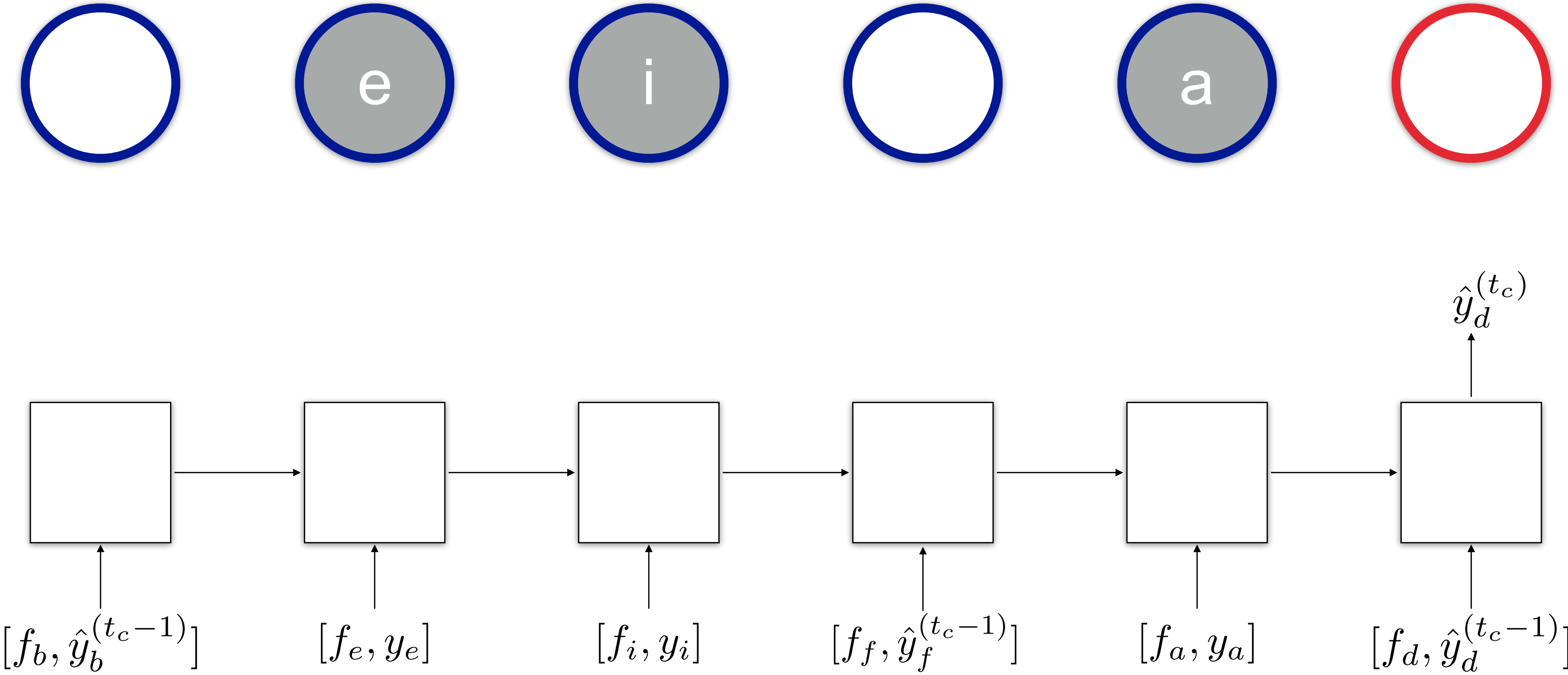
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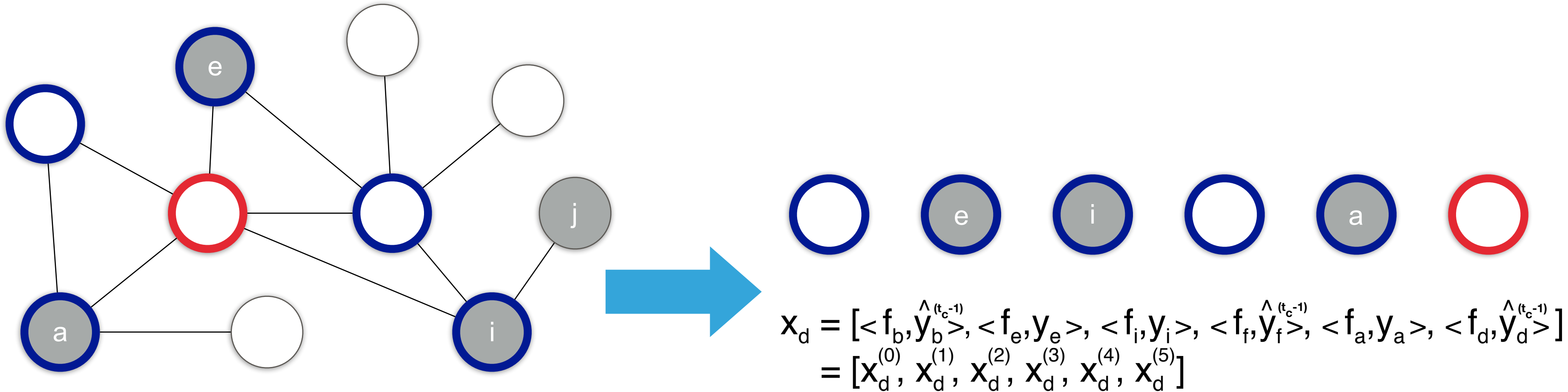


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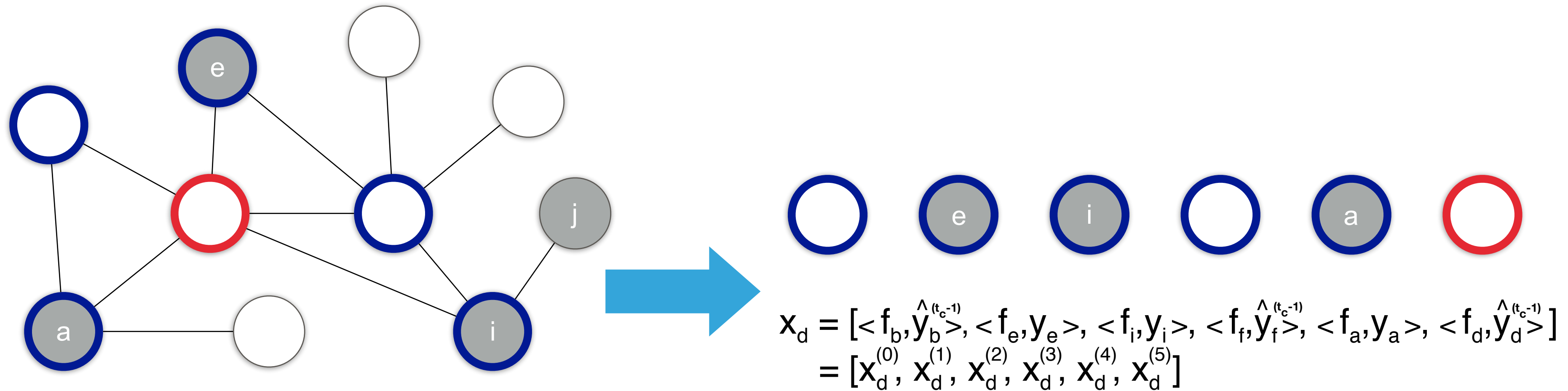


# Deep collective inference (DCI) *(Moore & N AAI'17)*



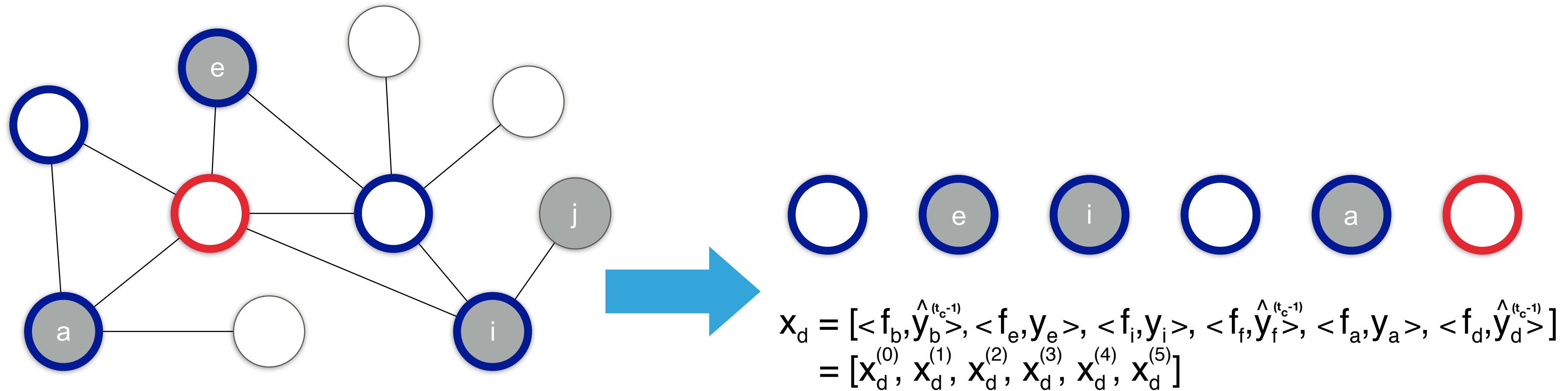
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- For node  $v_i$ , and current iteration  $t_c$ , the input is node features concatenated with previous prediction  $[f_i, \hat{y}_i^{(t_c-1)}]$  and neighbor features concatenated with predictions/labels  $\{[f_j, (y_j \text{ or } \hat{y}_j^{(t_c-1)})] \mid v_j \in \mathcal{N}_i\}$



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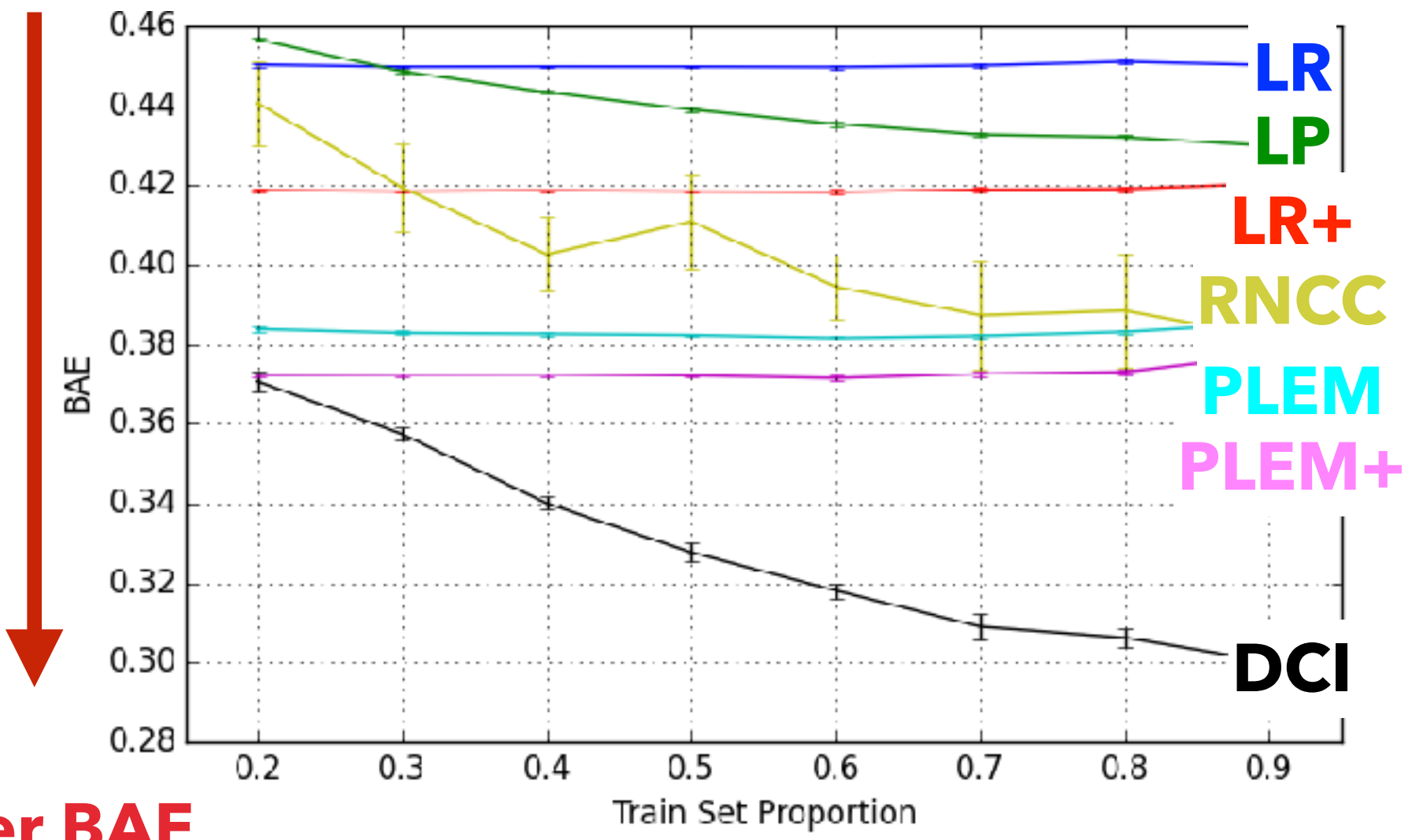
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- Learn LSTM conditional with relational EM. Key design choices:
  - Initialize label predictions** with non-collective relational model
  - Randomize neighbor order** on every iteration
  - Correct for imbalanced classes**, either by balancing the objective function or by balancing the data with augmentation

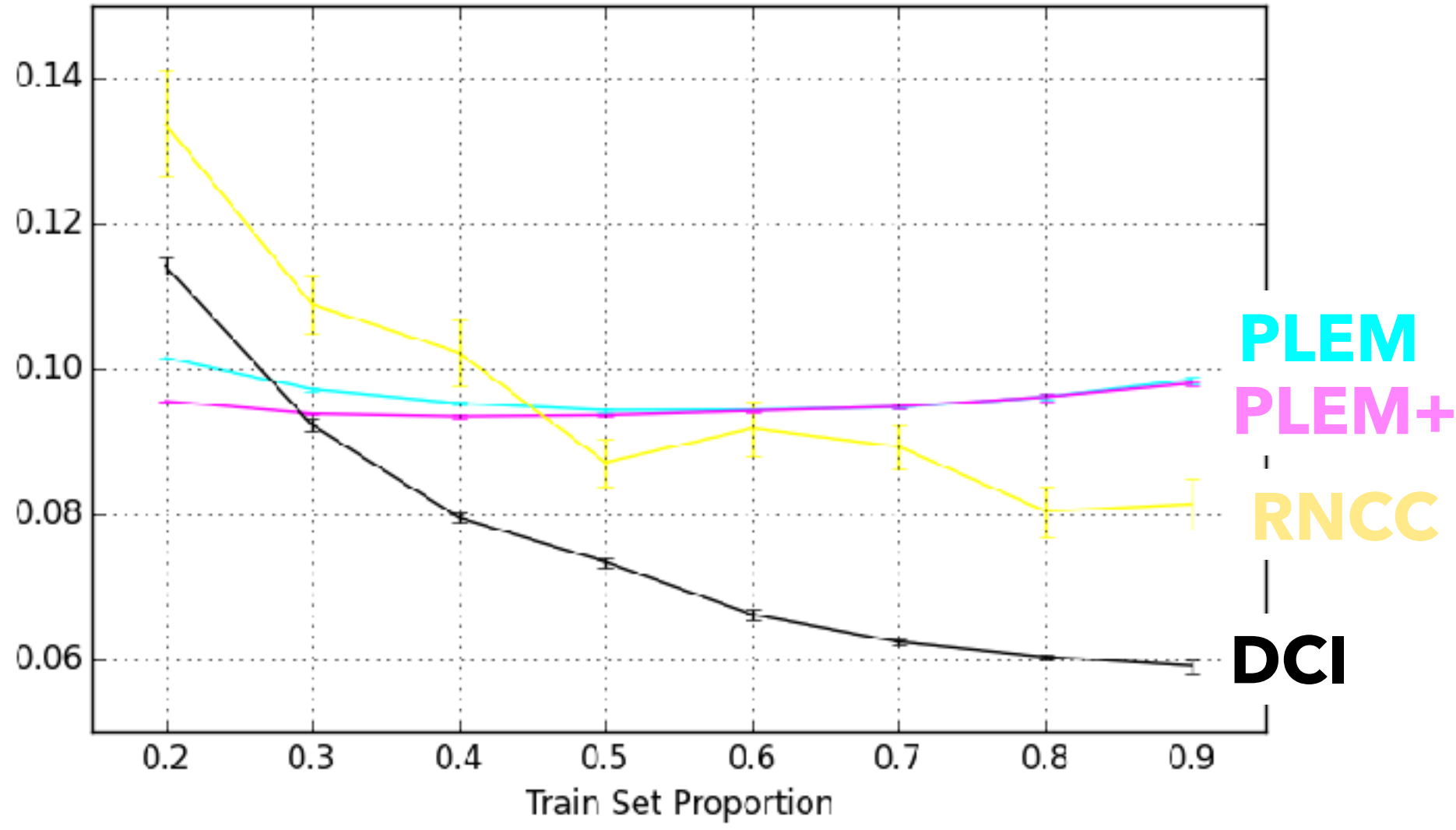
Evaluation shows that neural network (DCI) can produce better conditionals, if objective is designed carefully

Amazon DVD (50/50)



Lower BAE is better

Patents (17/83)



Predicting subgraphs in evolving heterogeneous graphs

# Predicting subgraph evolution over time

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# Predicting subgraph evolution over time

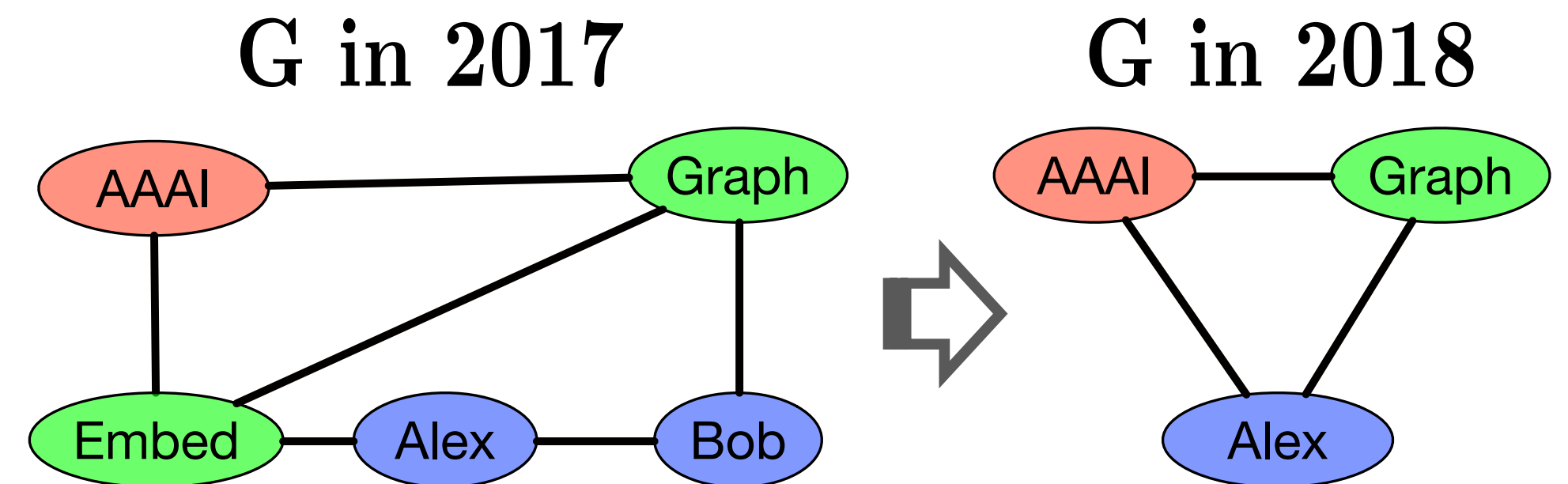
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- **Task:** Predict topology and/or label evolution of subgraphs
  - E.g., from observed subgraphs in  $G_{t=2017}$  to  $G_{t=2018}$ , predict their evolution in  $G_{t=2019}$
- **Challenges:** How to incorporate subgraph dependencies in a tractable way? How to represent data such that it is invariant to graph isomorphisms?
- Naive approach: adapt existing graph prediction methods

# Predicting subgraph evolution over time

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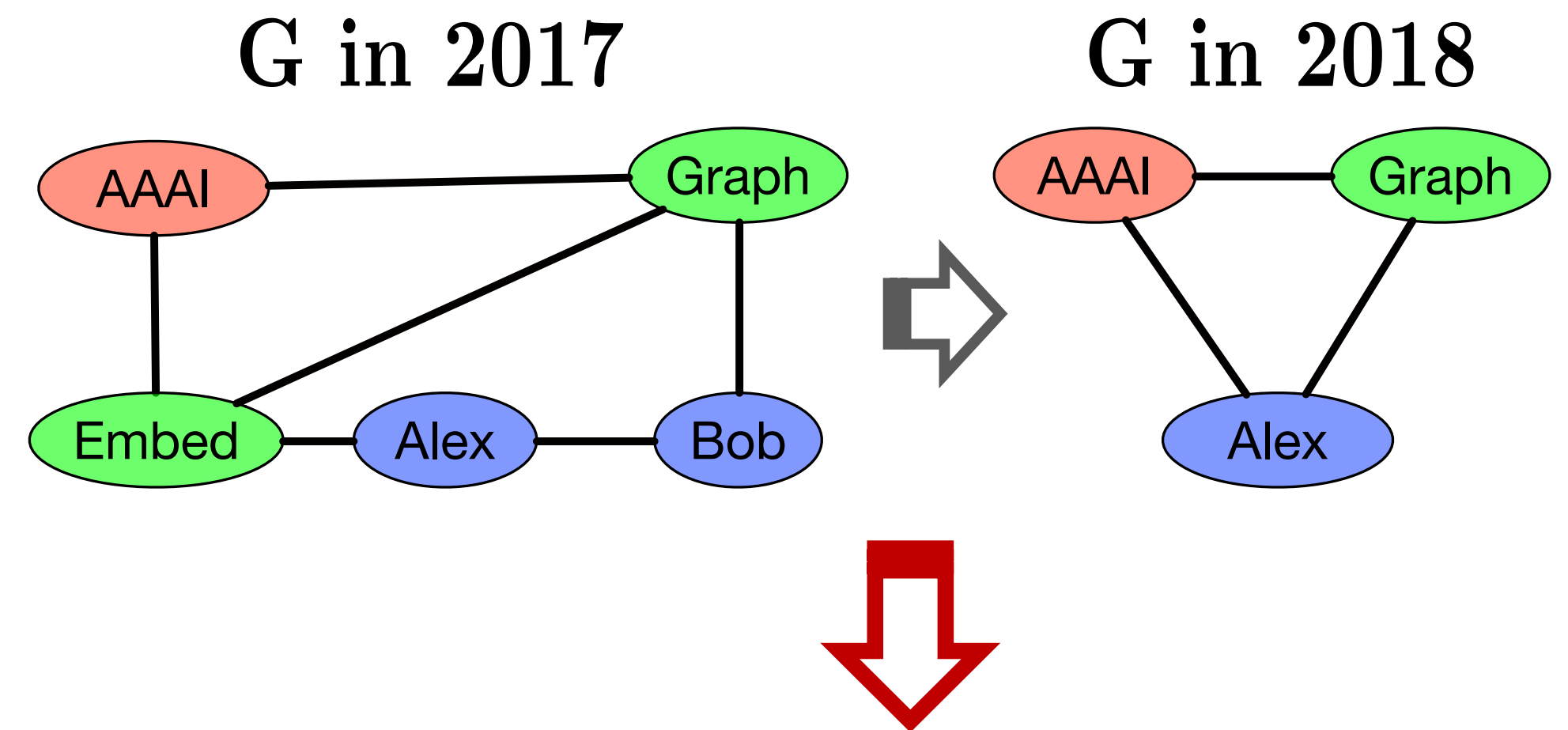
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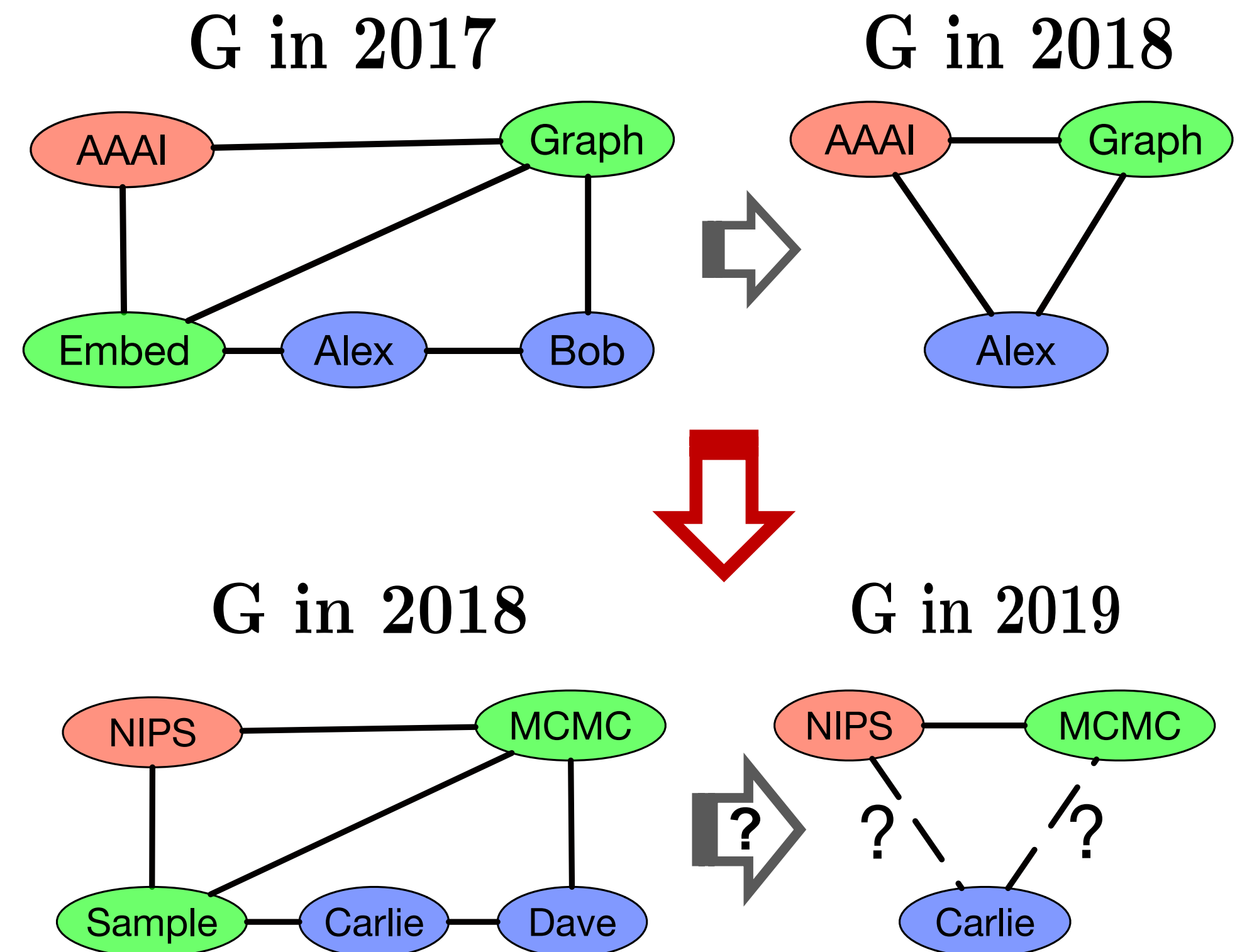
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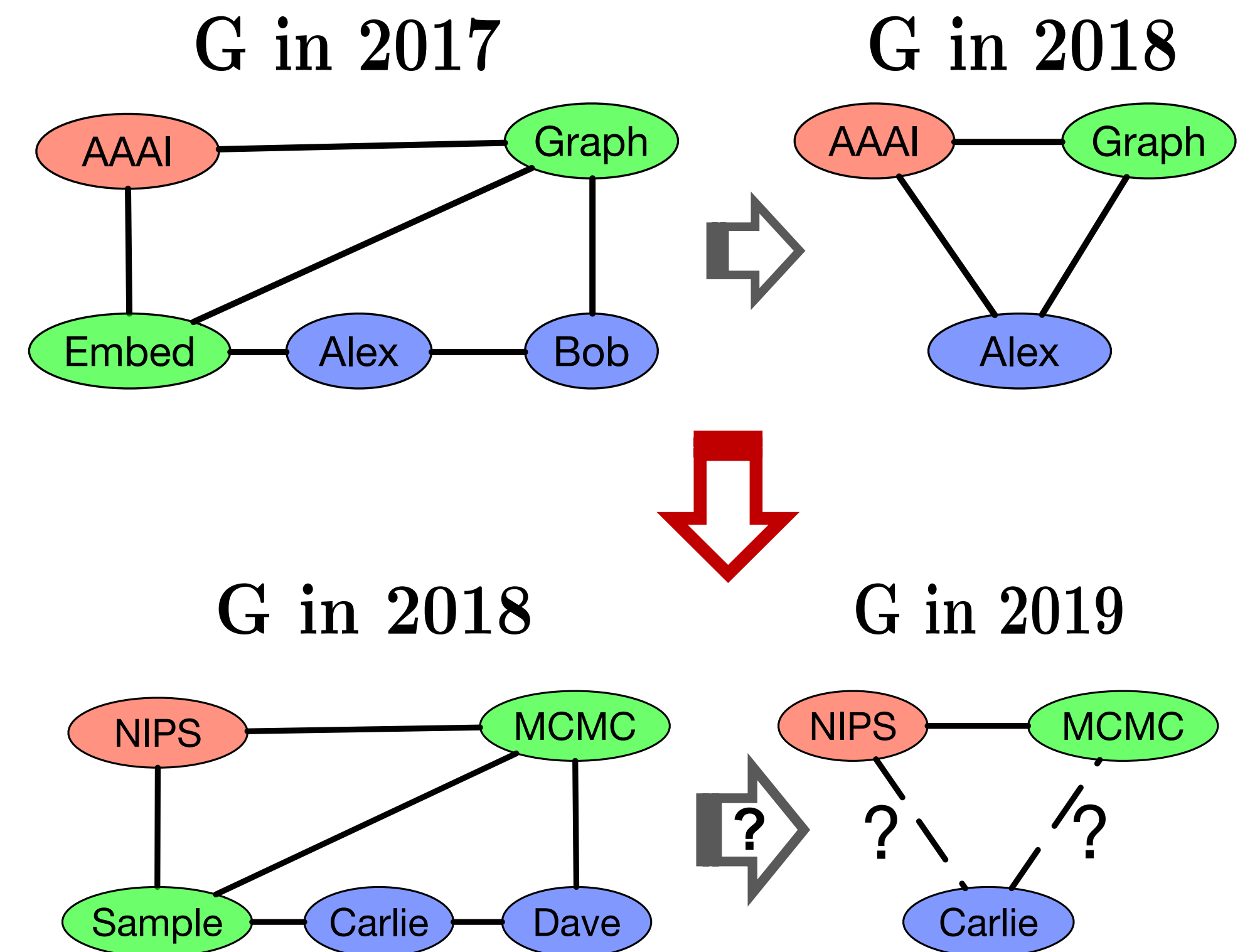
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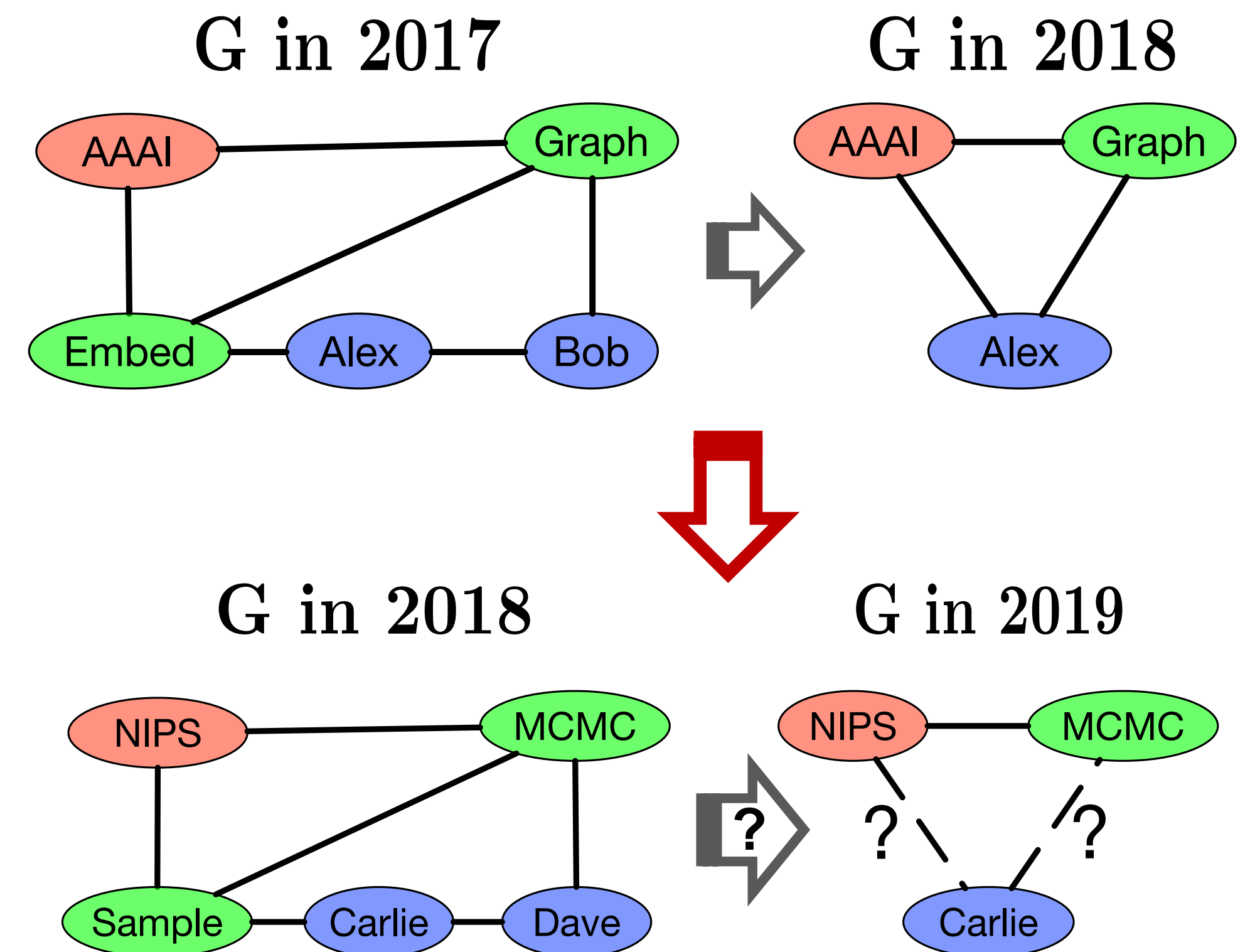
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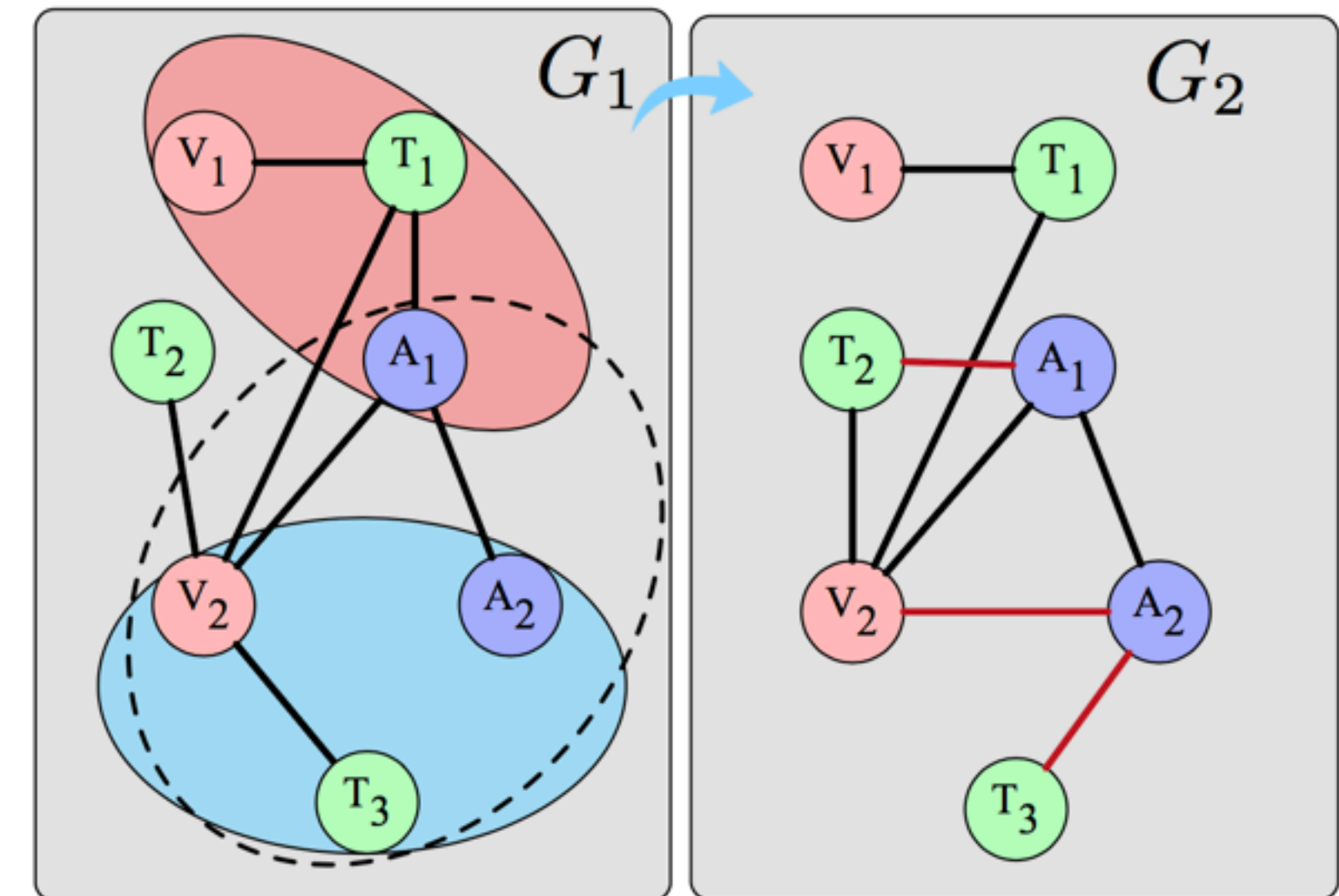


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  - Use link prediction methods to independently predict multiple links (*doesn't learn jointly*)
  - Use graph classification methods for subgraph prediction (*doesn't consider context around subgraph*)



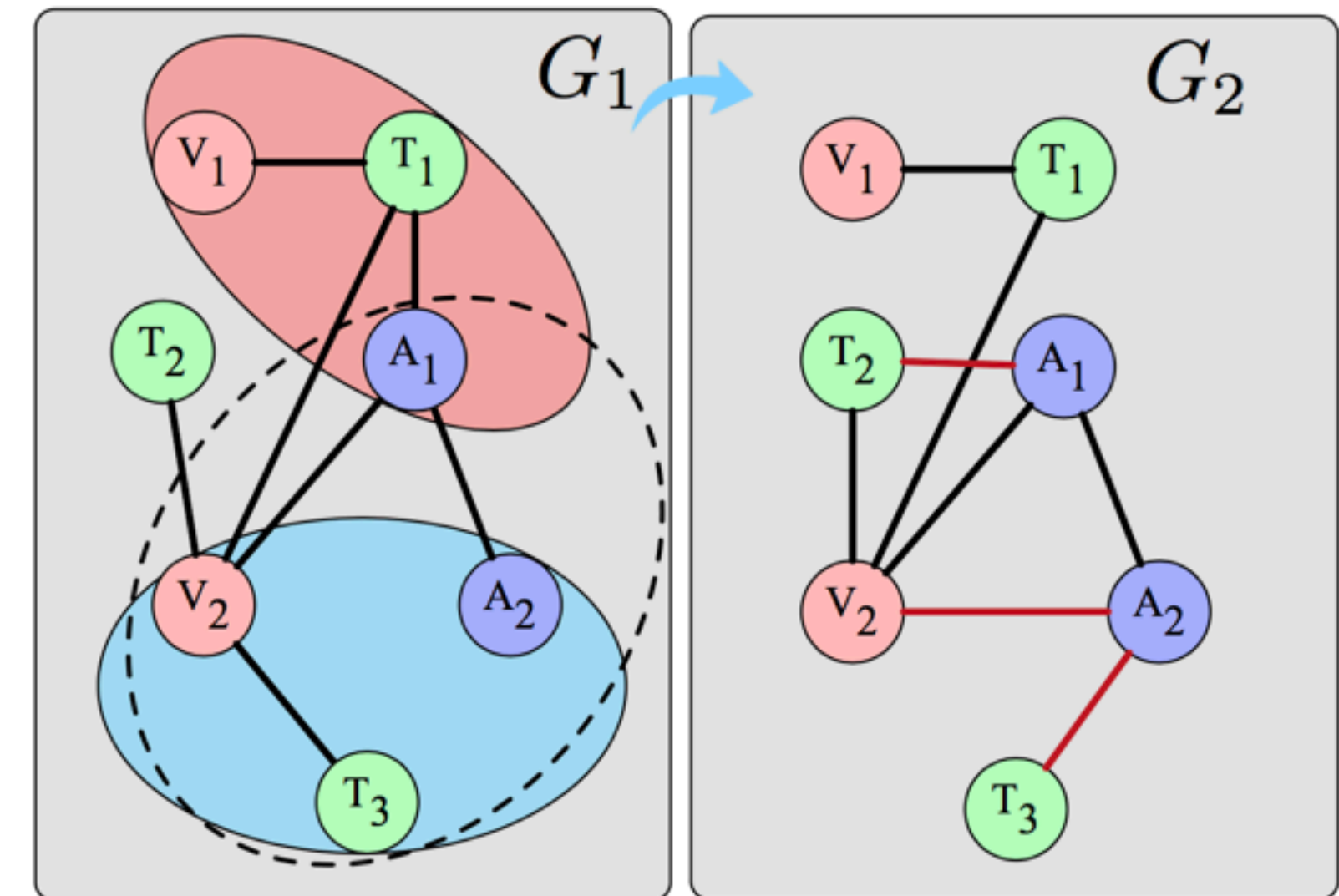
# Subgraph Pattern Neural Network *(Meng, Mouli, Ribeiro, and N AAI'18)*



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- **Problem formulation:**

- Use induced labeled subgraph patterns to map from set of nodes in one time step to next
- Learn subgraph embedding for joint edge-node-attribute predictions
- Examples drawn from larger **connected** subgraphs

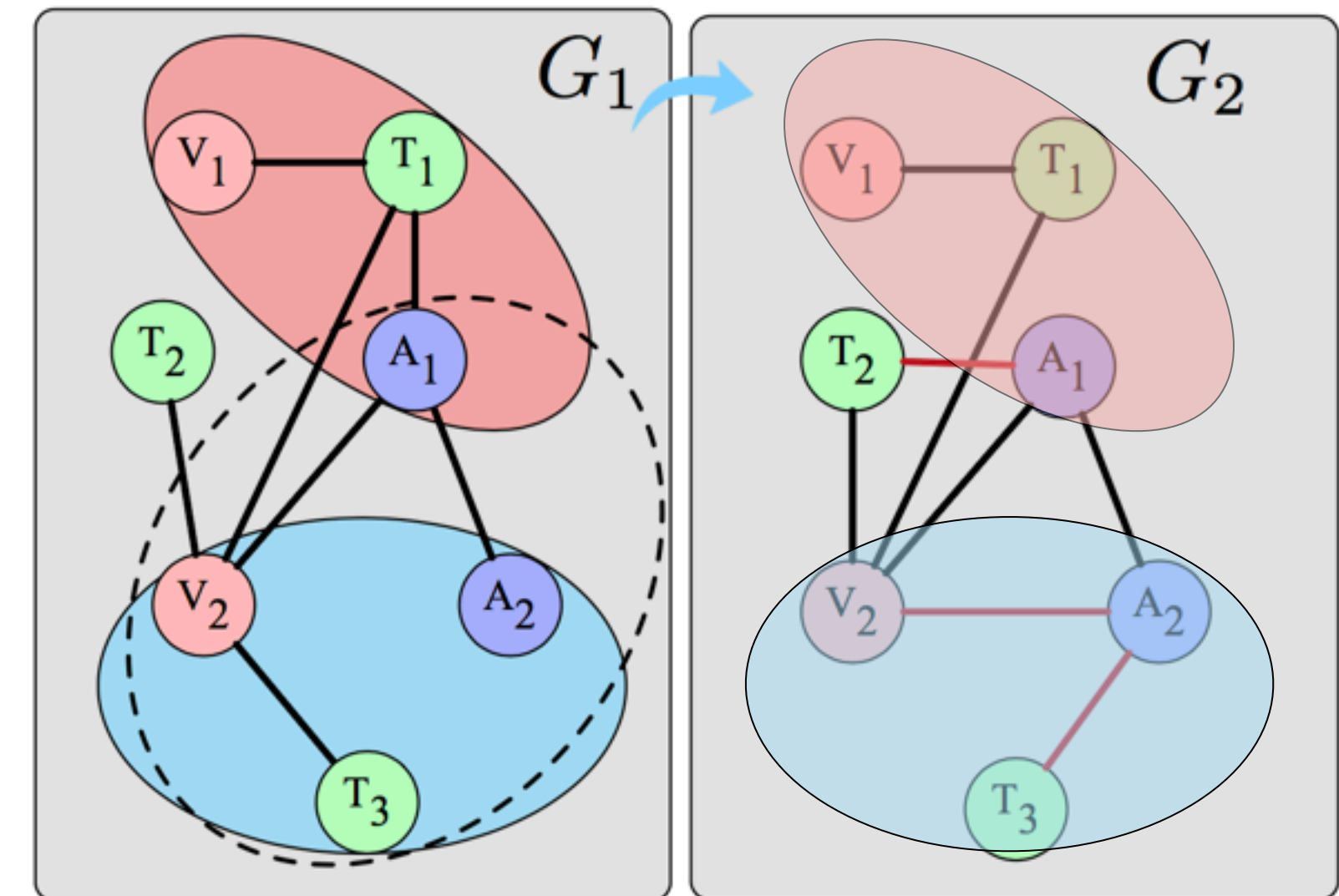




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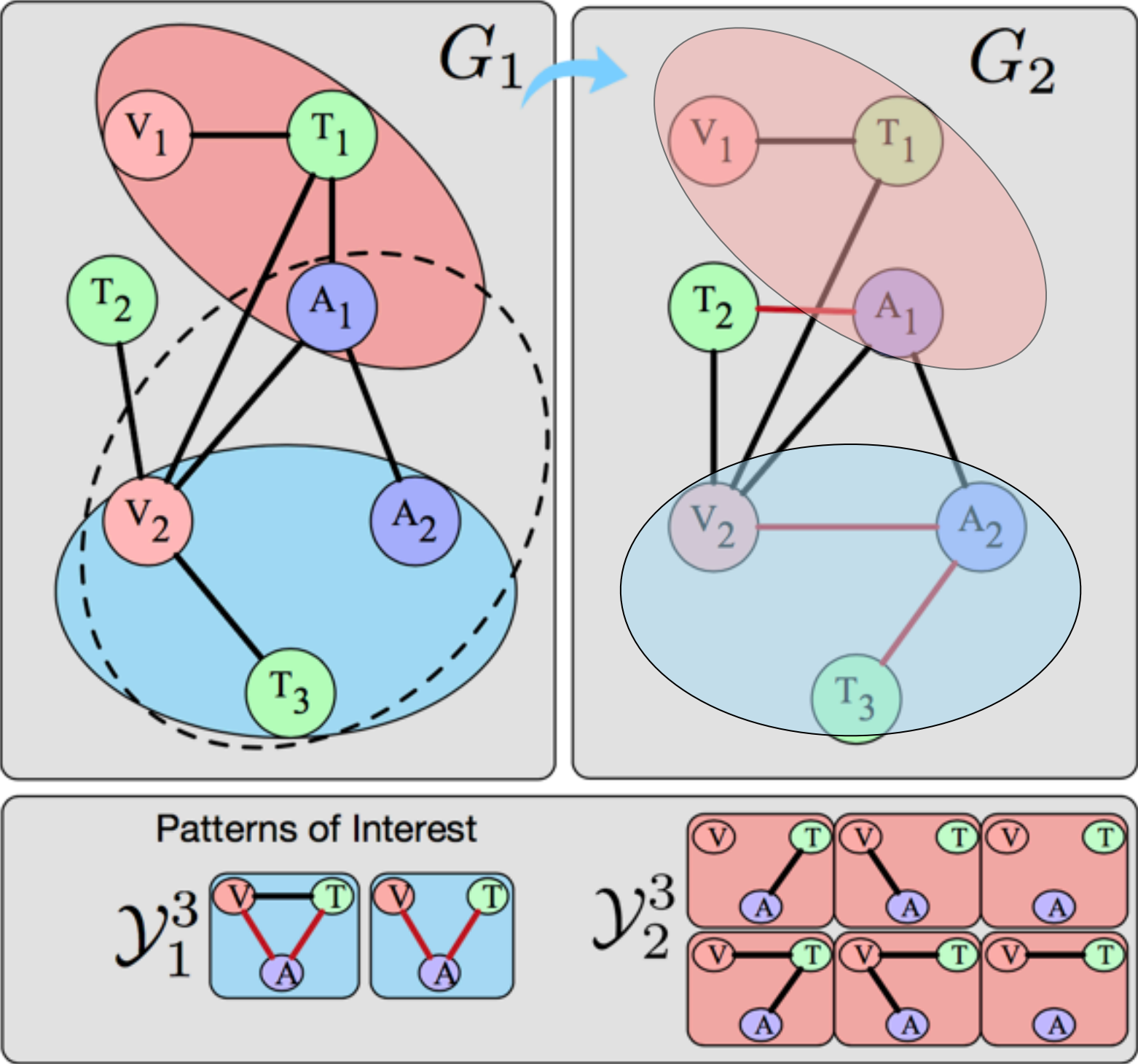
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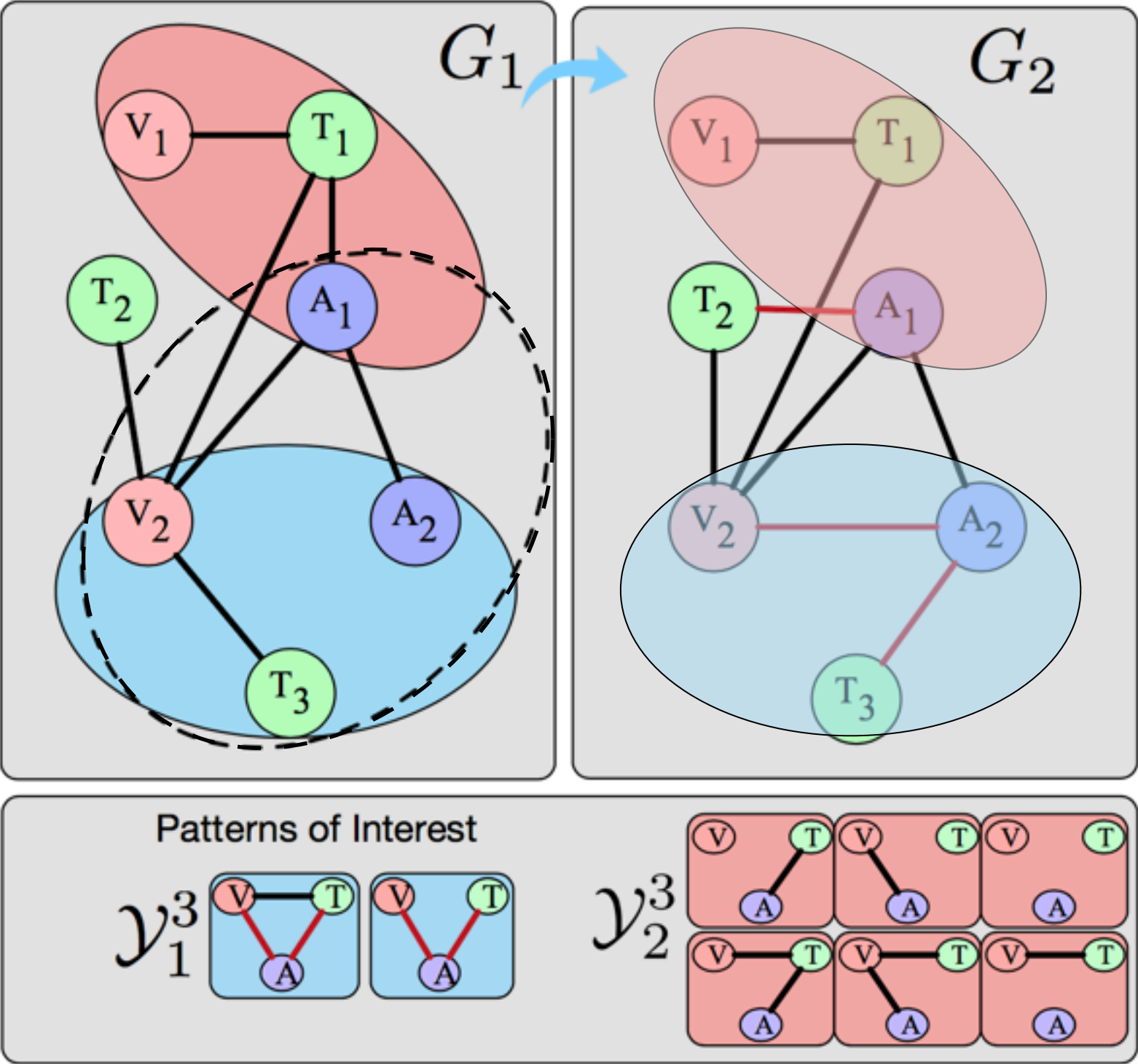
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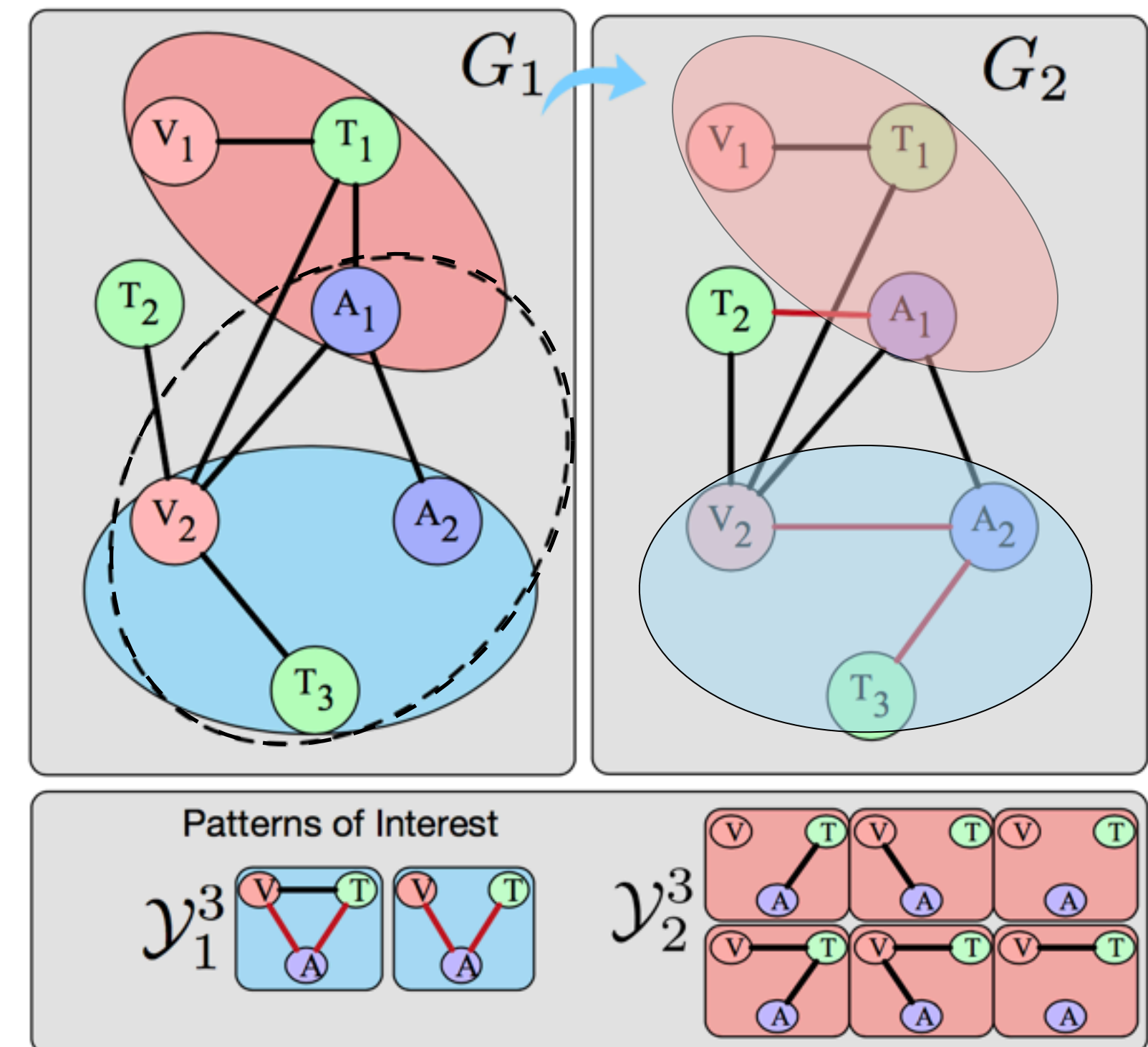
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- **Our model (SPNN):**

- Input features are local induced isomorphism densities within a radius  $d$  of example
- Neural network architecture represents **high-order network structures in local neighborhood**



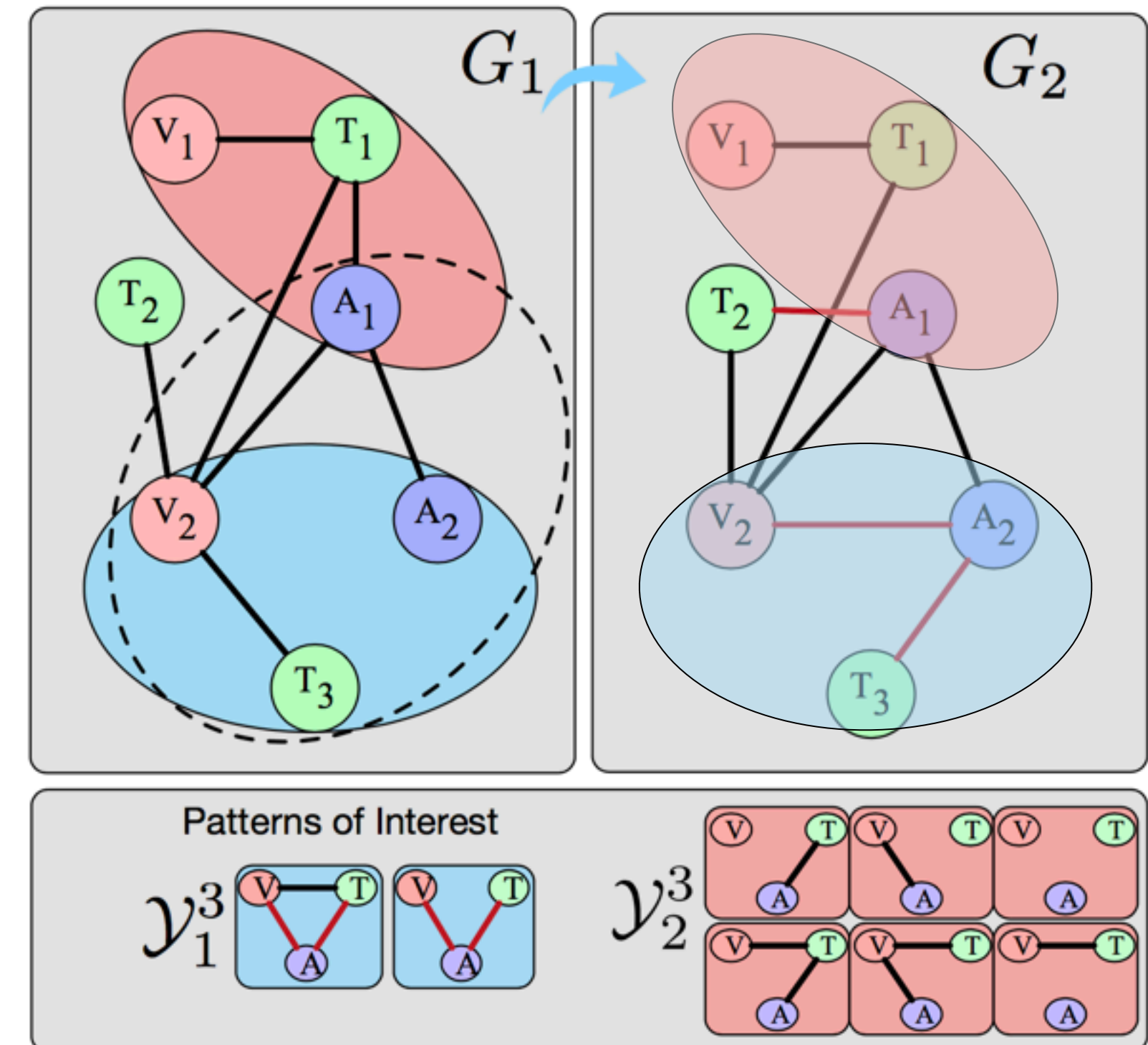
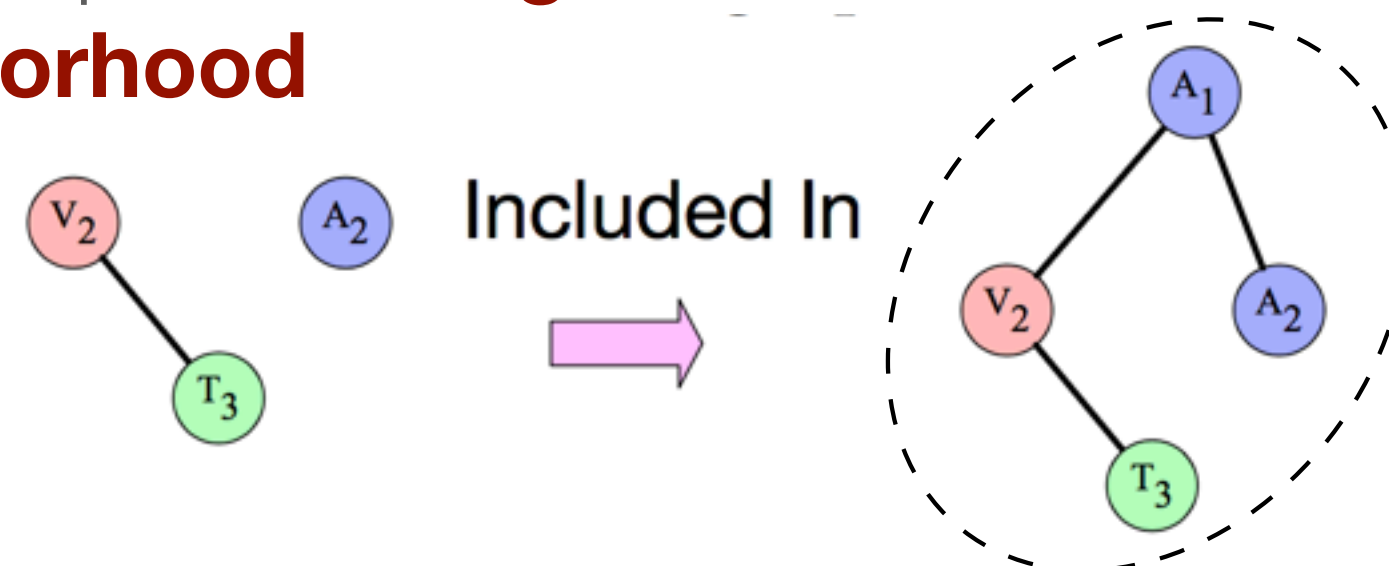
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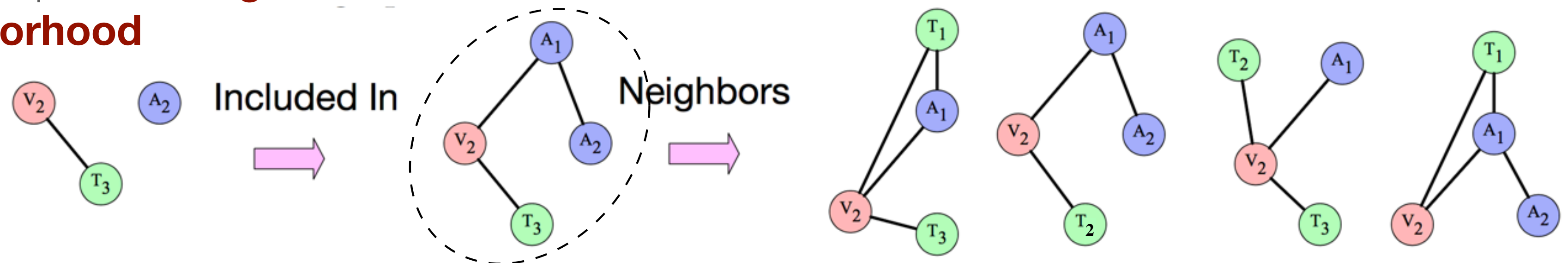
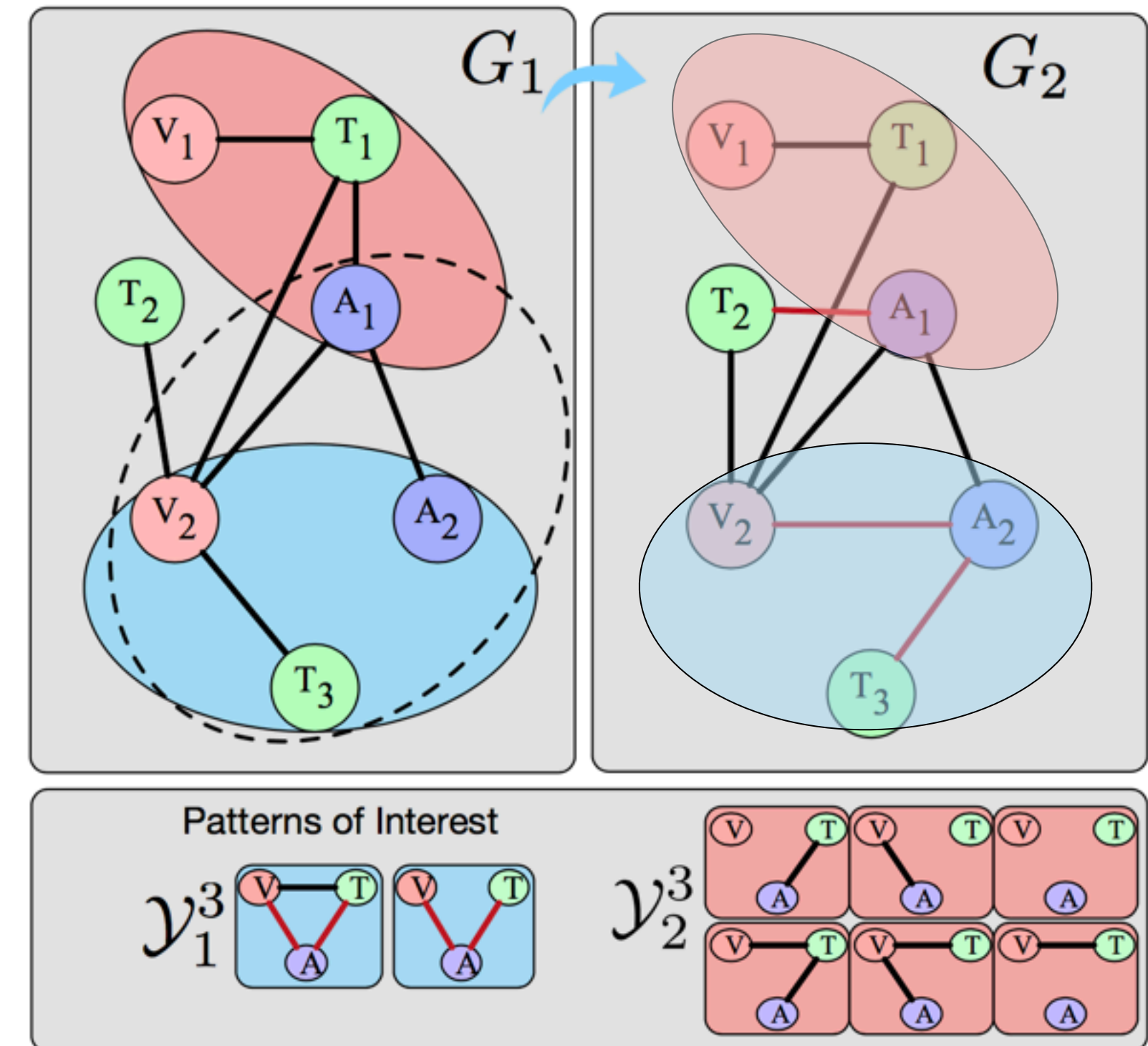
# Subgraph Pattern Neural Network *(Meng, Mouli, Ribeiro, and N AAAI'18)*

- **Problem formulation:**

- Use induced labeled subgraph patterns to map from set of nodes in one time step to next
- Learn subgraph embedding for joint edge-node-attribute predictions
- Examples drawn from larger **connected** subgraphs

- **Our model (SPNN):**

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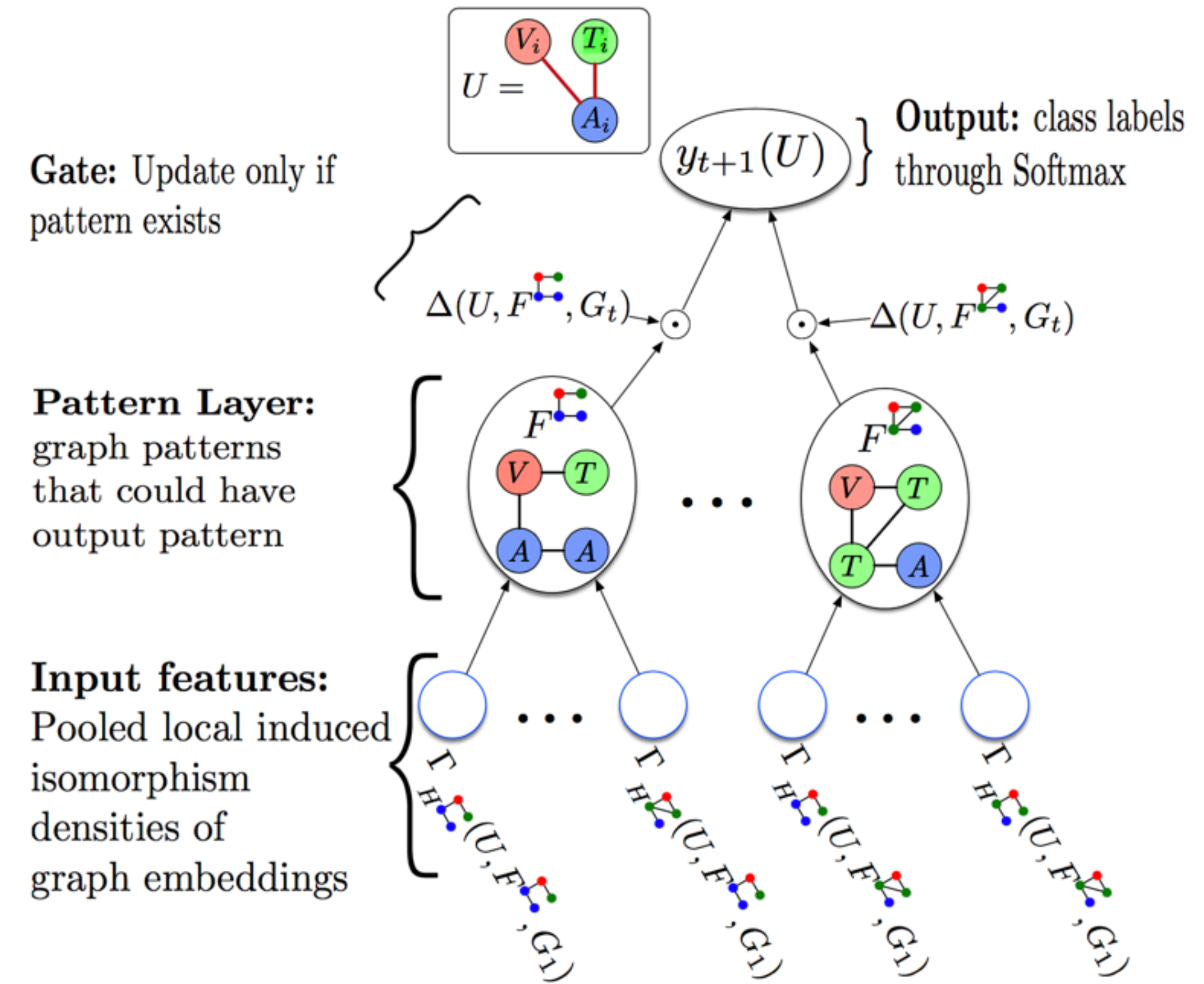
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- SPNN is a 3-layer gated neural network
  - The pattern layer is a set of neurons, each neuron corresponds to one subgraph pattern
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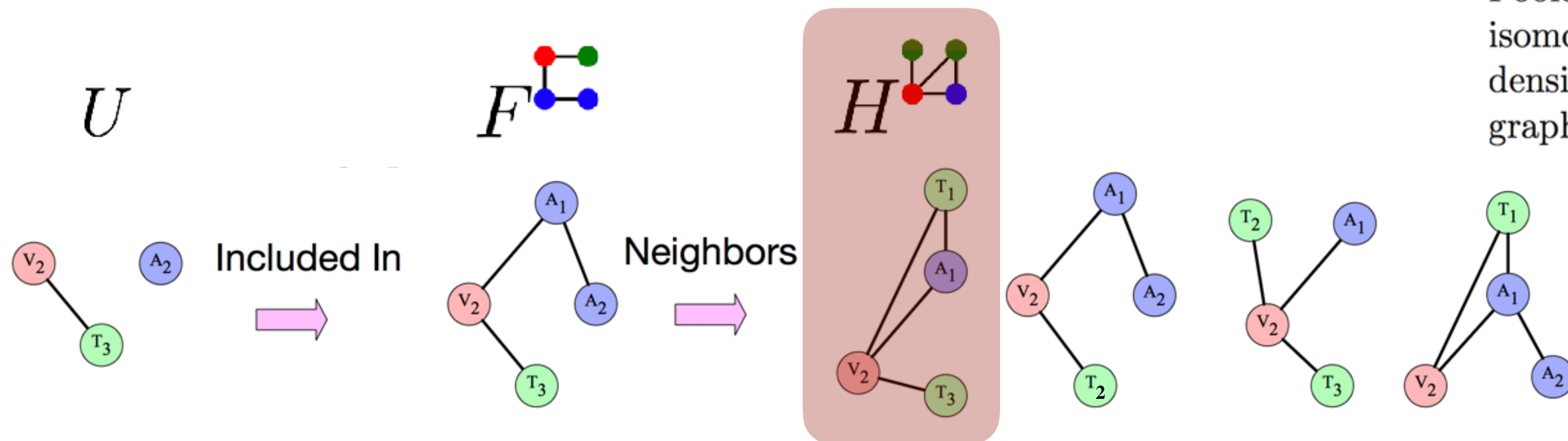
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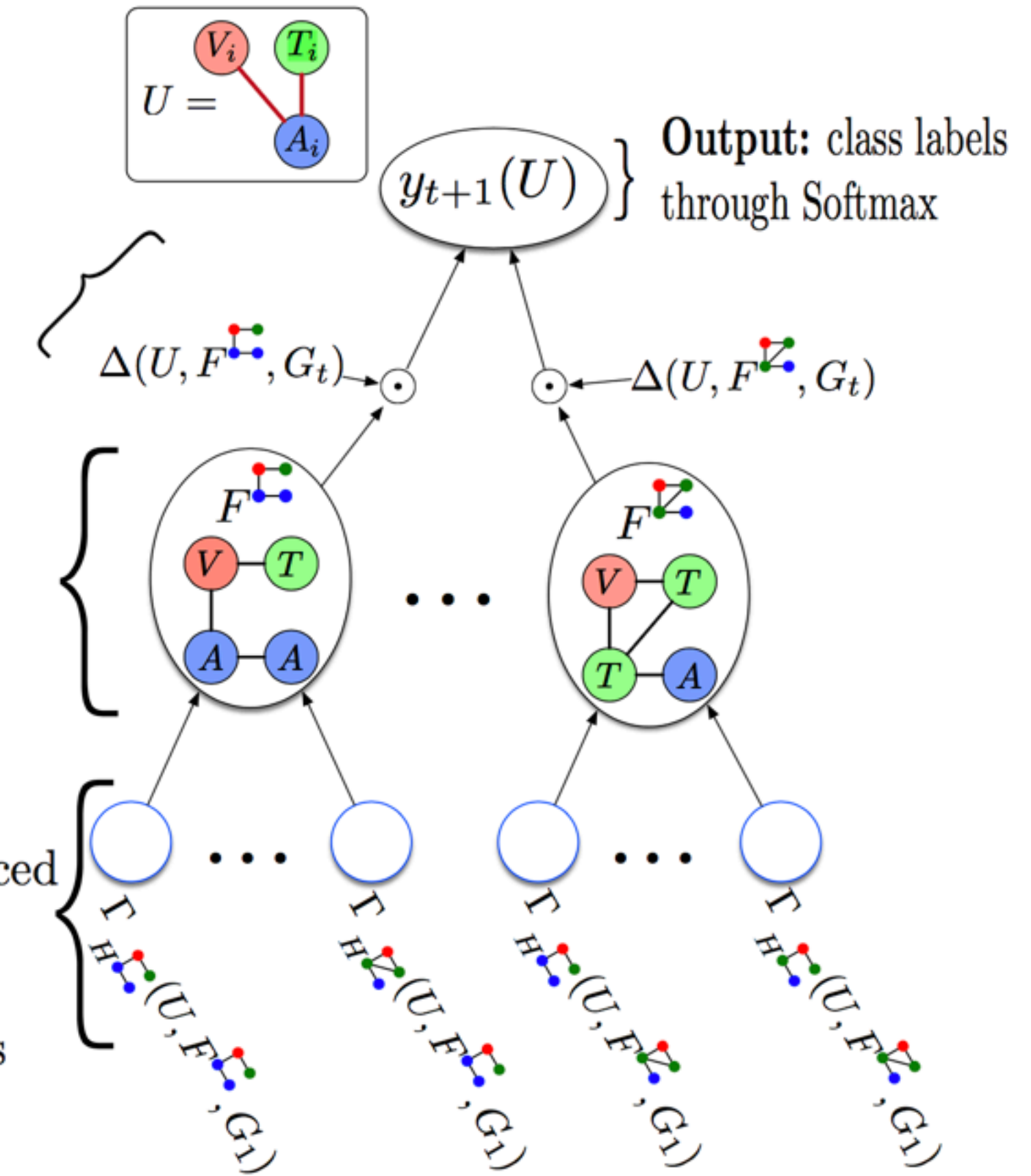
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**Gate:** Update only if pattern exists

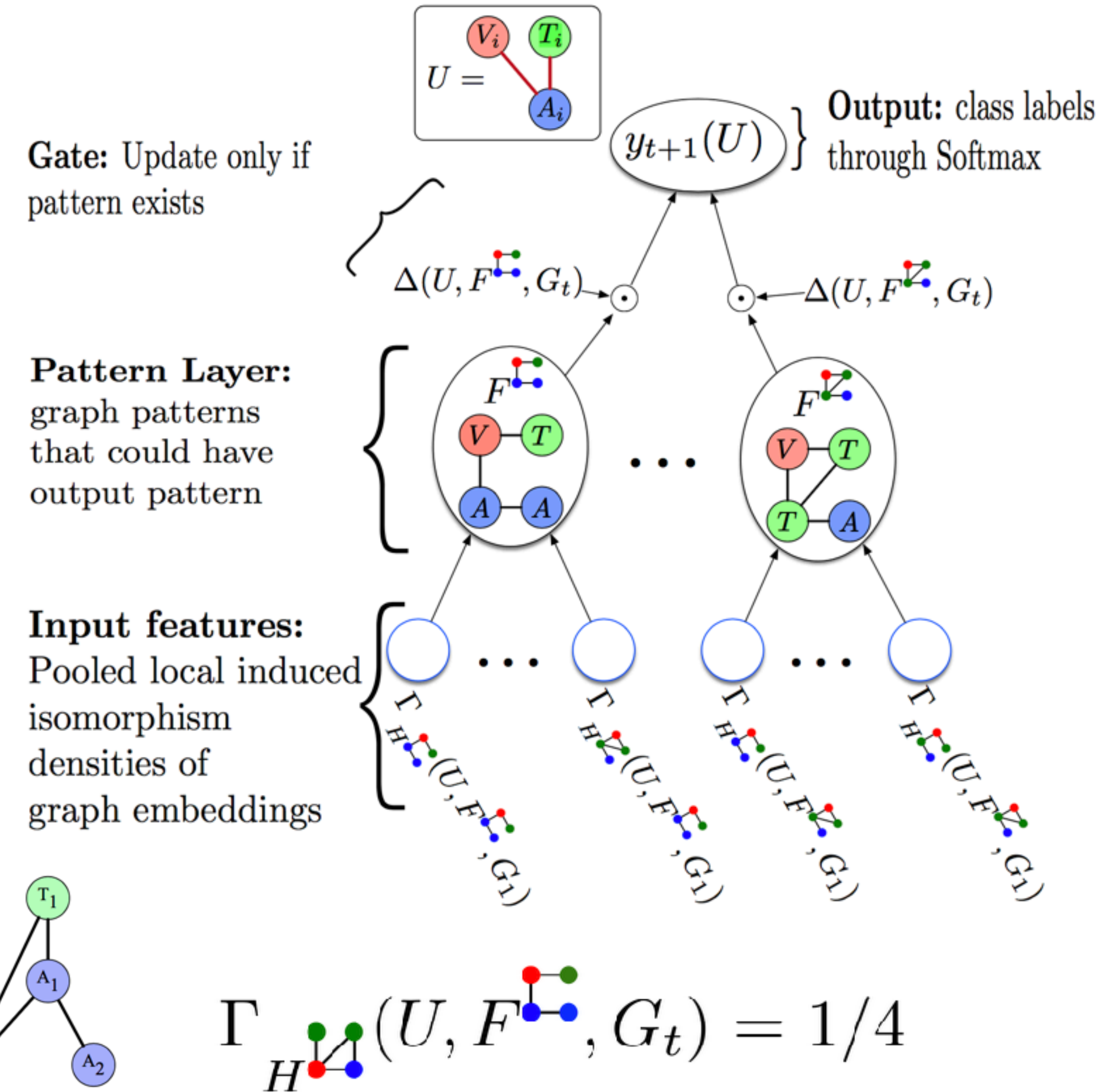
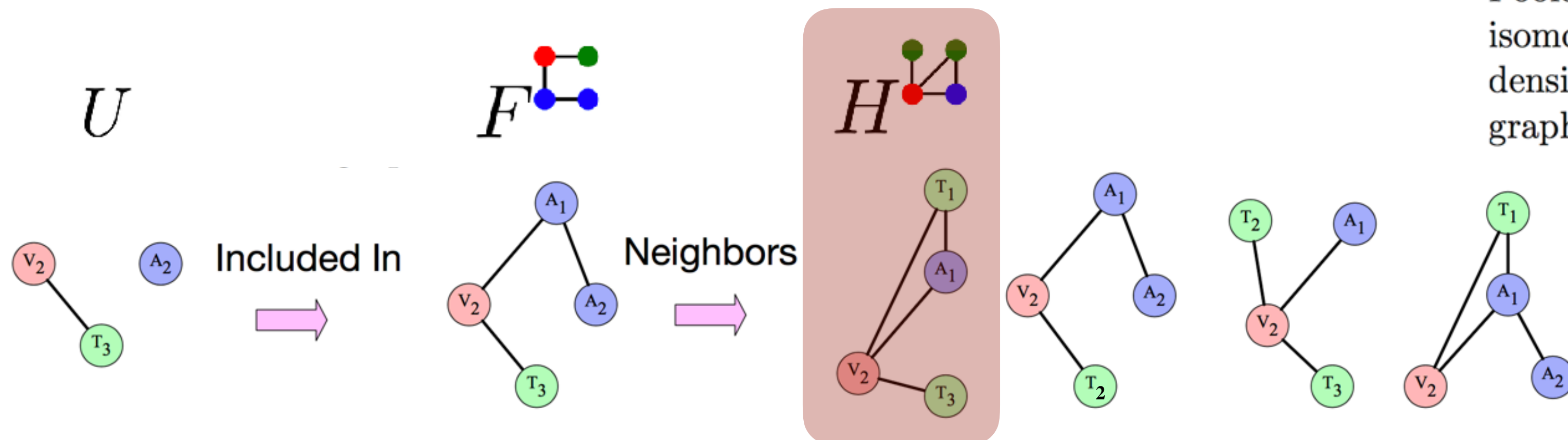
**Pattern Layer:** graph patterns that could have output pattern

**Input features:** Pooled local induced isomorphism densities of graph embeddings



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# Experimental Results

## • Subgraph prediction

### • Datasets.

**DBLP**: scientific papers in four related areas with 14k papers, 14k authors, 8k topics, and 20 venues

**Friendster**: 14 millions users with hometown, college, interests, and 75 million messages between users

### • Results.

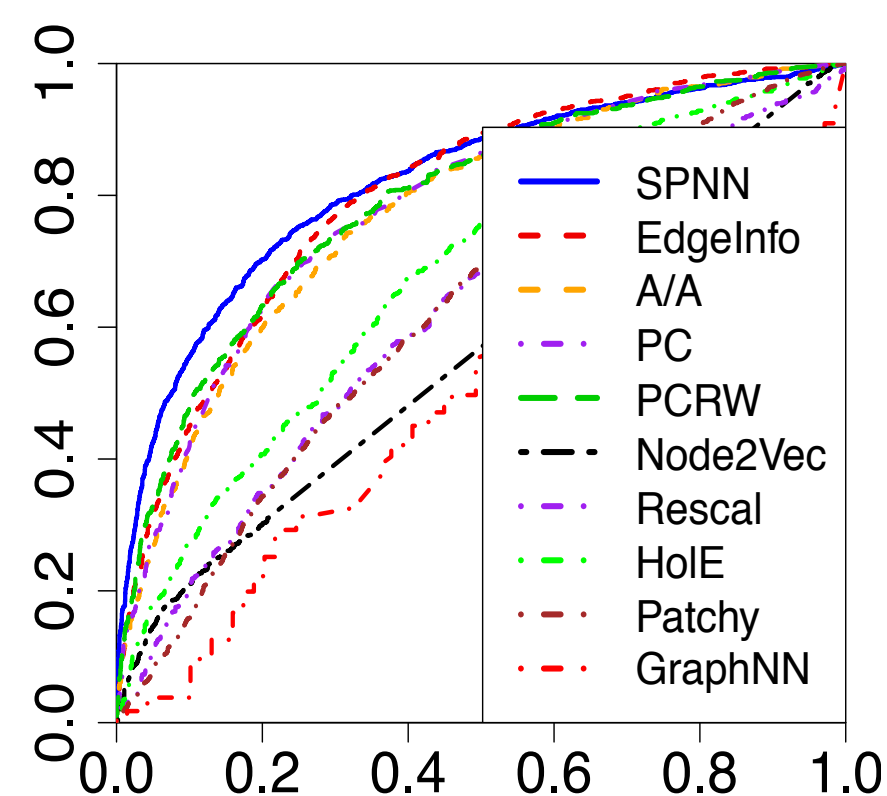
Improved subgraph prediction accuracy in tasks: (a) Topology Evolution, (b) Activity Level Prediction, (c) Group dissolution

**AUC score**

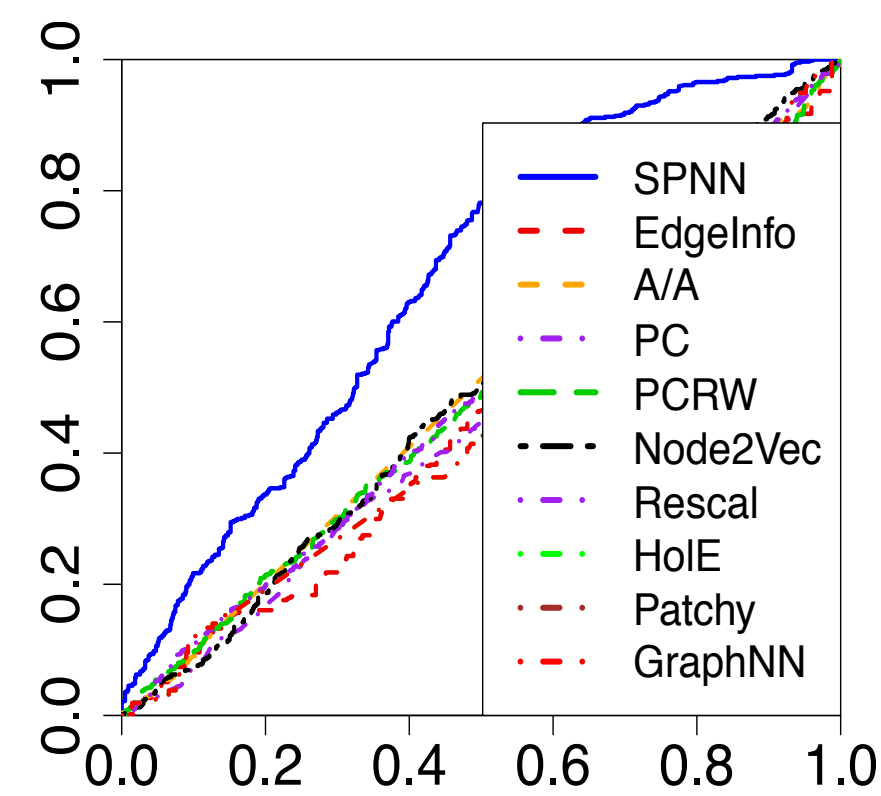
**ROC curve**

### Jointly Trained Multi-Link Task

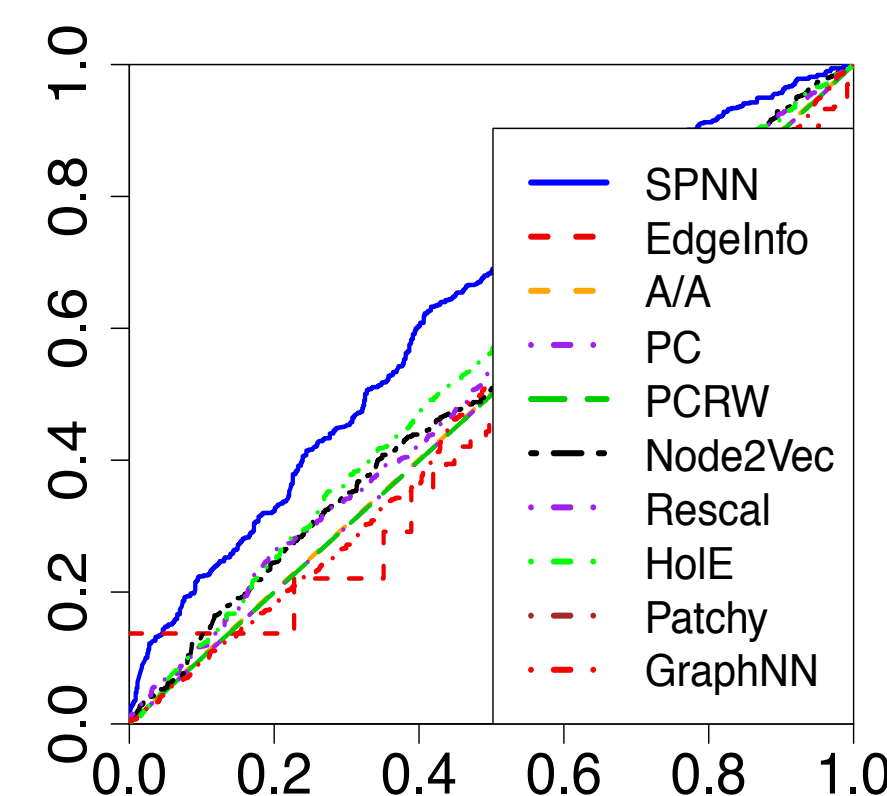
	EdgeInfo	PCRW	PC	N2V	Rescal	HolE	Patchy	GraphNN	<b>SPNN</b>
DBLP	0.830	0.782	0.788	0.582	0.611	0.690	0.627	0.571	<b>0.846</b>
	$\pm 0.007$	$\pm 0.007$	$\pm 0.014$	$\pm 0.007$	$\pm 0.025$	$\pm 0.024$	$\pm 0.003$	$\pm 0.021$	$\pm 0.011$
Friendster (Activity)	0.502	0.516	0.515	0.524	0.502	0.506	0.519	0.521	<b>0.690</b>
	$\pm 0.007$	$\pm 0.012$	$\pm 0.012$	$\pm 0.018$	$\pm 0.012$	$\pm 0.013$	$\pm 0.010$	$\pm 0.023$	$\pm 0.008$
Friendster (Structure)	0.501	0.502	0.552	0.540	0.521	0.530	0.547	0.523	<b>0.607</b>
	$\pm 0.004$	$\pm 0.002$	$\pm 0.019$	$\pm 0.017$	$\pm 0.017$	$\pm 0.021$	$\pm 0.025$	$\pm 0.019$	$\pm 0.017$



(a) DBLP



(b) Friendster Activity



(c) Friendster Structure

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## • Subgraph prediction

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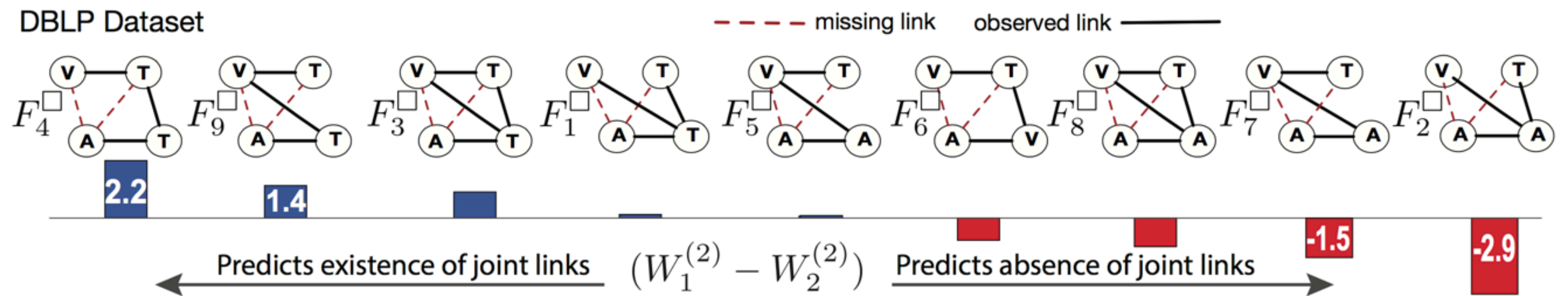
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## Pattern weights explain predictions



Translational embeddings using message content

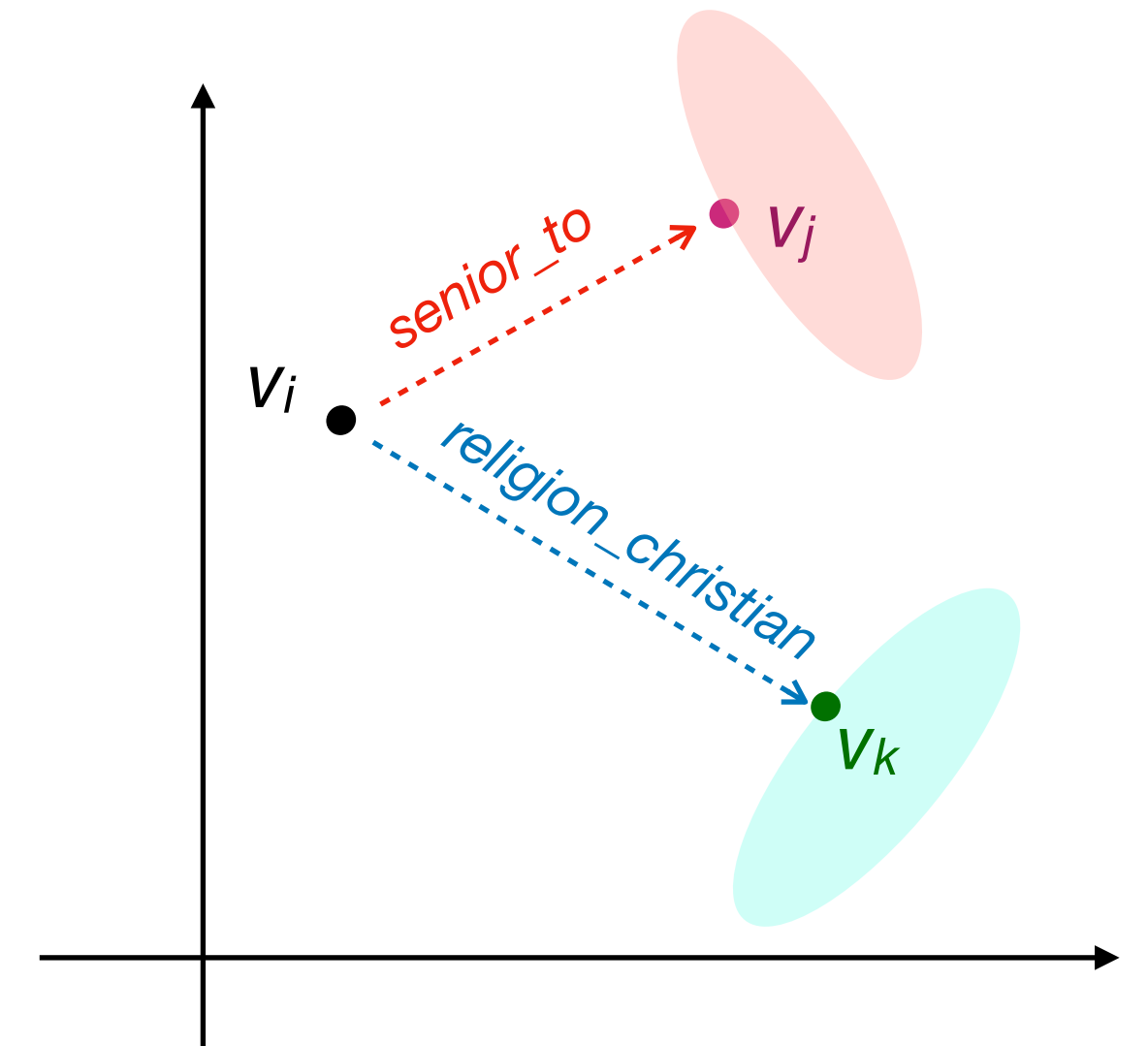
# Learning translational social relation embeddings

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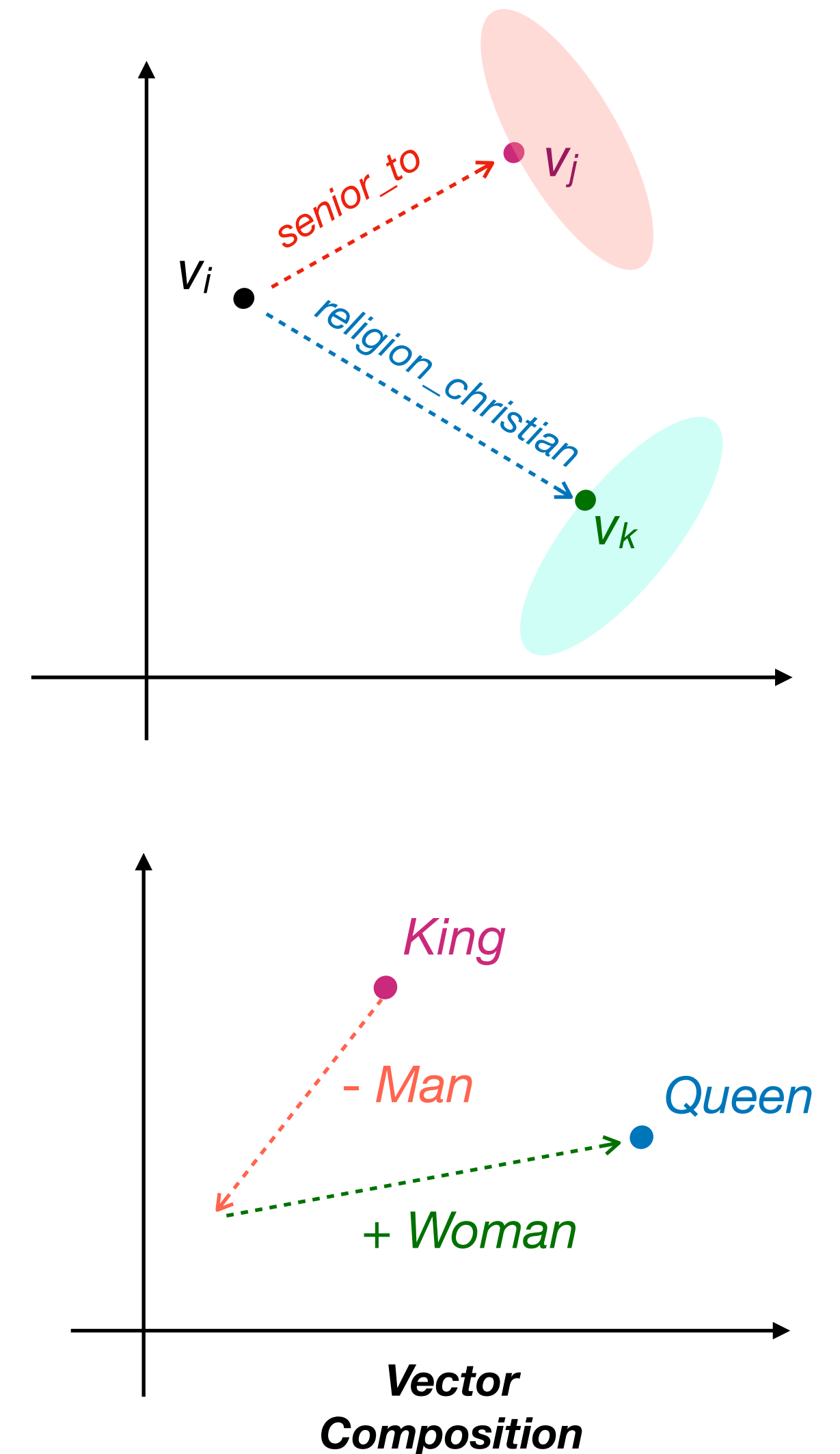
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- **Task:** Learn explicit relationship representation between users in social networks
  - Perform link prediction through vector composition
  - Recommend friends directly via relationship types



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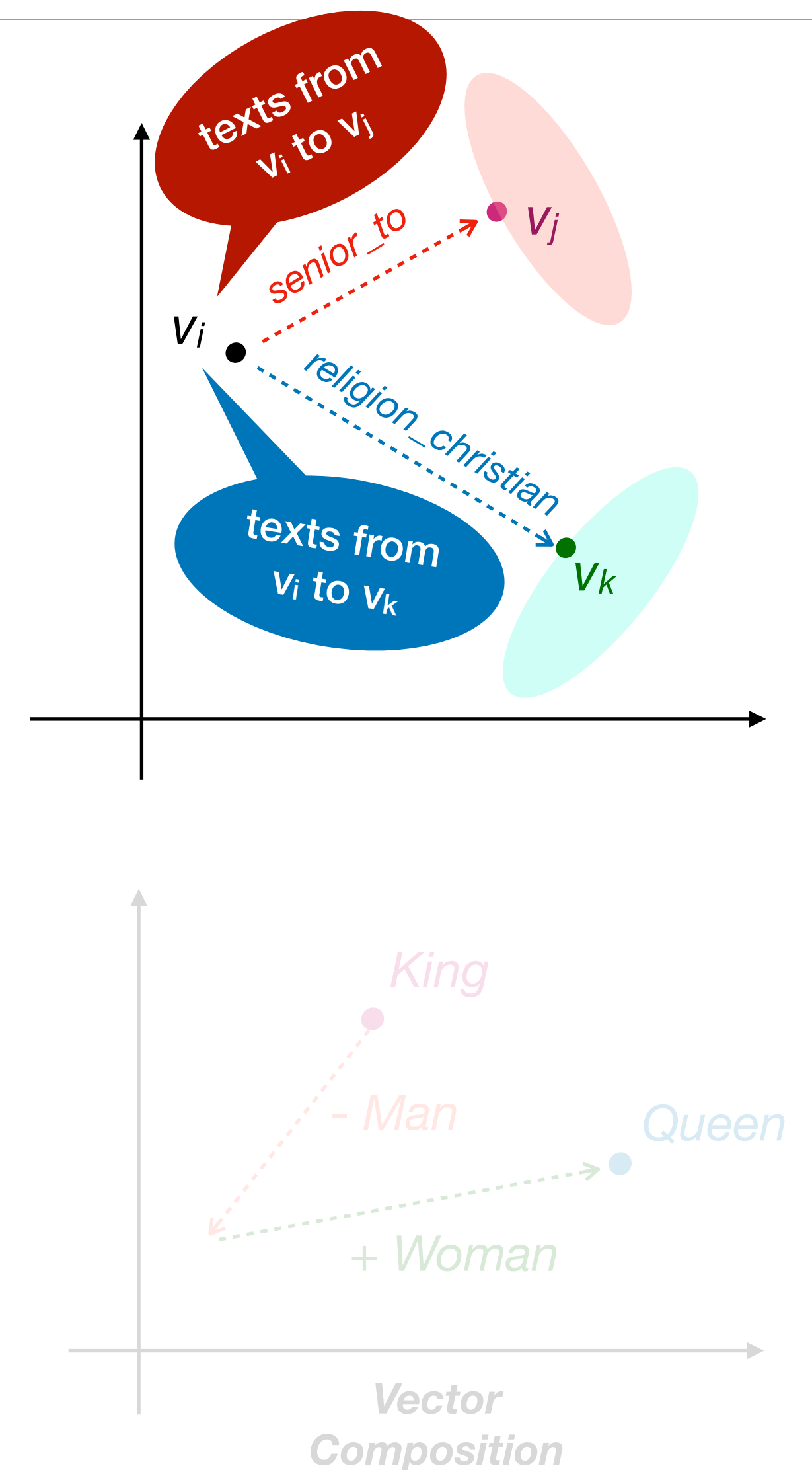
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  - *Word2Vec (Mikolov et al '13) uses vector arithmetic to encode word analogies*
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- **Goal:**
  - Learn edge representation explicitly
  - Consider multiple relationships between pair of users
  - Consider textual interactions between pair of users



# Conversation-based factors

---

- Textual communication reflects the **degree of affinity** and **intensity of interaction** between  $u_i$  and  $u_j$



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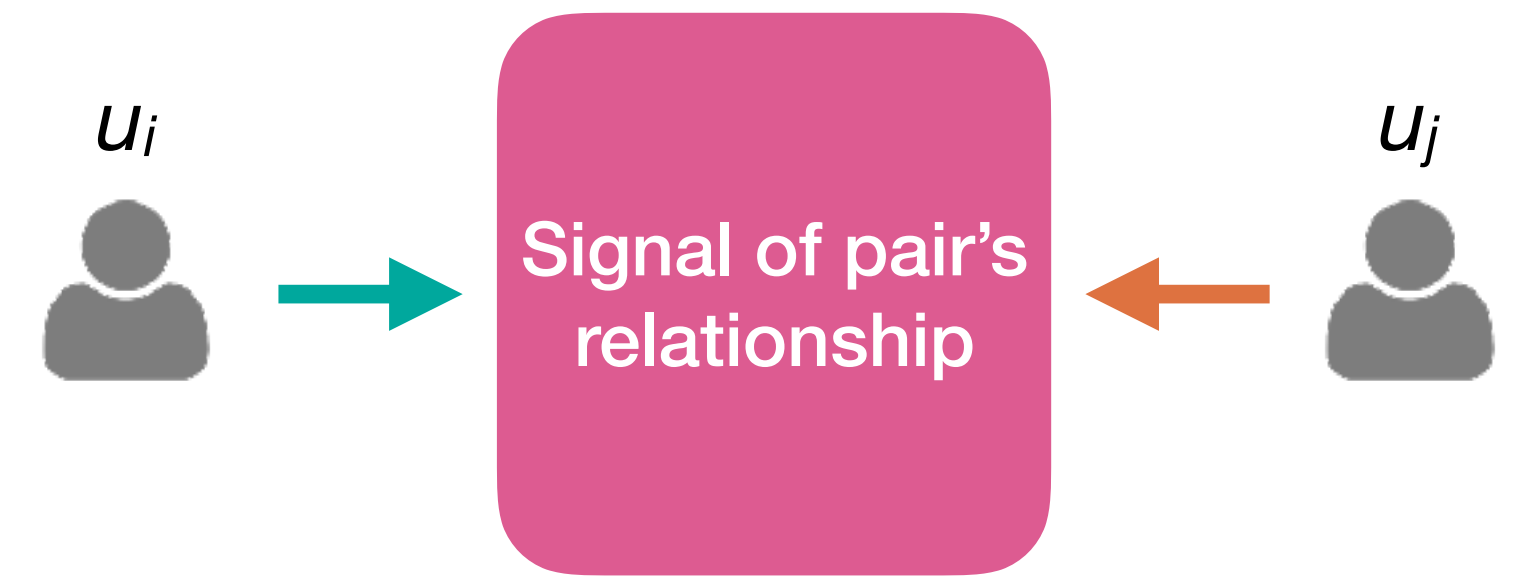
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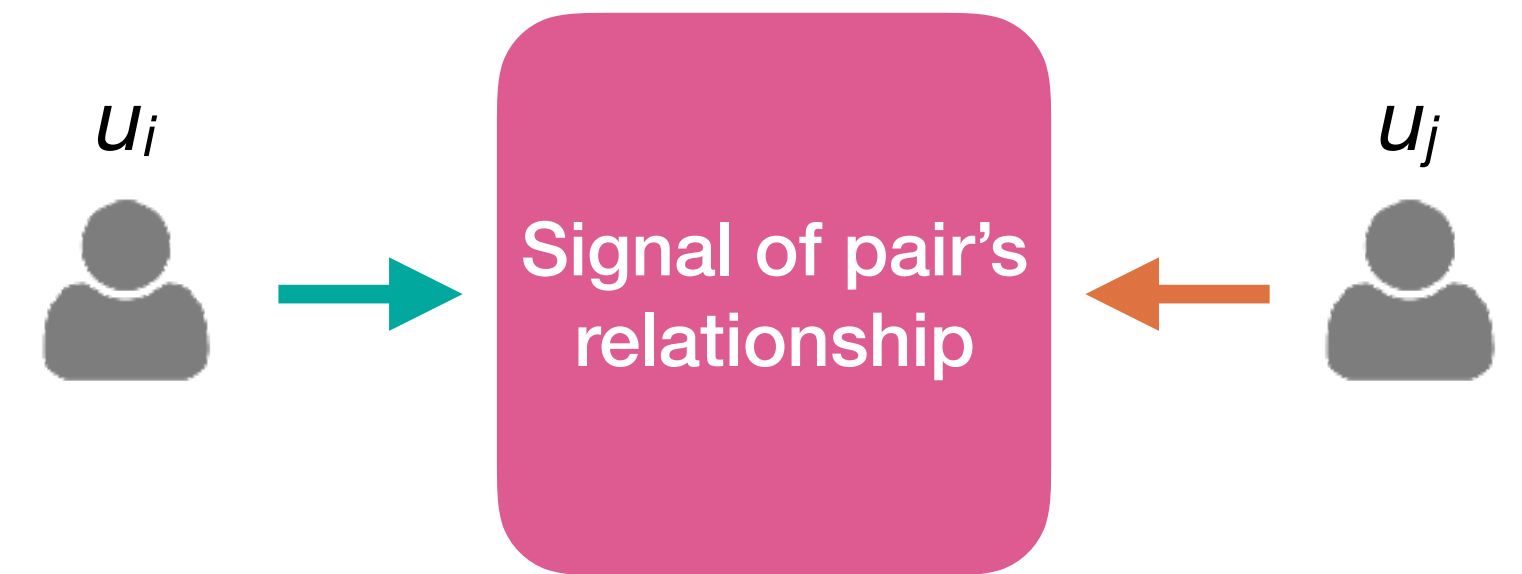
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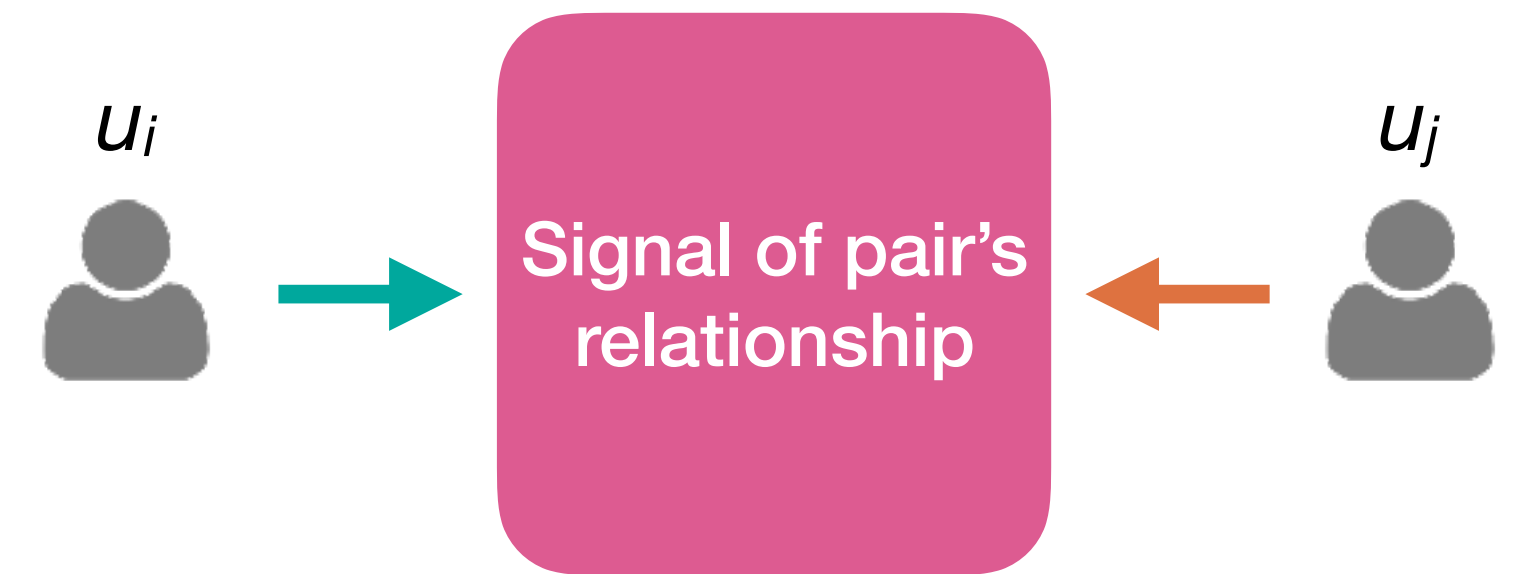
- Capture textual similarity of interaction
- Identify most representative set of words as dictionary  $W_r$  for each relation  $r \in R$
- Based on  $W_r$ , transform conversations  $u_i \rightarrow u_j$  and  $u_j \rightarrow u_i$  to relevant word vectors and then compute the similarity

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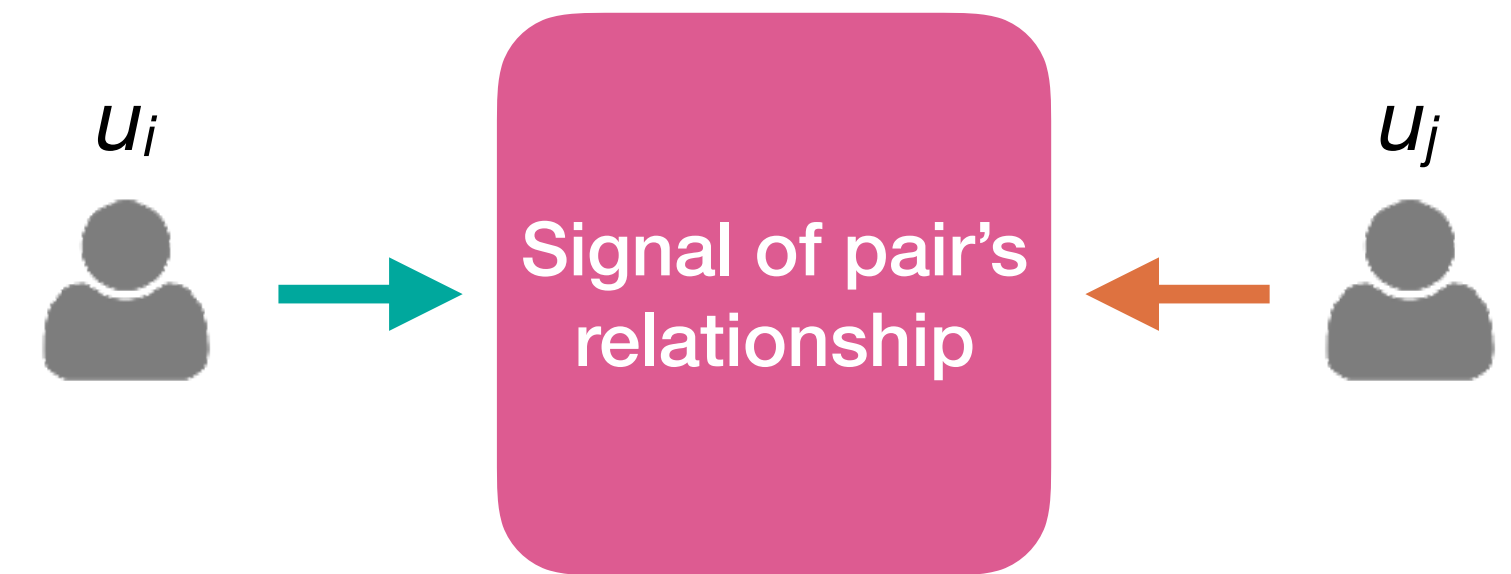
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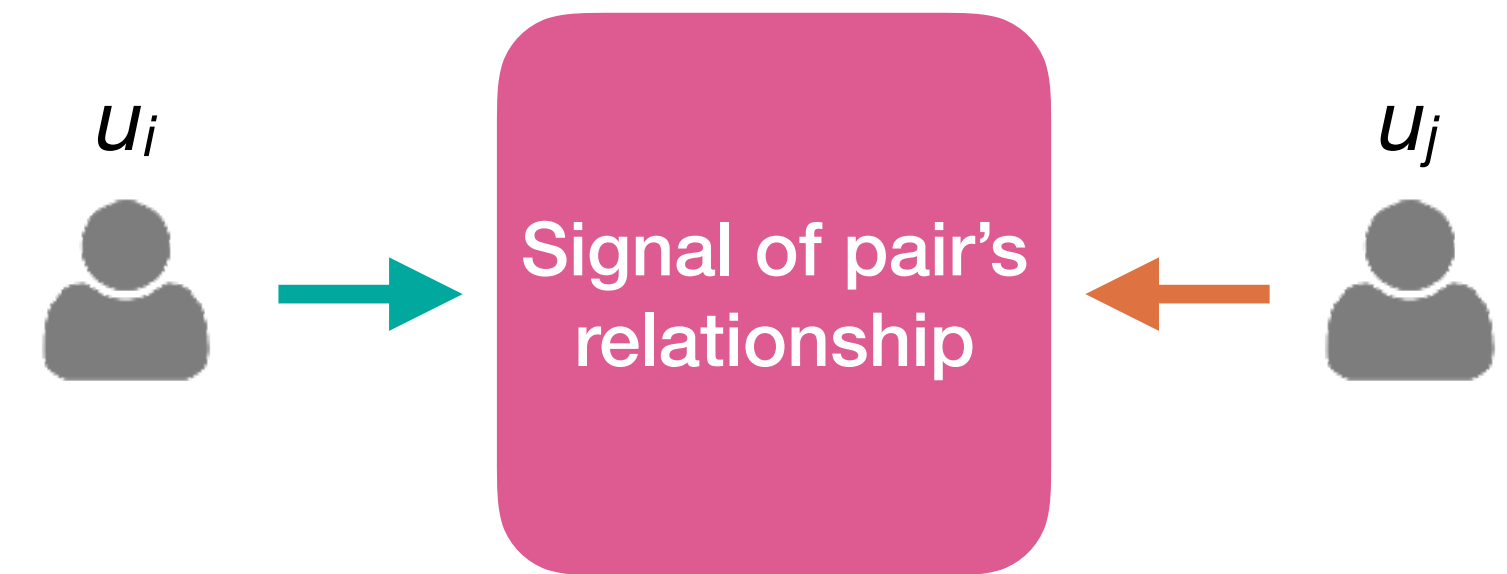
- Conversation Frequency Factor ( $\Phi^{r_{ij}}$ )**

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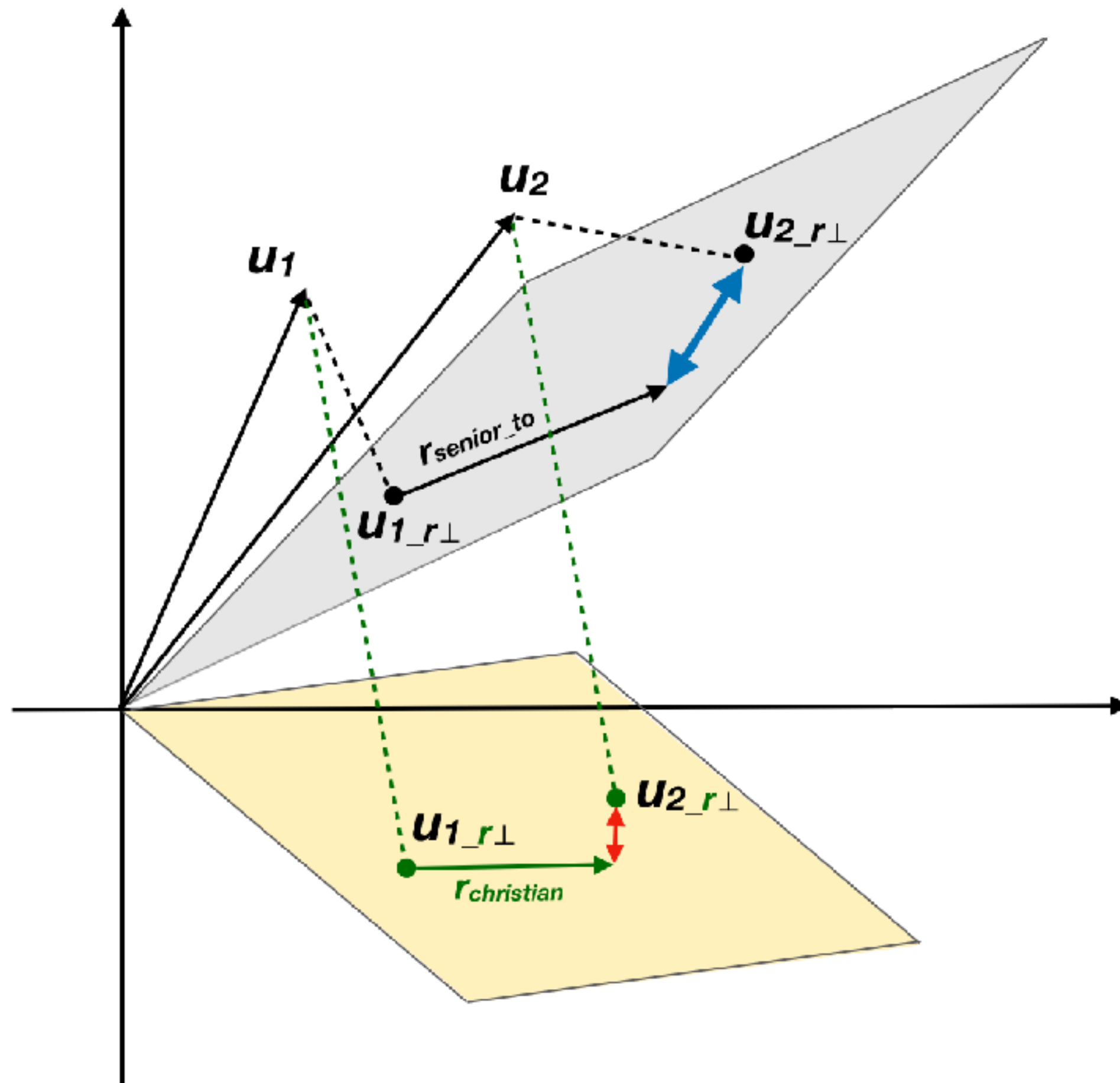
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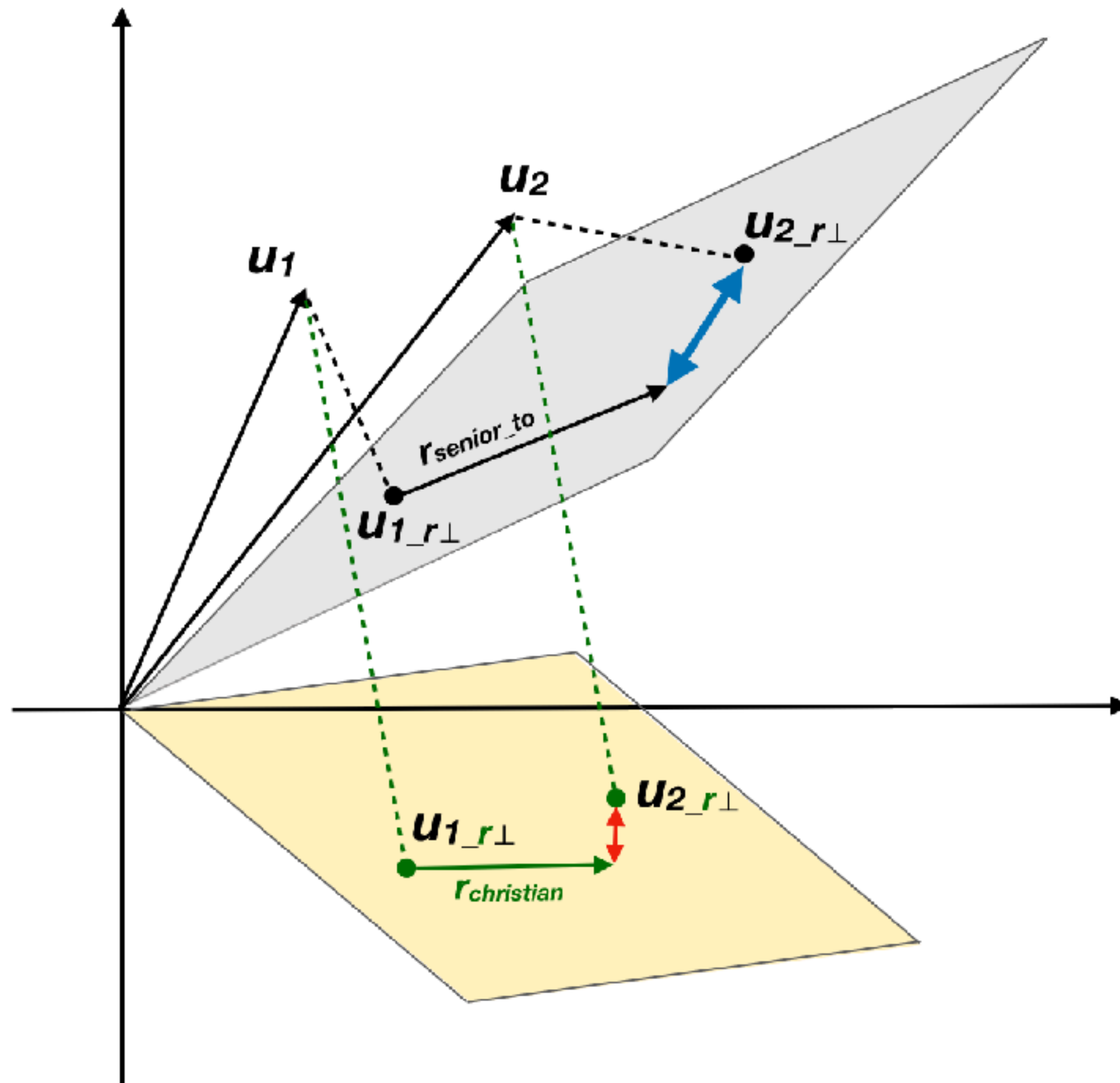
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Higher  $\Phi^{r_{ij}}$  indicates pair have stronger interaction wrt  $r$

# Trans-Conv Relational Embeddings *(Lai, N, and Goldwasser AAAI'19)*



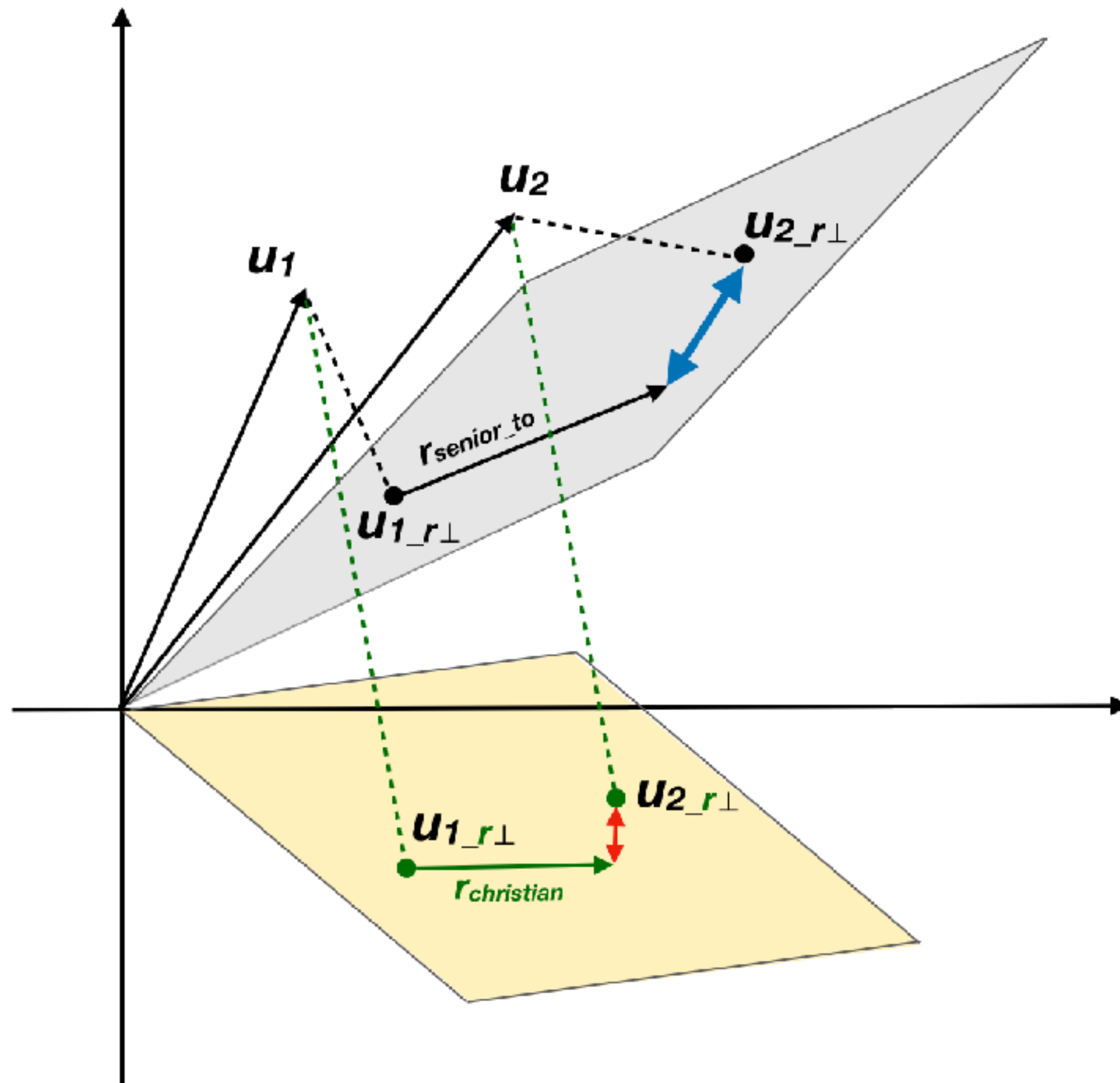
# Trans-Conv Relational Embeddings *(Lai, N, and Goldwasser AAAI'19)*



## Example:

- $u_1$  and  $u_2$  have two relationships in data:  $(u_1, r_{senior\_to}, u_2)$ ,  $(u_1, r_{christian}, u_2)$ .
- But  $u_1$  and  $u_2$  discussion focuses more on *christian* topics than *senior\_to* topics
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- Conversational factors capture this to indicate which relation is stronger

- Learn embeddings jointly with relation-specific hyperplanes
- Score function  $f_r$  measures the plausibility that the triplet  $(u_i, r, u_j)$  is incorrect

$$f_r(u_i, u_j) = [1 + \underbrace{\alpha \mu_{ij}^r + (1 - \alpha) \phi_{ij}^r}_{\text{conversational factors}}] \|\hat{u}_{i\perp} + \hat{r} - \hat{u}_{j\perp}\|_{l_{1/2}}$$

**conversational factors**

# Experimental Results

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- **Link prediction**

# Experimental Results

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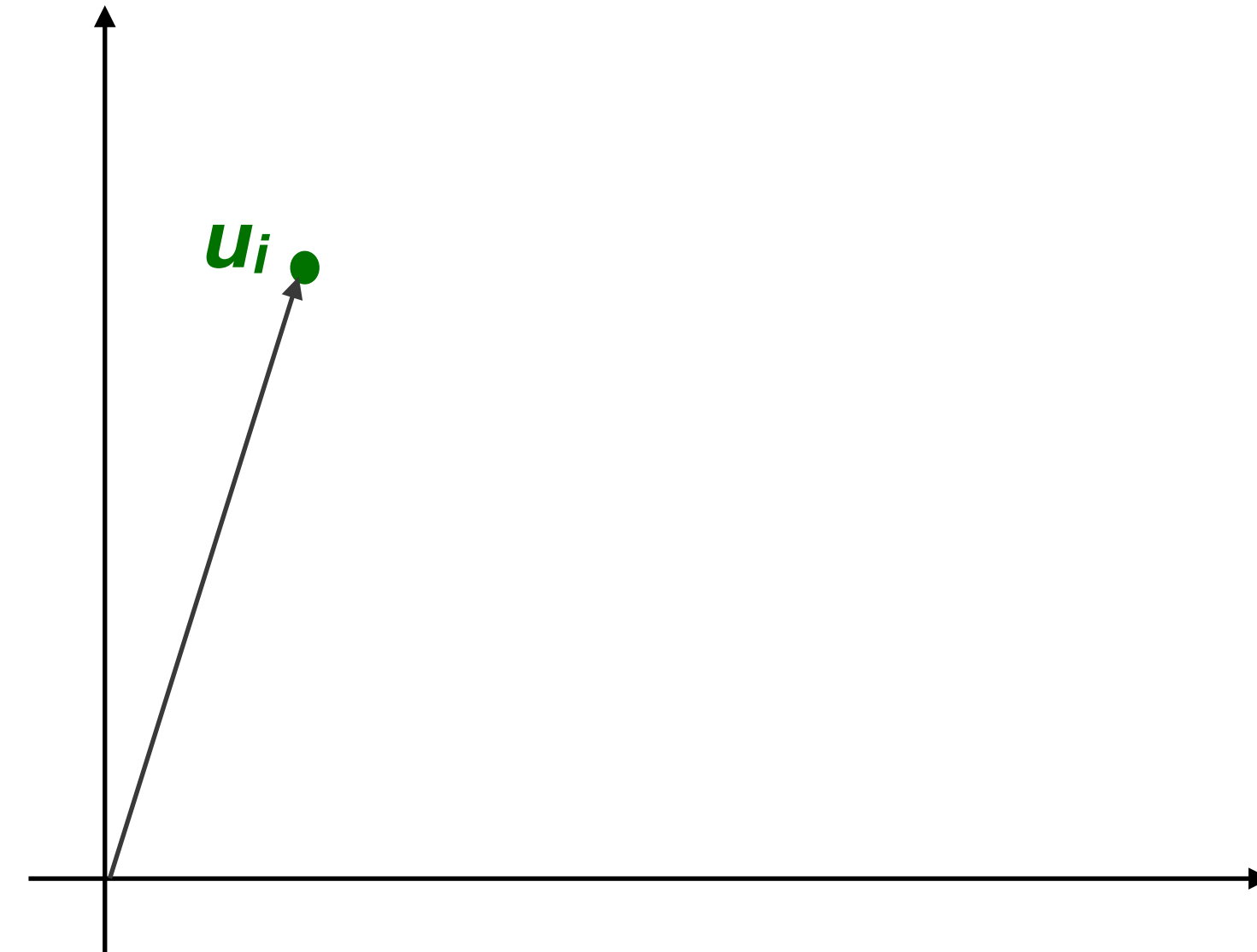
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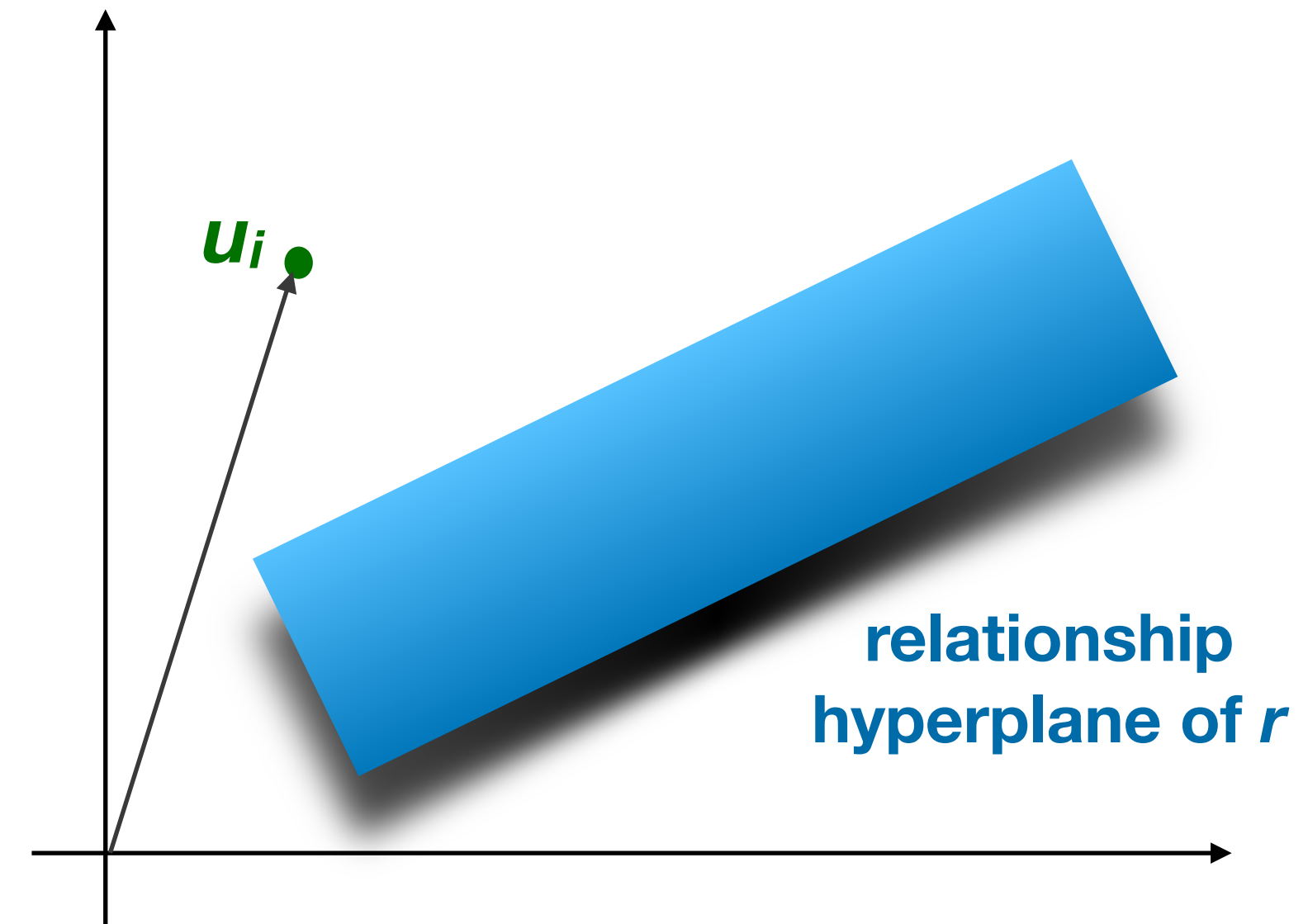
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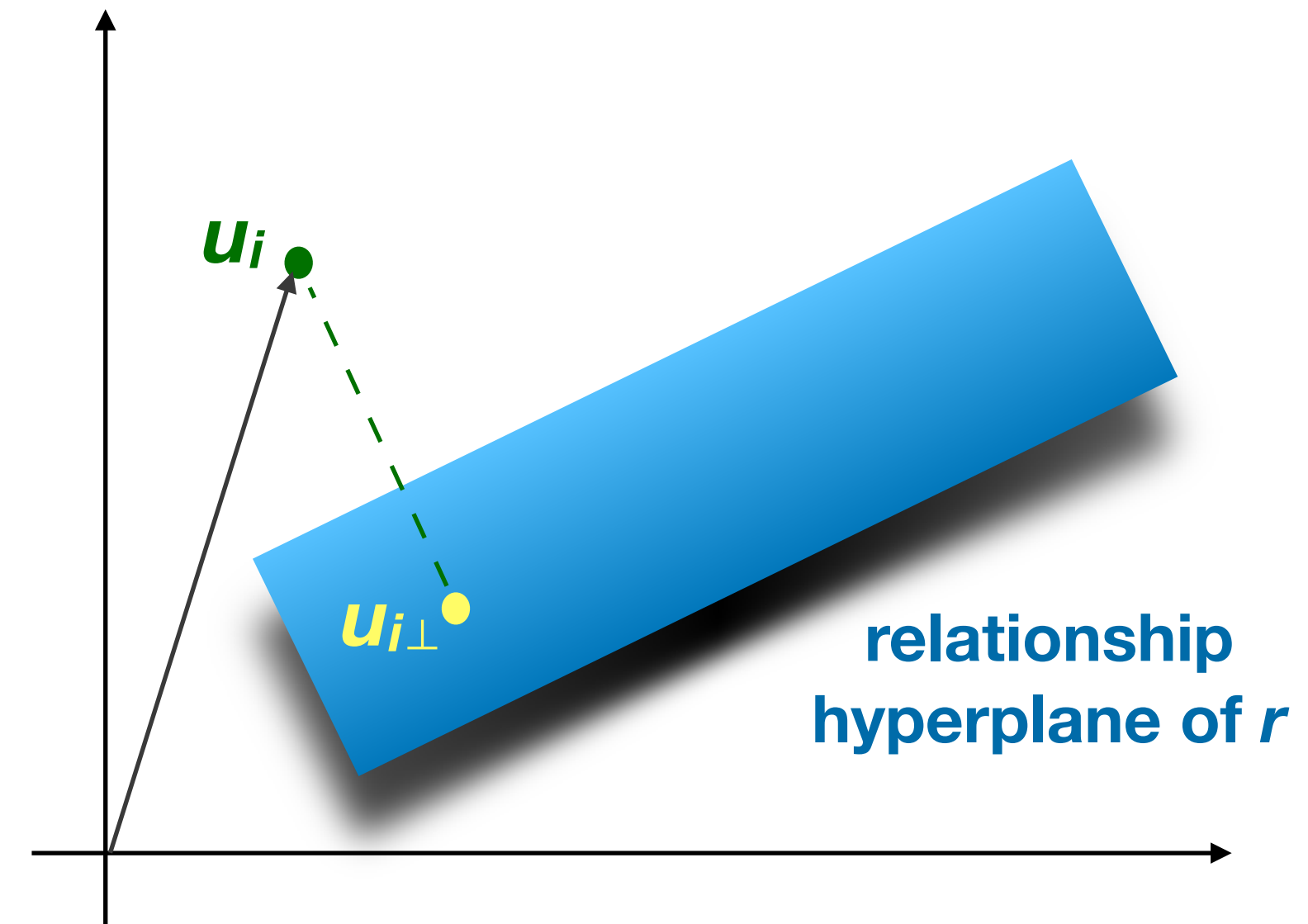




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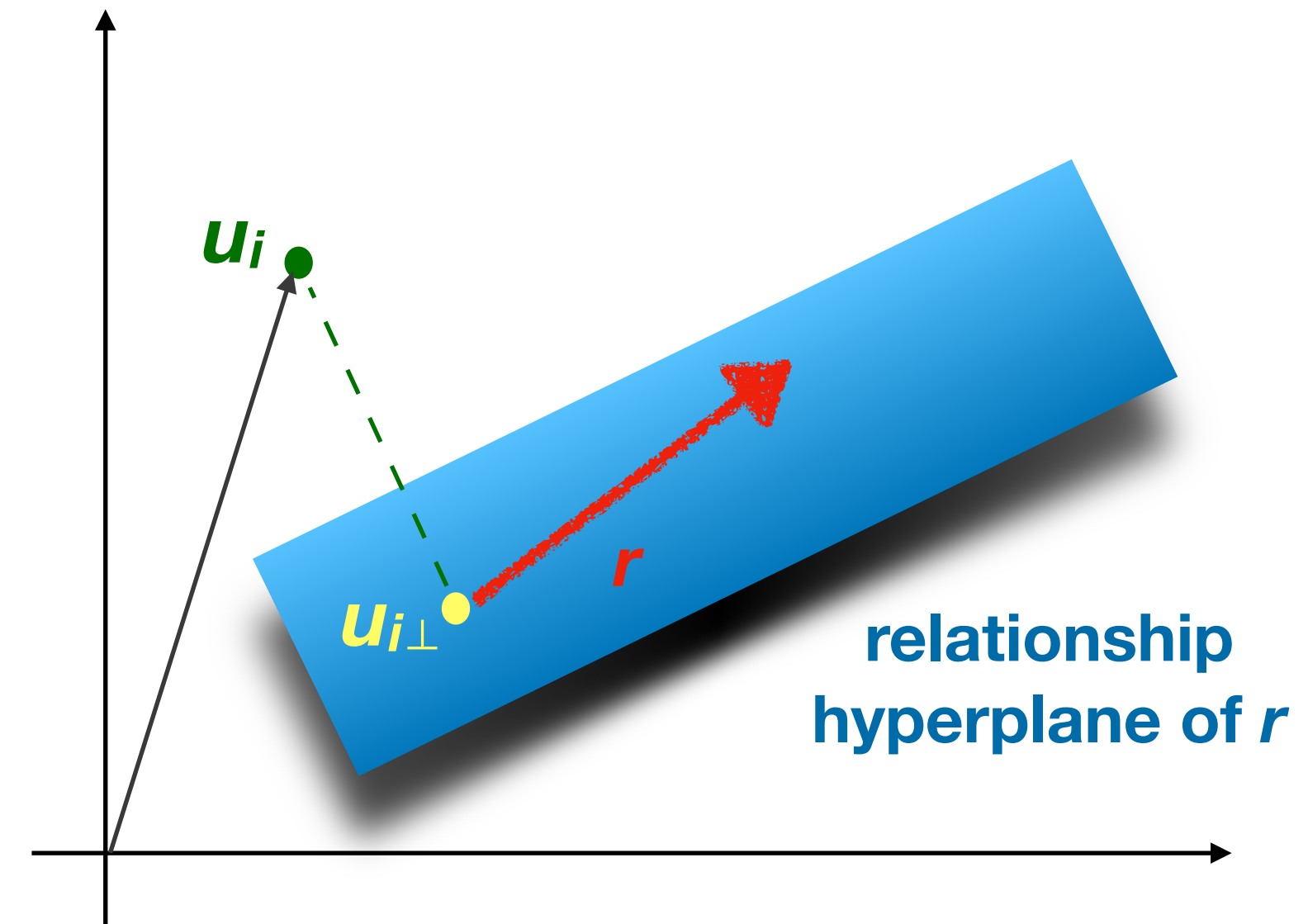
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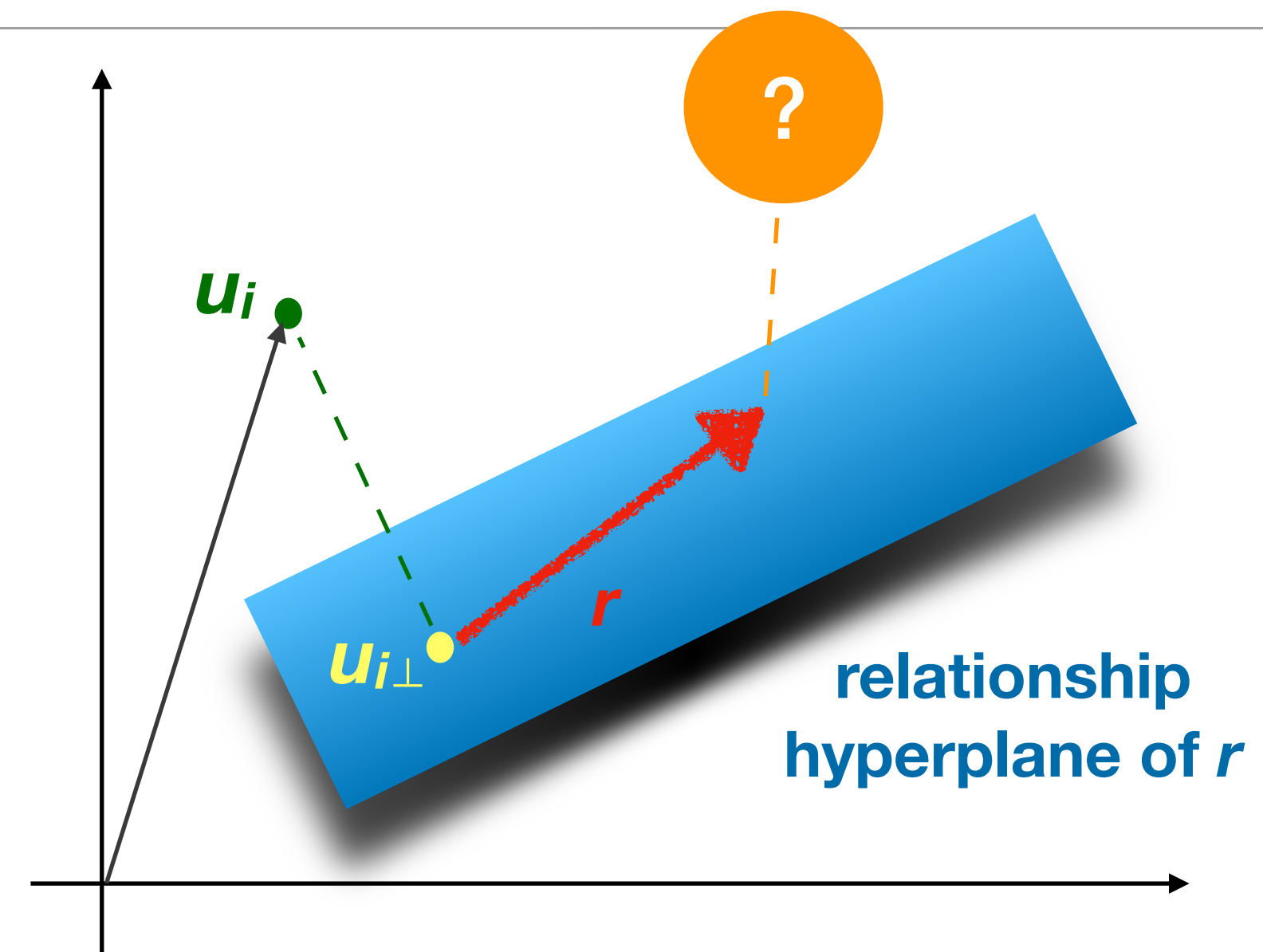
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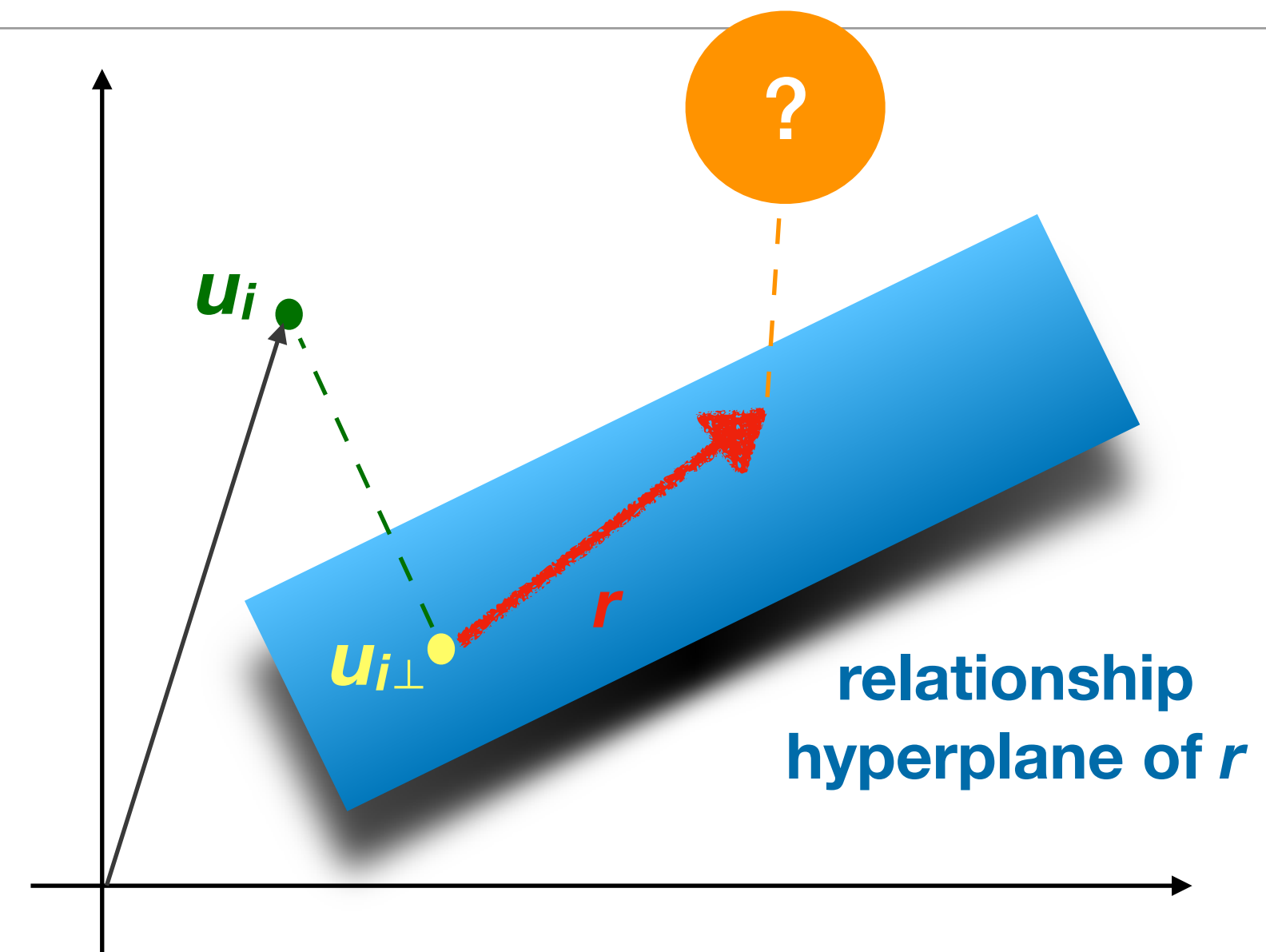
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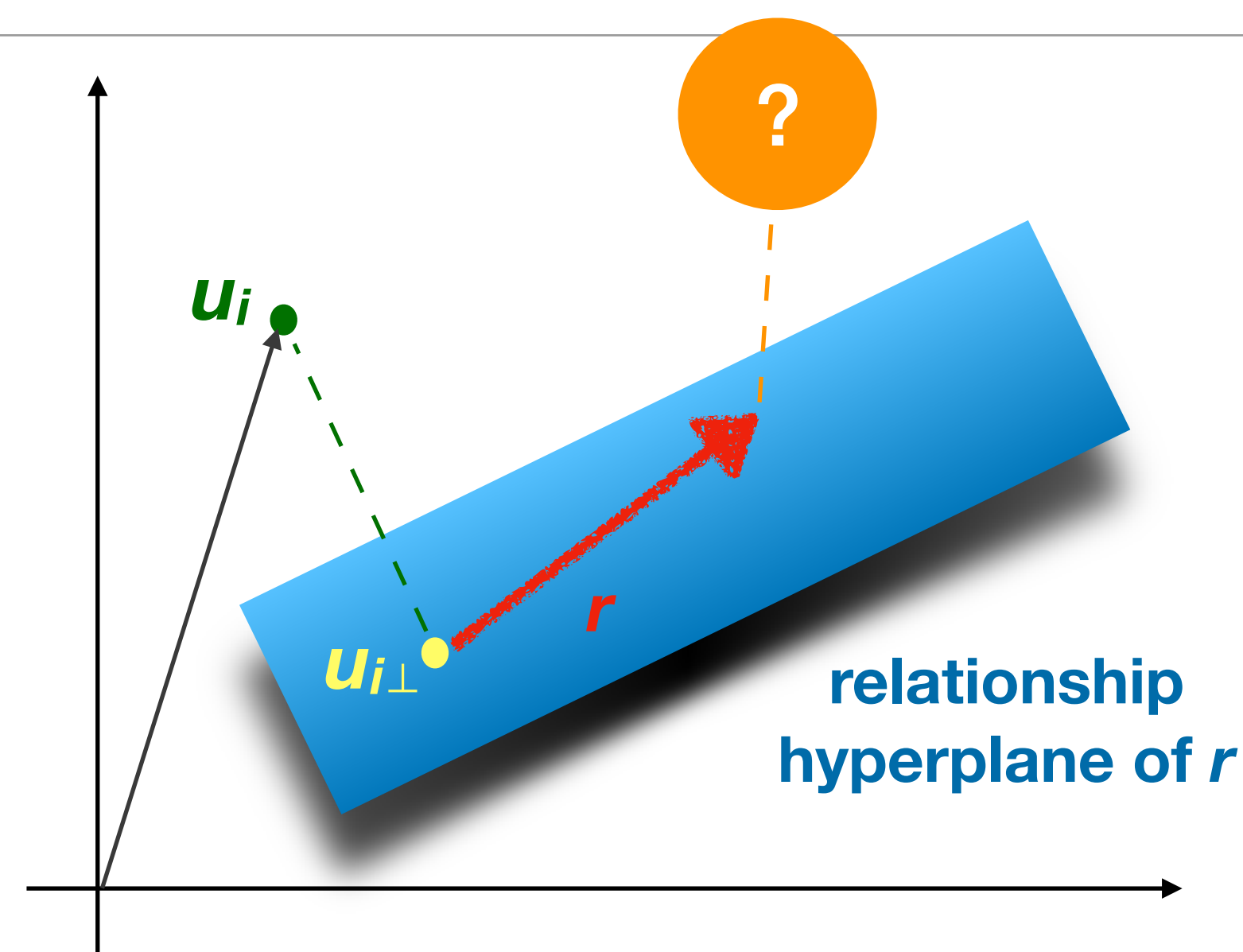
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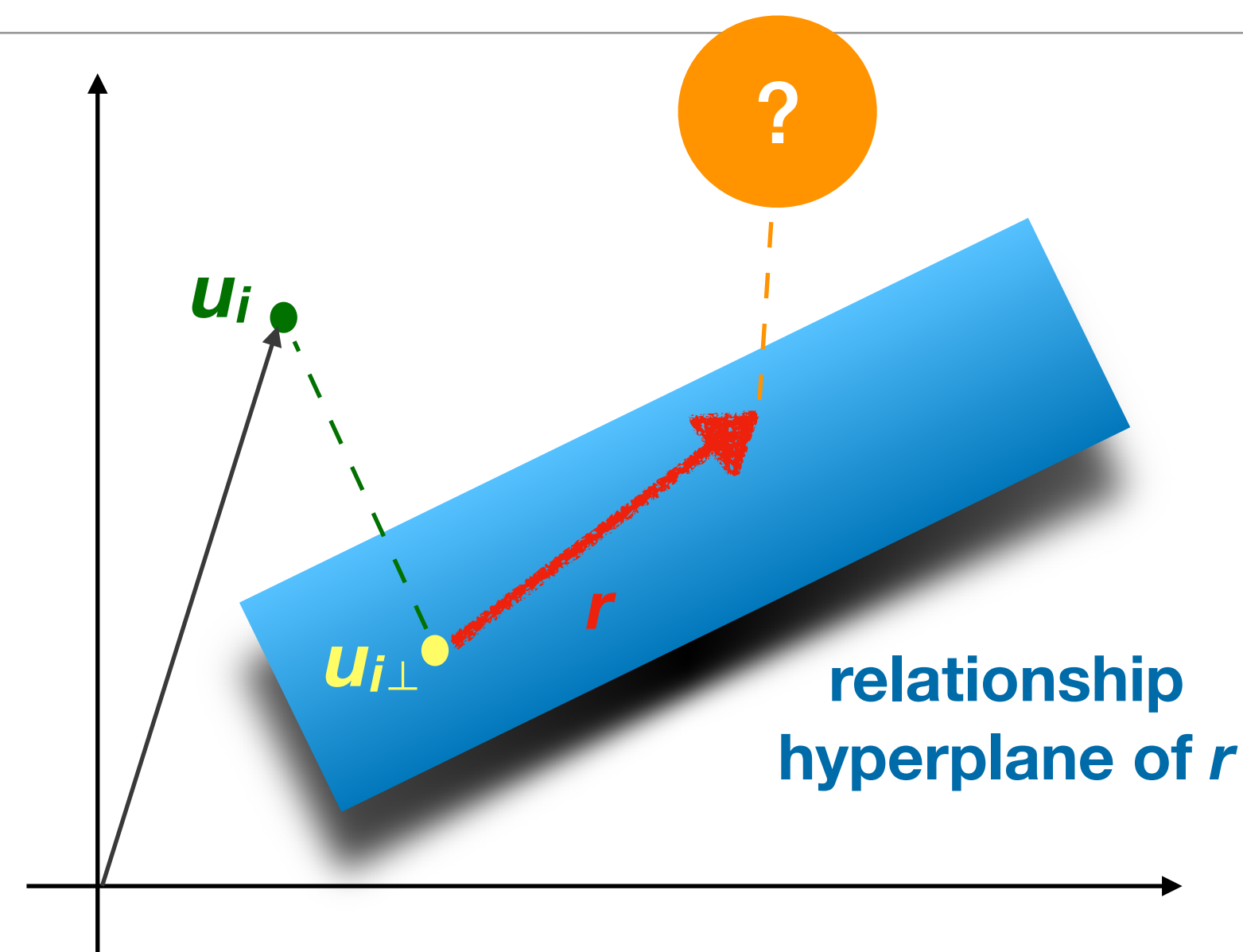


Model	Mean Rank		Mean Hits@N (%)							
	Raw	Filter	N=10		N=5		N=3		N=1	
			Raw	Filter	Raw	Filter	Raw	Filter	Raw	Filter
TransE	305	304	50.6	52.3	37.3	39.9	27.3	30.3	11.4	13.5
TransH	168	168	73.8	76.3	57.5	62.2	43.1	49.0	18.7	23.7
TransR	195	194	75.5	78.7	56.3	61.9	41.6	48.0	18.0	22.7
TransD	295	294	50.6	52.2	37.3	40.0	27.5	30.5	11.4	13.8
DKRL(CBOW)+TransE	5,579	5,577	5.5	6.7	3.4	3.9	2.3	2.3	0.9	1.1
<i>TransConv</i>	<b>36</b>	<b>35</b>	<b>83.5</b>	<b>86.9</b>	<b>63.0</b>	<b>68.8</b>	<b>46.5</b>	<b>53.0</b>	<b>20.0</b>	<b>24.8</b>

Evaluation results of link prediction on Facebook dataset.

# Experimental Results

- **Link prediction**
  - Using *conversational factors* significantly improves prediction **accuracy**
- *TransConv* outperforms other models, particularly for *sparse relationships* where there are fewer examples



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But heterogeneous, dependent structure makes it difficult to identify a NN structure/method that works well

*Current approaches:* padding, random walk sequences, randomization, aggregation over repeated local structure

Even though graphs are often very large, the connectivity structure can be very sparse, which limits effective sample size

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Multiple competing views of data: static/temporal, local/global, community/neighbors

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**Using inductive bias in latent space/model structure is helpful**

**Thanks**

*neville@cs.purdue.edu*  
*www.cs.purdue.edu/~neville*